

# The effect of air-entraining admixture and superabsorbent polymer on bond behaviour of steel rebar in pre-cracked and self-healed concrete

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## Abstract

This paper intends to study the effect of air-entraining admixture (AE) on self-healing method at rebar-concrete interface using superabsorbent polymer (SAP). AE with a constant dosage of 0.83 kg/m<sup>3</sup>, and 0.25% and 1.0% SAP dosages are considered. Two types of superabsorbent polymer with different chemical compositions and particle sizes are considered for the experimental tests. Pull-out test results of mixtures containing AE admixture are compared with those in non-AE concrete. Scanning electron microscopy/energy dispersive X-ray spectrometry (SEM/EDS) along with microscopic analysis is performed to study the healing products at crack surface and SAP macro voids around the rebar.. Overall, results indicate that AE admixture has a considerable impact on the performance of the self-healing method at the rebar-concrete interface especially for higher dosage of SAP (1.0%). This can be attributed to the internal voids networks around the

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21 rebar generated by AE admixture, which can ease the water transfer between SAP macro voids to  
22 participate in healing cracks after wet-dry cycles. SEM analysis shows that stalactites, healing  
23 products at the external surface of crack, are composed of a large amount of calcium and oxygen.  
24 **Keywords:** bond behaviour; air-entraining admixture; superabsorbent polymer; self-healing;  
25 pre-cracking phenomenon

## 26 **1 Introduction**

27 The interaction between reinforcing bar (rebar) and surrounding concrete, known as the “bond-  
28 slip” phenomenon, plays a crucial role in the structural behaviour of a reinforced concrete (RC)  
29 member. The bond-slip phenomenon affects the structural efficiency of different sub-elements in  
30 an RC frame including column [1, 2], beam [3], interior and exterior beam-column joint [4, 5], and  
31 slab [6, 7]. Improving bond characteristics can considerably affect the structural performance of  
32 these sub-elements along with the integrity of RC frame. Previous studies have shown that concrete  
33 composition has a considerable influence on bond properties including water-to-cement ratio [8,  
34 9], mineral admixture [10, 11], aggregate type [12, 13], and chemical admixture [14]. Among these  
35 variables, there is no specific study on the effect of air-entraining (AE) admixtures on bond  
36 characteristics of steel rebar in uncracked and pre-cracked specimens.

37 Air-entraining (AE) admixtures are organic surfactants which entrain a controlled quantity of air  
38 in concrete that is a uniformly dispersed discrete bubbles [15]. Content, size, spacing and specific  
39 surface of air voids are important parameters for AE concrete mixture. Regarding the size  
40 distribution of air voids, a wide range of values for different types of AE admixtures was obtained  
41 by previous studies. For instance, air void sizes with ranges of 0.25-1.0 mm [16], 0.10-2.0 mm  
42 [17], and air voids with a diameter larger than 0.1 mm (without specifying the max diameter) [18]

43 were reported by the literature for AE concrete mixtures. Initial water-to-cement ratio, type of AE  
44 admixture, and dosage of AE admixture considerably affect the size distribution of the air-void  
45 system [19]. AE admixtures, as a surfactant, reduce the surface tension of water, resulting in bubble  
46 formation and stabilization [20]. Uniform dispersion and appropriate stability are obtained by the  
47 mutual repulsion of the negatively charged air-entrainer molecules and the attraction of the air-  
48 entrainer molecules for the positive charges on the cement particles [21]. AE increases the  
49 workability and consistency of concrete [22-24], so that mixtures with AE admixture have a higher  
50 slump value as compared to normal concrete (NC) at the same water content. On the other hand,  
51 the presence of air bubbles acts as a lubricant. AE concrete is less sensitive to bleeding and  
52 segregation than is non-AE concrete [15]. AE admixtures have no noticeable impact on the  
53 hydration rate of cement or on the heat evolved by that process. The strength of the hardened  
54 concrete is decreased as the amount of air is increased.

