Ultrafast Carrier Dynamics in Graphene under a High Electric Field

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We investigated ultrafast carrier dynamics in graphene with near-infrared transient absorption measurement after intense half-cycle terahertz pulse excitation. The terahertz electric field efficiently drives the carriers, inducing large transparency in the near-infrared region. Theoretical calculations using the Boltzmann transport equation quantitatively reproduce the experimental findings. This good agreement suggests that the intense terahertz field should promote a remarkable impact ionization process and increase the carrier density.

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Graphene possesses many unique properties arising from its truly 2D honeycomb structure, and offers us a solid state playground of Dirac fermions [1]. One exciting property in graphene is its extraordinary transport property owing to its massless band structure and high Fermi velocity [2], which is significant for both fundamental physics and industrial applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications. Although great achievements of dc electron transport in graphene [2–6], current saturation restricts applications.

Thanks to recent advances in high-power and time-resolved terahertz (THz) technologies [9], we can apply electric fields of high strength (MV/cm) with a pulse width of ~100 fs to probe the ultrafast nonlinear optical properties of materials in the THz frequency region. For instance, novel carrier dynamics in semiconductors have been reported such as THz-field-driven mass anisotropy in doped InGaAs [10], and highly efficient carrier multiplication in GaAs quantum wells [11], to name only two. In graphene, S. Winnerl et al. have performed THz-pump THz-probe measurements, revealing that the excitation and relaxation dynamics of carriers strongly depend on the excitation frequency in the THz region [12]. In these studies, THz pulses are of picosecond duration, which is longer than the typical optical phonon emission time scale in graphene. A shorter pulse is required to prevail over current saturation caused by optical phonon emission.

In this Letter, we investigated ultrafast carrier dynamics under high electric field in graphene using 200 fs half-cycle THz excitation pulses and monitoring their dynamics with 50 fs long near-infrared (NIR) probe pulses. Large THz induced transparency is observed in the NIR region for the first time. Numerical calculations using the Boltzmann equation quantitatively reproduce the experimental findings and demonstrate the importance of efficient carrier multiplication by impact ionization in graphene. This multiplication achieved by ultrashort THz pulse excitation may drastically suppress the current saturation effect.

The sample used in our experiment is a commercial CVD graphene grown on Cu foil, which is transferred onto a SiO2 substrate. We have confirmed the sample’s single-layer nature and uniformity by confocal Raman imaging microscope [13]. The transmissivity of our sample at 800 nm is 97%, comparable with the value obtained from universal conductivity of intrinsic single layer graphene [1]. Because graphene is deposited on SiO2, substrate-induced inhomogeneity at the graphene-oxide interface gives rise to p-type doping with Fermi energy over 200 meV [14].

To investigate hot electron transport properties in graphene, we performed transient absorption measurement in the NIR region under intense THz excitation, as illustrated in Fig. 1(a). We used a collinear air plasma method for generation of intense half-cycle THz pulses [15][Fig. 1(b)]. An 800 nm laser pulse (Ti:Sapphire amplifier that delivers 3 mJ with 35 fs duration laser pulses) was split into two pulses for the THz generation (2.4 mJ) and the time-resolved transmission probe (<1 nJ). We used a collinear air plasma method for generation of intense half-cycle THz pulses. An undoped germanium substrate was inserted in the THz excitation line to remove any remaining 800 nm-pump beam after THz generation. The THz pulse was focused on the sample by an off axis parabolic mirror. With some time delay, the 800 nm probe pulse was also focused at the same spot on the sample. The spot size of the probe pulse (30 μm) was carefully taken smaller than that of the THz excitation pulse (80 μm) to ensure a homogeneous excitation. The probe light intensity after passing through the sample was measured with an amplified photodiode. A lock-in amplifier (SRS SR830), connected to the photodiode and referenced to the chopper that switched the excitation on and off at 500 Hz, was used to detect the probe
light intensity change by the THz excitation. The temporal waveform of the THz pulse was measured using an electro-optical sampling technique by replacing the sample with a 50-μm GaP crystal, in which THz-field-induced birefringence rotates the polarization of the probe pulse proportional to the field strength. Figure 1(c) shows a temporal profile of the THz pulse with a peak electric field of 300 kV/cm and a full-width at half-maximum of 100 fs. Notice that the spectrum of the THz pulse covers from 0.5 to 7 THz [inset of Fig. 1(c)] with the photon energy several tens of times smaller than that of the probe pulse. All measurements were performed at room temperature and under dehydrated air to suppress THz absorption from water vapors.

