

# An Adaptive Search Ordering For Rate-Constrained Successive Elimination Algorithms

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#### Introduction

- Block-matching algorithms (BMAs) must select the best candidate block (C) from a search area in one or many anchor frames to serve as a predictor for the content of the current block (B) (see Fig. 1).
- ▶ Beyond HD video formats (e.g., 4K or 8K), multiview video content and feature-rich video compression standards are all factors that require video encoders to consider more block sizes, more anchor frames, and use bigger search areas.
- ▶ The solution space for BMAs is so big, that state of the art approaches only consider a subset of that space and won't always find the optimal solution.
- ▶ We propose an adaptive ordering of block matching candidates that eliminates unnecessary block matching operations and allows for early termination.

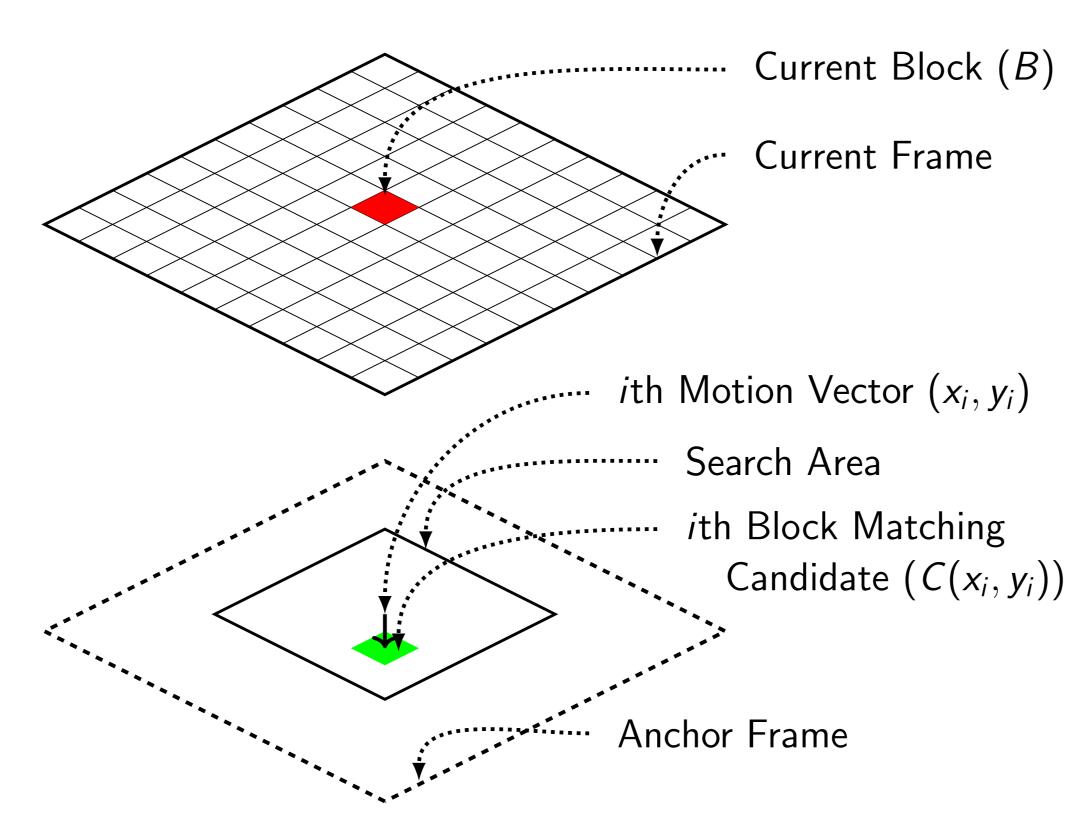


Figure 1: Block-matching consists of comparing candidate blocks ( $C(x_i, y_i)$ ) in a search area against the current block B using a cost function.

# Rate-Constrained Successive Elimination Algorithms

► The BMA evaluates candidates by computing the rate-constrained sum of absolute differences (RCSAD)

$$\mathsf{RCSAD}(x,y) = \sum |B - C(x,y)| + \lambda R(x,y)$$
. (1)

▶ The rate-constrained successive elimination algorithm (RCSEA) uses a 1D projection of the RCSAD, the rate-constrained absolute difference of sums (RCADS), as a lower bound for the RCSAD

$$RCADS(x,y) = \left| \sum B - \sum C(x,y) \right| + \lambda R(x,y) \leqslant RCSAD(x,y).$$
 (2)

► The RCSEA can use this lower bound to filters out unnecessary block matching operations. For example, let  $(x_{i-1}^*, y_{i-1}^*)$  be the best candidate found so far, if (3)

$$\mathsf{RCSAD}(x_{i-1}^*, y_{i-1}^*) \leqslant \mathsf{RCADS}(x_i, y_i) ,$$

then computing  $RCSAD(x_i, y_i)$  is unnecessary.