55 Most of the previous studies on the field of AE concrete concentrated on the resistance of mixtures  
56 exposed to low temperatures (winter exposure) and freeze-thaw cycles in water-saturated RC  
57 members such as outdoor slabs, pavements and bridges [25, 26], i.e., durability problem in cold  
58 climates. Perenchio et al. (1990) [27] postulated that the diffusion of gel water to capillary pores  
59 encompassing ice causes the growth and expansion of ice lenses, results in generating micro  
60 cracks. The freezing cycle increases the width of these micro-cracks, which afterward filled with  
61 water during thawing cycles. This cycle causes a rapid deterioration of concrete. Frost damage of  
62 concrete can be attributed to the osmotic pressure, in which unfrozen water is compelled to  
63 capillary pores under a salt concentration gradient [28]. The growth of ice in such locations causes  
64 considerable degradation. The resistance of hardened concrete to this type of damage is  
65 considerably improved by the use of AE admixtures [20, 29-33]. This is achieved by the presence

66 of stabilized entrained-air bubbles network within concrete mixture generated by AE admixture,  
67 acting as expansion chambers to accommodate the ice formed within the capillaries [34, 35].  
68 Moreover, for a given workability, AE concrete is more durable, as compared to the non-AE  
69 concrete by providing lower water-to-cement ratio [36]. Total volume of the entrained air, average  
70 volumic surface, and spacing of the air bubbles are the fundamental characteristics of this “air  
71 bubble network”, which is comprehensively discussed by Gagné (2016) [37]. These air bubbles  
72 need to be homogeneously dispersed in the mix, which can be characterized by what is called the  
73 “spacing factor of the bubbles network”.

74 Despite the extensive studies on the effect of stabilized air bubble network (provided by AE  
75 admixture) on durability properties of concrete, there is no specific study to determine the effect  
76 of AE admixture on bond properties of steel rebar embedded in intact and internally-damaged  
77 concrete specimens. Moreover, there is no study so far demonstrating the effect of AE admixture  
78 on the autogenous healing capacity of concrete with or without healing agents at the rebar-concrete  
79 interface. Hence, the present study intends to fill these research gaps by using AE admixture within  
80 the mixtures to partly or entirely mitigate internal damages, due to the pre-cracking phenomenon,  
81 at the rebar-concrete interface using the self-healing method. Superabsorbent polymer (SAP) is  
82 used in the present study to accelerate the self-healing capacity of concrete. Regarding SAP, most  
83 of the previous researches only concentrated on autogenous shrinkage [38, 39], drying shrinkage  
84 [38], fresh properties and passing ability [40], tensile strength [41], compressive strength [40, 42,  
85 43], chloride ion permeability [39], and self-sealing and –healing cracks [44-46]. However, only  
86 NC was studied in the literature. Moreover, only a few studies focused on the self-healing method  
87 by SAP to mitigate internal damages at the rebar-concrete interface [47, 48]. Additionally,  
88 although there is a growing tendency to study the pre-cracking phenomenon in steel-congested

89 regions such as beam-column joints and shear walls [49-51], only NC was considered by the  
90 literature. Hence, to extend the previous study for the cold regions, where using AE admixture is  
91 necessary, the main objectives of the present study are as follows:

92 1- How much does the AE admixture affect the bond strength of steel rebar in pre-cracked  
93 concrete?

94 2- How much AE admixture is efficient for the self-healing method by SAP at the steel rebar-  
95 concrete interface?

96 To address these questions, an extensive experimental plan is conducted in the present study.  
97 Results are comprehensively compared with the results of a recently published paper by authors  
98 for NC [47]. Three main statuses of specimens are used including uncracked, pre-cracked, and  
99 healed specimens. Statistical analysis is also carried out, to identify the most significant factors  
100 affecting performance of the self-healing method.

## 101 **2 Experimental program**

### 102 **2.1 Material properties and experimental plan**

103 Five concrete mixtures are considered for this study to compare the results between AE concrete  
104 with non-AE concrete (reported by recently published paper by authors [47]). Mixtures were  
105 designed to determine the effect of different parameters including (a) SAP percentages; (b) SAP  
106 size and chemistry; (c) concrete flowability; and (d) AE admixture on bond behaviour of  
107 uncracked, pre-cracked, and healed specimens. The concrete composition of AE mixtures is  
108 illustrated in Table 1. Details of non-AE mixtures for both NC and SAP-modified NC were  
109 mentioned in Mousavi et al. (2020) [47]. General use (GU) cement was used for all mixtures with

110 a density of  $3.15 \text{ g/cm}^3$ . Natural sand with a maximum grain size of 1.25 mm and a specific gravity  
111 of 2.68, and gravel with a nominal maximum diameter of 14 mm and a particular gravity of 2.68  
112 were considered for mixtures. The SAP was added at a range of 0.0-1.0 wt.% of cement for non-  
113 AE concrete and only 0.25% and 1.0% for AE-contained mixtures. To adjust the flowability of  
114 concrete mixtures, superplasticizer was added, at different proportions. AE concrete mixtures  
115 contained an aqueous solution compound of synthetic chemicals by  $0.83 \text{ kg/m}^3$  of concrete  
116 mixture, with a specific gravity of 1.006, 7.5% of solids by weight, and a pH of 11.0.