Figure 1(d) shows a typical THz induced differential optical density (OD) measurement as a function of time with a peak THz electric field of 300 kV/cm. To clarify the physical meaning observed here, we define the normalized differential OD by $\Delta OD/OD_{\text{ref}} = (OD_{\text{ex}} - OD_{\text{ref}})/OD_{\text{ref}}$ for $T/OD_{\text{ref}}$, where OD$_{\text{ref}}$ is the OD of graphene at 800 nm without THz pulse excitation, and OD$_{\text{ex}}$ is that with THz pulse excitation. The value of $-\Delta OD/OD_{\text{ref}}$ corresponds to the population occupation at the energy of an 800 nm transition. After THz pulse excitation, the differential OD immediately goes negative (e.g., graphene becomes transparent in the NIR region under THz pulse excitation) and returns to zero within 2 ps. Experimentally, the maximum value of $\Delta T$ reaches $5 \times 10^{-3}$ for a peak electric field of 300 kV/cm. This large induced transparency over 16% should be caused by electron filling or hole depletion of the corresponding energy levels.

Figures 2(a) and 2(b) show the temporal profile of induced NIR transparency for peak electric fields of 170 and 300 kV/cm. The maximum values of induced transparency drastically increase for the higher electric field, while carrier relaxation time tends to increase linearly with field strength. The origins leading to the nonlinearity will be discussed in subsequent paragraphs.

Figure 2(e) shows the maximum values of induced transparency as a function of a peak electric field. A power law with exponent 2.5 is found experimentally. This is in contrast with ultrafast optical pump-probe experiments [16,17], which reported a quadratic dependence on the electric field at low fluences and saturation for higher fluences. With optical excitation, the field dependence cannot exceed a power law with exponent 2 because of a limited number of interband transition dipoles [18,19]. The superquadratic dependence found here suggests nonlinear coupling between the THz field and electronic system, and can be explained by the rapid increase in the number of carriers with field strength.

As examined in detail in previous studies from THz to NIR regions [12,20,21], electromagnetic wave excitation...
The Boltzmann equation is as follows: The use of the semiclassical Boltzmann equation should be appropriate because the kinetic energy of carriers reaches several hundreds meV and much larger than the THz photon energy, so that interband polarization can be ignored. The Boltzmann equation is as follows:

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\frac{\partial}{\partial t} f_{\lambda}(k, t) = - \frac{q_{\lambda}}{\hbar} E(t) \frac{\partial}{\partial k} f_{\lambda}(k, t) + \int dk' \{ S^{\lambda-e}_{k,k'} + S^{\lambda-ph}_{k,k'} - S^{\lambda-e}_{k',k} - S^{\lambda-ph}_{k',k} \} + \int dk' \{ S^{II}_{k,k'} + S^{AR}_{k,k'} - S^{II}_{k',k} - S^{AR}_{k',k} \},
\]

where \( f_{\lambda}(k, t) \) is a distribution function of electrons and holes (\( \lambda = e, h \)), \( q_{\lambda} \) is the charge of carrier, and \( E(t) \) is the incident THz electric field on graphene at time \( t \). \( S^{\lambda-e}_{k,k'} \) represents intraband CC scattering rates with coulomb interactions [27]. Intervalley \( k-k' \) scattering is neglected for large momentum exchange [28]. \( S^{\lambda-ph}_{k,k'} \) represents intra- and interband phonon scattering rate with \( \Gamma \) and \( K \) optical phonon modes [28]. Electron-phonon coupling strength is from Ref. [29]. \( S^{II}_{k,k'} \) and \( S^{AR}_{k,k'} \) represent impact ionization (II) and Auger recombination (AR) rates [30], respectively. The last two terms (II and AR) change the number of carriers through interband CC scattering as in Fig. 3(l). The II process creates an extra electron-hole pair while losing the kinetic energy of another electron or hole, as schematically shown in Fig. 3. The AR is the inverse process of II, which reduces the number of carriers. The first term represents carrier acceleration on linear dispersion relation \( E = h v_F |k| \) (Dirac cone) with an electric field, where \( E \) is the energy of the carrier and \( v_F \) is the Fermi energy in graphene. In the second term, momentum-resolved hot phonon effects are included [28]. Acoustic phonon scattering negligibly contributes in our observation time scale and was not included in our calculations [12,28].