## Adaptive Search Ordering

- ▶ The efficiency of RCSEA depends on the ordering of block matching candidates.
- ▶ For example, the best filtering is achieved when  $(x_1, y_1)$  is the best candidate (see eq. 3).
- ▶ The proposed solution is outlined in Fig. 2. The main ideas are:
- ▶ Prune the candidates with eq. 3, but instead of  $(x_{i-1}^*, y_{i-1}^*)$ , we use RCSAD $(x_p, y_p)$  for each candidate, where  $(x_p, y_p)$  is the predicted motion vector (MVP).
- Sort in ascending order the retained candidates by RCADS.
- ▶ Perform BMA on the ordered candidates using *RCSEA*.
- ▶ Stop the BMA when eq. 3 is met for a candidate (early termination).

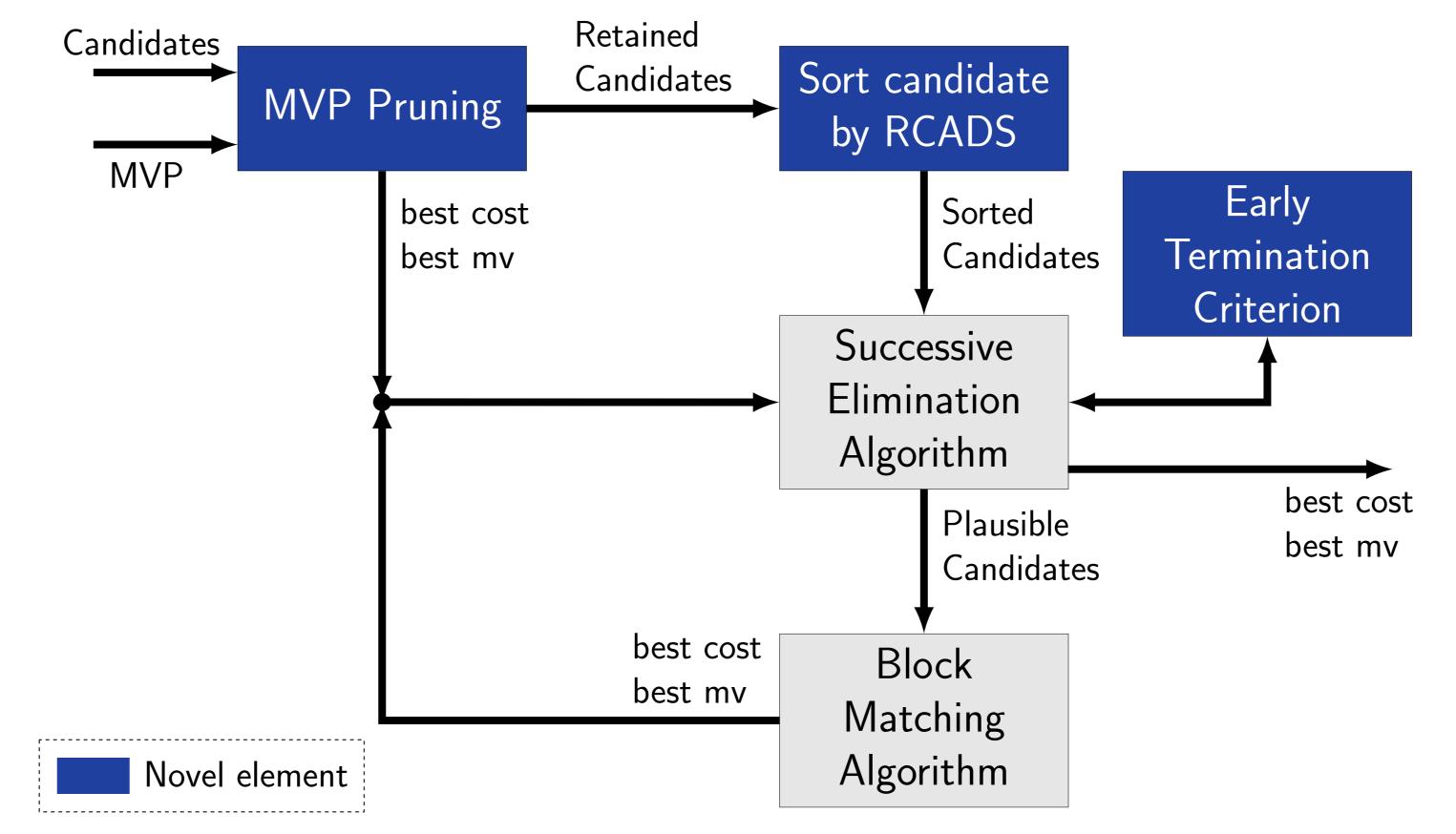


Figure 2: Outline of the proposed solution. See the paper for a complete algorithm.