117 Two different types of SAP were considered in this experimental study including (1) SAP-1, a  
118 cross-linked copolymer of acrylamide and potassium acrylate with a maximum particle size of 500  
119  $\mu\text{m}$ . SAP-1 had water absorption of 249 g/g (gram water per gram of SAP) and 25 g/g in deionized  
120 water and pore solution, respectively; (2) SAP-2, a crosslinked anionic polyacrylamide with a  
121 maximum particle size of 150  $\mu\text{m}$ . SAP-2 had water absorption of 170 g/g and 25 g/g in deionized  
122 water and pore solution, respectively. The water absorption capacity of SAPs was measured by  
123 three different methods [47] including (1) the tea bag method; (2) the slump test method; and (3)  
124 the water desorption method (the absorption of a centrifuged cement pore solution). Both SAP  
125 types were produced through the bulk polymerization method, where blocks of polymers were  
126 powdered into irregular-shaped powder [47]. The specific values  $d_{10}$ ,  $d_{50}$ , and  $d_{90}$  correspond to  
127 sphere diameters that have volumes equal or larger than 10 vol%, 50 vol%, and 90 vol% of the  
128 total volume of the particles, respectively. The median particle size ( $d_{50}$ ) of dry SAP particles  
129 were 260  $\mu\text{m}$  and 47  $\mu\text{m}$  for SAP-1 and SAP-2, respectively. The small diameters ( $d_{10}$ ) of dry  
130 SAP particles were 92  $\mu\text{m}$  and 13  $\mu\text{m}$  for SAP-1 and SAP-2, respectively. The large diameters  
131 ( $d_{90}$ ) of dry SAP particles were 450  $\mu\text{m}$  and 92  $\mu\text{m}$  for SAP-1 and SAP-2, respectively. Specific  
132 gravity values of SAP-1 and SAP-2 are 1.51 and 1.49, respectively. Bulk densities of SAP-1 and

133 SAP-2 were 0.82 and 0.84, respectively. Specimens were initially cured 28 days in the moisture  
134 room at 97.3% RH and 23 °C. Those healed specimens, which were subjected to wet-dry healing  
135 cycles, kept in the curing tank for longer periods of 14 and 28 days (20 °C, 60% RH) after pre-  
136 cracking. One wet-dry healing cycle represents 24 hours in water followed by 24 hours in dry  
137 condition (normal atmospheric or laboratory-controlled conditions). Consequently, 7 and 14 cycles  
138 took 14- and 28-day wet-dry healing cycles, respectively. Configurations of concrete mixtures  
139 studied in the present study are illustrated in Table 2. Reference mixes were designated by “R”,  
140 “RA-1”, and “RA-2”. Character “A” in the names of some mixtures determines AE mixtures. “S1”  
141 and “S2” correspond to mixtures containing SAP-1 and SAP-2 respectively. Numbers of 25, 50,  
142 and 100 in some mixtures show 0.25%, 0.50%, and 1.0% SAP by weight of cement respectively.  
143 Cylindrical specimens with diameter of 150 mm and height of 113 mm were considered for pull-  
144 out specimens. Embedded length was  $5d_b$  for all specimens. Steel rebar with nominal diameter of  
145 10 mm, rib spacing of 13.22 mm, and rib height of 1.89 mm was used in the experimental  
146 specimens. Specified yield strength and ultimate tensile strength of steel rebar were 432 MPa and  
147 620 MPa, respectively. Three repetitions were considered for uncracked specimens. However, due  
148 to the brittle nature of splitting tests (to simulate the pre-cracking phenomenon), specimens with  
149 different crack widths were obtained so that less than 3 specimens were tested for some pre-  
150 cracked and healed specimens. The designation of specimens is as follows: first character in  
151 specimen identification describes mixture type including R=reference; RA2=reference mix with  
152 AE admixture; 25S1=0.25% SAP-1; 25S2=0.25% SAP-2; 50S1=0.5% SAP-1; 100S1=1.0% SAP-  
153 1; 25S1A=0.25% SAP-1 with AE admixture; 25S2A=0.25% SAP-2 with AE admixture; and  
154 100S1A=1.0% SAP-1 with AE admixture. The second character indicates the initial crack width  
155 before healing; For instance, C0.3= crack width of 0.30 mm. The last character determines the

156 healing period so that 14H and 28H show specimens after 14- and 28-day healing periods,  
157 respectively.