The occurrence of II and AR in graphene is controversial because of restrictions from energy and momentum conservation laws in the Dirac cone. Although some authors have stated that these processes are prohibited because of a limited number of possible initial and final momentum configurations [31], some experimental and theoretical studies have indicated the possibility of using these processes [12,24,25,27,30,32]. Here, we allow these processes by loosening the momentum conservation law by \( \Delta k = 2 \times 10^4 \) \( \text{cm}^{-1} \) (~1 meV in kinetic energy). This may come from imperfection of our CVD graphene, which possibly results in larger II and AR processes [24,33].

Calculated induced NIR transparency is plotted as a function of a peak electric field in Fig. 2(e) (solid line). The experimental results are quantitatively reproduced.

**FIG. 3** (color online). (a)–(e) Distribution function of holes in \( k \) space with various time delays. Dashed circles represent momenta corresponding to the energy of 800 nm transition. (f)–(j) Angle-resolved energy distribution of holes. Fermi-Dirac fitting is represented as a dashed line. Vertical arrows indicate the energy of 800 nm transition. (k), (l) Carrier scattering processes included in the calculation: carrier-carrier scattering (CC), optical phonon scattering (op), impact ionization (II) and Auger recombination (AR).
when II and AR processes are included. For comparison, the calculations by strictly applying conservation laws (without II and AR) are also plotted as a dashed line. In the latter case, the sublinear scaling with field strength clearly deviates from the experiment for the higher electric field because of rapid optical phonon scattering. We have to stress here that the only adjustable parameter is the initial Fermi energy, which is tuned to reproduce the magnitude of induced transparency in Fig. 2(e). The best-fitted Fermi energy is \(-280 \text{ meV}\), which is a reasonable value for graphene on a SiO2 substrate [14]. Note that the changes of the initial Fermi energy only offset the field dependence without affecting the power law. This good agreement indicated that efficient carrier multiplication by II prevails over AR under the high electric field condition.

To emphasize the effect of carrier multiplication, we plot the calculated carrier density as a function of time in Figs. 2(c) and 2(d). The number of carriers becomes almost five times larger than the initial number of carriers with a peak electric field of 300 kV/cm, resulting in the observed large induced transparency. Recovery of the absorption change at 800 nm is also calculated and shown as solid lines in Figs. 2(a) and 2(b). Our calculations qualitatively reproduce the field dependent relaxation time, which confirm the longer relaxation time at higher excitation density. This is due to the hot phonon effect [21,28].

Figures 3(a)–3(e) show calculated distribution of holes in the \(k\) space at various time delays for the maximum applied electric field of 300 kV/cm. Figures 3(f)–3(h) and 3(j) show the corresponding angle-resolved energy distribution of holes defined as \(f_h(E) = \langle f_h(E, \phi) \rangle_{\theta - \pi/4 < \phi < \theta + \pi/4}\) with the angle \(\theta\) in Fig. 3(a). Before THz pulse excitation, holes are distributed within Fermi energy with 300 K thermal fluctuation [Figs. 3(a) and 3(f)]. As a THz electric field is applied, the carrier distribution becomes an asymmetric shape [Figs. 3(b) and 3(g), the electric field is rapidly increasing in the positive direction], and keeps its asymmetry until the peak electric field [Figs. 3(c) and 3(h)], although the asymmetry decreases rapidly by optical phonon scattering. After the THz excitation pulse is passing through the sample, the distribution immediately recovers its symmetric shape [Figs. 3(d) and 3(i)] and returns back to the initial distribution by emitting optical phonons [Figs. 3(e) and 3(j)]. This argument is well confirmed by angle-resolved energy distributions fitted with Fermi-Dirac distribution in the THz field direction \(k\) [Figs. 3(f)–3(j)]. For instance, temperature in the \(k\) direction is 300 K before excitation and is increased to 2860 K after THz pulse excitation, due to the impact ionization process. This is consistent with experiment [Fig. 3(h)].

In conclusion, we reported the first observation of large THz-induced near-infrared transparency in graphene. Our results were compared with simulations using the Boltzmann equation and we proved that carrier multiplication occurs in graphene driven by high field and ultra-short THz pulses. The observed dependence of the rise in charge density on THz peak field strength indicates an interband impact ionization mechanism in graphene. The impact ionization process may suppress optical phonon emission by reducing kinetic energies of carriers while conserving current, which could promote efficient carrier transport suppressing current saturation.

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