### Early Termination

- Let  $(x_1, y_1)$  be the best candidate. The BMA will compute the RCSAD for  $\{(x_i, y_i) \mid \mathsf{RCADS}(x_i, y_i) \leqslant \mathsf{RCSAD}(x_1, y_1)\}.$
- ▶ Now, let the best candidate be unknown and let the candidates be sorted by RCADS. The BMA will compute the RCSAD for  $\{(x_i, y_i) \mid \mathsf{RCADS}(x_i, y_i) \leqslant \mathsf{RCSAD}(x_{i-1}^*, y_{i-1}^*)\}.$
- ▶ Both sets contain the same candidates.

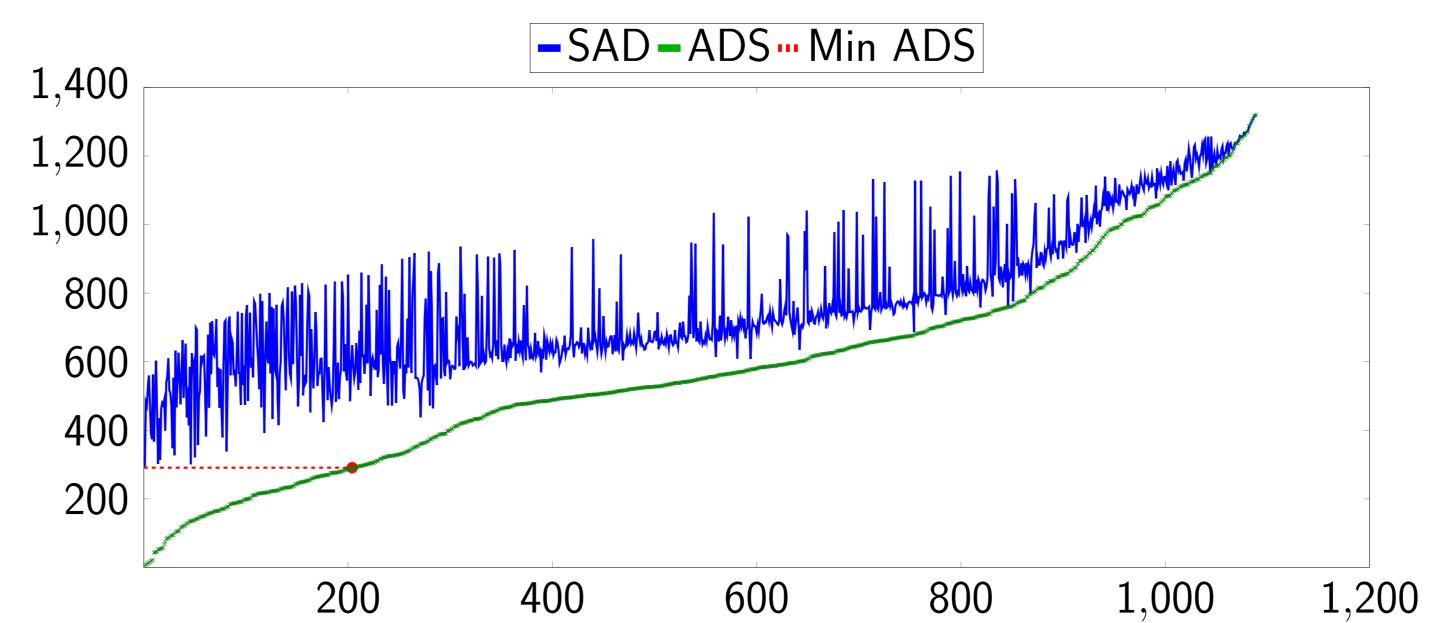


Figure 3: Block matching candidates sorted by RCADS. The early termination criterion is shown

### Experimental Results

- Our experiments where performed on the first 100 frames of Class C (832×480) video sequences ("Basketball Drill", "Party Scene", "BQ Mall" and "Race Horses") using the main profile.
- ▶ The results are presented by block sizes and by QP values in Fig. 4.
- ▶ The proposed algorithm is more effective for smaller block sizes.
- ▶ Smaller blocks comprise fewer pixels leading to more precise ADS values. This filters out more unnecessary cost function evaluations.
- ► As the QP increases, the effectiveness of the proposed algorithm also increases.