## 158 **2.2 Experimental procedure**

159 The pre-cracking test was carried out as detailed in Mousavi et al. (2019 & 2020) [47, 49, 50].  
160 Controlled Brazilian tests (splitting), recommended by Desnerck et al. (2015) [52], were used to  
161 produce different crack widths parallel to the rebar direction (Fig. 1(a)). To control crack opening,  
162 crack gauges were installed at both sides of specimens, along with a manual measurement of crack  
163 widths. Based on empirical observations, the displacement rate of 0.11-0.15 mm/min was  
164 considered for splitting tests. Crack widths ranging from 0.10 to 0.50 mm were obtained by the  
165 splitting tests. Then, direct pull-out tests were conducted after three stages of uncracked, pre-  
166 cracked (by a splitting test), and healed (after 14 and 28 days re-curing) specimens with a  
167 displacement rate of 0.50 mm/min (Fig. 1(b)). Slip was measured at the free-end of the steel rebar  
168 during the pull-out test. To prevent corrosion influences for 28-day healing periods, the heat-  
169 shrinkable tube was used at both end sides of specimens (Fig. 1(c)). To analyse the results,  
170 maximum bond stress (or bond strength,  $\tau_u$ ), residual bond stress which corresponds to the bond  
171 stress value observed at an almost constant plateau, following the descending branch of the bond-  
172 slip curve and starting at a slip of 10 mm ( $\tau_r$ ), and area under the bond-slip curve until the slip of  
173 12 mm (absorbed energy) are used in the present study. Moreover, as recommended by RILEM  
174 [53], average bond stress ( $\tau_m$ ) is used as the arithmetic mean of bond stresses of  $\tau_{0.01}$ ,  $\tau_{0.1}$ , and  
175  $\tau_{1.0}$  corresponding to slips of 0.01 mm, 0.10 mm, 1.0 mm, respectively.



### 176 2.3 Experimental results

177 Three main characteristics of average bond stress ( $\tau_m$ ), maximum bond stress called bond strength  
178 ( $\tau_u$ ), and residual bond stress ( $\tau_r$ ) are considered in the following subsections to analyse the  
179 results. General observations showed that uncracked and cracked specimens with  $w < 0.15$  mm  
180 experience pulling out the rebar from the concrete cylinder without noticeable propagation of  
181 splitting cracks (perpendicular to the rebar) (Fig. 2(a)). This corresponds to the high value of  
182 concrete cover-to-rebar diameter ratio, providing enough confinement surrounding the rebar in  
183 uncracked specimens to completely shear-off concrete key between two adjacent ribs. However,  
184  $w > 0.15$  mm leads to complete splitting of the specimens and slippage out of the rebar (Fig. 2(b)).  
185 Large initial cracks cause rebar-concrete surface separation and a considerable reduction in  
186 concrete confinement surrounding the rebar. As explained in literature [50], this surface separation  
187 due to the pre-cracking phenomenon change the failure mode from pull-out (shear-off concrete  
188 key) to crushing a wedge-shaped concrete block on the rib front face (splitting failure mode).  
189 Similar observations were obtained for failure modes of healed specimens so that splitting failure  
190 modes were observed for partly and fully recovered bond strength specimens. Results show that  
191 the accelerated self-healing method by SAP cannot improve the failure mode after healing periods.  
192 Compressive strength of concrete mixtures is shown in Fig. 3. Generally, results indicate that  
193 25S1A is the optimum mixture among other air-entrained mixtures. Results show that using AE  
194 causes considerable reduction effect on the compressive strength so that strength reductions of  
195 18.6%, 7.0%, 16.5%, and 33.2% are obtained for mixtures of RA-1, 25S1A, 25S2A, and 100S1A  
196 respectively (Fig. 3(a)). Moreover, results show that AE has lower impact on the compressive  
197 strength of concrete containing SAP with larger particle size (25S1A) as compared to the smaller  
198 size SAP (25S2A). Besides, results show that AE has higher devastating impact on the

199 compressive strength of mixture containing higher dosage of SAP (100S1A) as compared to the  
200 lower dosage (25S1A). As illustrated in Fig. 3(b), the present study proposes Eqs. (1) and (2) for  
201 the 28 days compressive strength of non-air-entraining and air-entraining SAP concrete mixtures  
202 respectively, as a function of the total water-to-cement ratio ( $W_T/c$ ), as follows:

$$f'_c = 152.7e^{-2.31(W_T/c)} \quad (1)$$

$$f'_c = 163.62e^{-3.0(W_T/c)} \quad (2)$$

203

### 204 2.3.1 Uncracked concrete

205 Results of uncracked concrete are shown in Fig. 4 for all mixtures. To compare all mixtures, the  
206 effect of concrete compressive strength is eliminated by normalization. This is achieved by  
207 dividing these stresses by the square root of the concrete compressive strength including  
208 normalized average bond stress,  $\tau_m^* = \tau_m/\sqrt{f'_c}$ , normalized bond strength,  $\tau_u^* = \tau_u/\sqrt{f'_c}$ , and  
209 normalized residual bond stress,  $\tau_r^* = \tau_r/\sqrt{f'_c}$ . Results indicate that RA-2 and R mixtures have  
210 the highest normalized average bond stress among other mixtures (Fig. 4(a)). In the case of  
211 normalized bond strength, RA-2 has higher values (4.2), as compared to other mixtures (Fig. 4(b)).  
212 Similar results are observed for normalized residual bond stress (Fig. 4(c)) and energy dissipated  
213 by the bond mechanism (Fig. 4(d)). This can be attributed to the higher slump value of RA-2,  
214 which affects the rebar-concrete bond strength. Generally, results indicate that concrete  
215 composition has a significant impact on bond properties of steel rebar embedded in uncracked  
216 concrete specimen, which was similarly confirmed by the literature [10, 54-56]. Only lightweight  
217 aggregate concrete (LWC) was considered in concrete design codes due to a lower bond strength

218 of steel rebar in LWC as compared to NC, while results of the present study emphasize that specific  
219 specifications are required for different concrete mixtures.

### 220 **2.3.1.1 Effect of SAP percentage on bond strength of AE and non-AE concrete**

221 Fig. 5 shows the effect of SAP percentage on the bond response of uncracked specimens. General  
222 results show that SAP percentage higher than 0.25% leads to a significant reduction in the  
223 normalized bond properties in uncracked specimens due to the higher number of SAP macro pores  
224 around the rebar. In the case of low dosage of SAP (0.25%), 2.9% and 0.0% bond strength  
225 reductions are obtained for AE and non-AE concrete mixtures, respectively. As mentioned in  
226 literature, this slightly bond strength reduction of a low dosage of SAP can be compensated by  
227 using fiber within the mixture to control the crack width [57, 58]. In the case of non-AE concrete,  
228 general results show that a higher dosage of SAP causes a considerable reduction in bond  
229 properties, especially for the residual bond stress (Fig. 5(a)). Among the bond properties, SAP  
230 dosage has higher effect on the maximum bond strength (44.1%), while lower impact on the  
231 residual bond stress (77.8%) for non-AE concrete. However, different trends are followed by AE  
232 concrete, so that approximate reduction of 50.0% is observed for all bond properties of 100S1A  
233 mixture (Fig. 5(b)). In the case of 0.25S1A mixture, 4.8% and 10% increases were recorded for  
234 the average and residual bond stress, respectively. This finding can confirm the fact that AE  
235 admixture is in good combination with 0.25% SAP for using in concrete mixtures. Despite the  
236 findings of the present section, more experimental studies are necessary for future works to  
237 confirm the obtained results.

### 238 **2.3.1.2 Effect of AE admixture on bond strength of AE and non-AE concrete**

239 In the case of reference mixture (R), AE admixture has no considerable effects on the maximum  
240 and average bond stress (Fig. 6(a)), while 44.0% reduction is obtained for the residual bond stress.  
241 For 0.25% SAP-1, maximum and residual bond stresses are the same for both AE and non-AE  
242 mixtures, while the average bond stress of 25S1A mixture is 29.0% more than that of 25S1 mixture  
243 (Fig. 6(b)). Similar results are obtained for 1.0% SAP-1 (Fig. 6(d)). However, results show that  
244 AE admixture has negative impacts on bond properties of SAP-2, so that 22.0%, 30.0%, and 62.0%  
245 reductions of average bond stress, bond strength, and residual bond stress are obtained respectively  
246 for using AE admixture (Fig. 6(c)), which is similar to the trend of the reference mixture (R, Fig.  
247 6(a)). Hence, comparable and higher bond properties of SAP-1 presented in Fig. 5(b), and Fig. 6(b  
248 and d) show the fact that SAP-1 is more adaptable with AE admixture when compared with SAP-  
249 2.