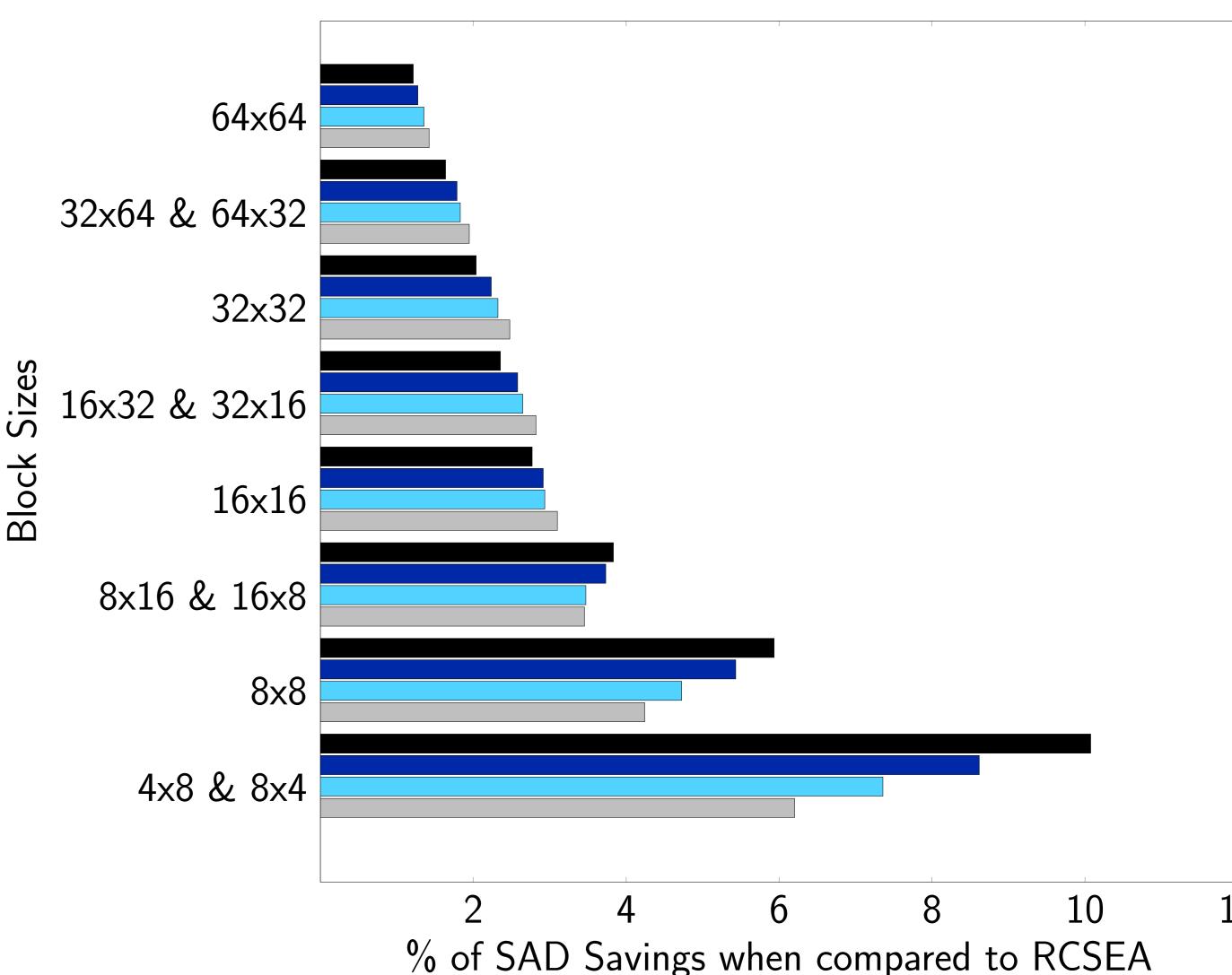


Figure 4: Percentage of SAD operations saved by the proposed solution.

#### Conclusion

#### We proposed:

- An adaptive search ordering for the motion estimation module that evaluates only necessary cost functions.
- An early termination criterion for the BMA.

#### Our experiments showed:

- ▶ Without our algorithm, an RCSEA using a spiral scan search ordering in the  $H.265/HEVC\ HM$  reference software would evaluate, on average, 3.5% of unnecessary cost functions.
- ▶ In some instances, the percentage of cost function evaluations can be reduced up to 15%.