### 250 **2.3.1.3 Effect of SAP particle size and type on bond strength of AE and non-AE concrete**

251 The effect of SAP particle size (and/or chemistry) is shown in Fig. 7. Bond properties are  
252 normalized by the square root of the concrete compressive strength of mixtures ( $\tau/\sqrt{f'_c}$ ). Results  
253 show that in the case of non-AE mixtures, SAP-2 has higher bond properties as compared to SAP-  
254 1. However, the results of Figs. 6 and 7 indicate that SAP-1 is more adaptable with AE admixture  
255 as compared to SAP-2. This can be attributed to different chemical compositions of SAP used,  
256 changing their absorption behaviours including total capacity and sorption kinetics. Moreover,  
257 different sizes of these healing agents ( $d_{50_{SAP-1}} \gg d_{50_{SAP-2}}$ ) can affect the absorption kinetics  
258 and microstructure of concrete mixture. Using different types of SAP changes the interfacial  
259 transition zone (ITZ) around the rebar, which is different from the effect of SAP on concrete

260 compressive strength [10]. In this context, Mousavi et al. (2020) [52] showed that SAP-2 produces  
261 a higher number of pores in paste around the rebar with a smaller void size. Therefore, the porosity  
262 pattern of SAP-2-contained concrete is different from SAP-1-contained concrete. A similar trend  
263 is reported by the literature [9, 10, 59], where the effects of water-to-cement ratio (w/c) and  
264 concrete composition were confirmed at ITZ around the rebar. It is worth mentioning that as the  
265 chemical part of SAP used is out of the scope of the present study, more experimental studies are  
266 necessary for future works to highlight the obtained results.

### 267 2.3.2 Pre-cracked concrete

268 Results of 100 pre-cracked pull-out specimens (excluding healed specimens) are summarized in  
269 Fig. 8 by the normalized reduced bond ratio  $((\tau)_c/(\tau)_{un})$  versus crack width-to-rebar diameter  
270 ratio  $(w/d_b)$ . Parameters of  $(\tau)_c$  and  $(\tau)_{un}$  corresponding to the bond properties of cracked and  
271 uncracked specimens, respectively. The significant impacts of the pre-cracking phenomenon on  
272 the average bond stress, bond strength, and residual bond stress are clear. Results show that  
273 residual bond stress is considerably affected by the initial induced cracks, so that even small crack  
274 widths cause more than 50.0% reduction in bond strength. However, three out of trend data is  
275 recorded for the residual bond stress with  $\tau_c > \tau_u$ . The following equations are proposed for  
276 reduced bond ratio after induced crack width:

$$\left(\frac{(\tau)_c}{(\tau)_{un}}\right)_m = 352.3 \left(\frac{w}{d_b}\right)^2 - 36.4 \frac{w}{d_b} + 1.0 \quad (3)$$

$$\left(\frac{(\tau)_c}{(\tau)_{un}}\right)_u = 26160.4 \left(\frac{w}{d_b}\right)^3 - 1609.2 \left(\frac{w}{d_b}\right)^2 + 1.67 \frac{w}{d_b} + 1.0 \quad (4)$$

$$\left(\frac{(\tau)_c}{(\tau)_{un}}\right)_r = 533.74 \left(\frac{w}{d_b}\right)^2 - 46.5 \frac{w}{d_b} + 1.0 \quad (5)$$

277 For uncracked specimens ( $w = 0$ ), proposed equations are equal to one, showing  $(\tau)_c = (\tau)_{un}$ .  
 278 These equations are obtained for  $0 < w/d_b < 0.05$ . Moreover, only nominal  $d_b = 10$  mm rebar  
 279 is used to normalize the initial crack width. So, more experimental studies with different values of  
 280  $w/d_b$  are necessary to be performed by future studies to confirm the proposed trend. To determine  
 281 the effect of AE on the pre-cracking phenomenon, the results presented in Fig. 8 is divided in two  
 282 separate groups of mixtures with AE and mixtures without AE for the average bond stress, the  
 283 bond strength, and the residual bond stress (Fig. 9). Overall, trends obtained for AE-contained  
 284 mixtures show that AE causes a higher bond reduction factor, leading to being less sensitive to the  
 285 internal damages due to the pre-cracking phenomenon (Fig. 9(a)). Similar results are obtained for  
 286 the bond strength and the residual bond stress (Figs. 9(b) and (c)). As crack width increases, this  
 287 deviation increases. Generally, results indicate that concrete composition has a significant impact  
 288 on bond properties of steel rebar embedded in pre-cracked concrete, which was similarly  
 289 confirmed by previous studies [47, 54]. Proposed equations for predicting bond reduction factors  
 290 are illustrated in Fig. 9. The effect of AE admixture on the pre-cracking phenomenon (i.e. bond  
 291 properties) is illustrated in Figs. 10, 11, and 12 for the average bond stress, the bond strength, and  
 292 the residual bond stress, respectively. General results of bond properties reduction show that  
 293 concrete mixtures containing AE admixture are less sensitive to the pre-cracking phenomenon  
 294 (higher  $(\tau)_c/(\tau)_{un}$  ratio), as compared to the non-AE concrete mixtures. This may be attributed

295 to the high flowability (slump flow) of AE mixtures, which is shown in Table 2. Similar  
296 observation was confirmed by literature [54], where SCC mixtures showed less sensitivity to the  
297 pre-cracking phenomenon as compared to NC.

### 298 2.3.3 Healed concrete

299 An improvement factor (IF) is defined in this section by Eq. (6) to measure the performance of  
300 SAP and AE for healing cracks at the rebar-concrete interface in different mixtures. As *IF*  
301 increases, the healing efficiency of the mixture increases. Zero value of IF corresponds to the  
302 specimens with lower or comparable bond properties than the cracked specimen with constant  
303 crack width ( $\tau_{Healed} \leq \tau_{Precracked}$ ), while  $IF > 0$  represents the healed specimens with higher  
304 bond properties as compared to those of pre-cracked specimens ( $\tau_{Healed} > \tau_{Precracked}$ ). It is  
305 necessary to emphasize that due to the brittle nature of concrete in tension, different crack widths  
306 were obtained by splitting tests. Hence, to compare bond results of healed specimens with cracked  
307 ones, bond reduction-crack width curves were used to predict bond properties of cracked  
308 specimens, in the case that different cracks were generated.

$$IF = \left[ \frac{\tau_{Healed} - \tau_{Precracked}}{\tau_{Uncracked} - \tau_{Precracked}} \right] \times 100 \quad (6)$$

309 A total number of 63 healed specimens for 14- and 28-day healing periods (in water tank) were  
310 tested in the present study. Improvement factor for the average bond stress ( $IF_{\tau_m}$ ) with a  
311 determined standard deviation (SD) is illustrated in Fig. 13 for all mixtures. Considerable healing  
312 of 0.15 mm crack widths after 28-day healing periods by 100S1A mixture is clearly depicted in  
313 Fig. 13, which is higher than 100% ( $IF_r=152.6\%$ ). However, a high SD is obtained for this case.

314 In this field, the reference mixture improved the average bond stress ( $\tau_m$ ) by 22.0% and 8.4% for  
315 crack widths of 0.30 mm and 0.40 mm, respectively. Moreover, mixtures of 25S1, 50S1, 100S1,  
316 25S1A, and 25S2A improved self-healing capacity up to  $IF_{\tau_m} \leq 25.4\%$  for average bond stress.  
317 Results of bond strength are more important as compared to other results, as this parameter affects  
318 directly structural and anchorage capacity. Similar to the average bond stress, concrete mixtures  
319 containing 1.0% SAP (100S1A and 100S1A) have significant improvement factor of bond strength  
320 (Fig. 14). General results of  $IF_{\tau_u}$  indicate that a reference mixture without a healing agent has a  
321 low improvement factor (5.7%), as compared to SAP mixtures. In this field, mixtures of 25S1,  
322 50S1, 25S1A, and 25S2A show  $IF_{\tau_u} \leq 58.0\%$ . It is clearly observed that SAP has a real potential  
323 of self-healing capacity and mitigating damage due to the pre-cracking phenomenon at the rebar-  
324 concrete interface. Similar results of the residual bond stress healing ( $IF_{\tau_r}$ ) are obtained for  
325 mixtures of 50S1, 100S1, and 100S1A (Fig. 15). Compared to the bond strength and the average  
326 bond stress, a lower improvement factor is observed for the residual bond stress of other mixtures.  
327 The general trend observed in Figs. 13-15 shows that SAP has considerable influences on healing  
328 cracks for mitigating damages, especially for mixtures of 50S1, 100S1, and 100S1A.

329 Bond-slip curves of 100S1A mixtures are illustrated in Fig. 16 for the pre-cracked and the healed  
330 specimens. Due to the low tensile strength of mixtures containing 1.0% SAP and AE, crack width  
331 of 0.15 mm is considered in the splitting test for this type of mixture. Pull-out failure modes are  
332 observed for this small crack width, which is obvious from the bond-slip curves, where no sudden  
333 drop presence after the maximum bond stress (Fig. 16(a)). Results show that the bond strength is  
334 considerably increased after both 14- and 28-day healing periods (Fig. 16(b)). Moreover, slip  
335 corresponds to the maximum bond stress is also increased along with strength recovery. Initial  
336 ascending parts of the bond-slip curve for different specimens are shown in Fig. 16(c). Results



337 show that the healed specimens have higher initial stiffness as compared to the cracked specimens.  
338 A similar observation is achieved for the residual bond stress (Fig. 16(d)). Energy absorbed  
339 (dissipated) by bond mechanism is also measured by the area under the bond-slip curve up to the  
340 slip of 10 mm, which is illustrated in Fig. 16(e). Results show that the self-healing method by 1.0%  
341 SAP significantly increased the absorbed energy, as compared to the cracked specimens. Overall,  
342 results show that a crack width of 0.15 mm can be mostly recovered by 1.0% SAP and AE.  
343 Bond-slip curves of 25S1A mixtures are illustrated in Fig. 17 for pre-cracked and healed  
344 specimens. Crack widths of 0.20, 0.25, and 0.30 mm are generated in the splitting test for this type  
345 of mixture. Splitting failure modes are observed for these crack widths. Sudden drops in the bond-  
346 slip curves are obtained for cracked specimens (Fig. 17(a)). Scattering results are obtained for this  
347 type of mixture with a low dosage of 0.25% SAP. Results clearly show that the 14-day healing  
348 period is not enough to recover bond properties. As shown in Fig. 17(b), higher bond strength is  
349 obtained for the healed specimens with crack widths of 0.30 mm after 28-day healing periods.  
350 Healed specimens have higher initial stiffness of bond-slip curves, as compared with cracked  
351 specimens (Fig. 17(c)). However, there are no promising results for residual bond stress of  
352 mixtures containing 0.25% SAP with AE (Fig. 17(d)), which is different from 1.0%SAP mixtures  
353 (Fig. 17(d)). Absorbed energy (dissipated) by the bond mechanism in 25S1A mixture is  
354 significantly affected b 28-day healing periods so that even higher area is observed as compared  
355 with uncracked specimens (Fig. 17(e)). However, splitting failure modes are observed for all  
356 healed specimens. Overall, results indicate that healing specimens cannot change the failure mode.  
357 Bond-slip curves of 25S2A mixtures are illustrated in Fig. 18 for pre-cracked and healed  
358 specimens. Crack widths of 0.20-0.40 mm are generated in the splitting test for this type of mixture.  
359 Splitting failure modes are observed for these crack widths. Sudden drops in the bond-slip curves

360 are observed for cracked specimens (Fig. 18(a)). For crack width of 0.30 mm, results for 28-day  
361 healing periods show higher bond strength as compared to the cracked specimens (Fig. 18(b)).  
362 Also, two cracked specimens with  $w = 0.40$  mm are considered for 28-day healing periods.  
363 General results of the initial stiffness (slop) of bond-slip curve show that healed specimens have  
364 slightly higher slop as compared to the cracked specimens, while the trend is weaker for 0.25%  
365 SAP (Fig. 18(c)) than 1.0% SAP (Fig. 16(c)). This may be attributed to the small crack width  
366 generated (by splitting test) for 1.0% SAP. Similar to 25SAP1A mixture, there is no clear trend  
367 for residual bond stress in 25SAP2A mixture. Despite the previous mixture containing SAP and  
368 AE, 25SAP2A mixture could not drastically improve the absorbed energy, especially for crack  
369 width of 0.25 mm (Fig. 18(e)).

370 Close photos of the healed specimens are shown in Figs. 19 and 20 (white crystals). Scanning  
371 electron microscopy/energy dispersive X-ray spectrometry (SEM/EDS) microanalysis method was  
372 conducted to identify and quantify all elements of healed products. A considerable amount of  
373 calcium deposits are mostly abundant close and at crack lips, which may be an illustration of  
374 calcium carbonate precipitation for healing cracks (Figs. 19 and 20). SEM/EDS results of one  
375 sample are illustrated in Fig. 21. To compare the results of SEM/EDS analysis between healing  
376 products obtained from the internal and external surfaces of cracks, results of some samples are  
377 shown in Fig. 22. Results indicate that healing products at the external surfaces of cracks have a  
378 considerably lower content of calcium (Ca), as compared to the internal ones. However, higher  
379 content of oxygen (O), carbon (C), and especially magnesium (Mg) are observed for external  
380 healing products, as compared to the internal ones. Snoeck et al. (2014) [46] reported that the  
381 external healing products consist of  $\text{CaCO}_3$  and washed out hydration products. However, there is

382 no accurate description of the differences between elements of the internal and the external  
383 products.

### 384 **3 Statistical analysis of healing improvement factor**

385 After presenting the results for non-AE and AE concrete, this section intends to perform a  
386 comprehensive statistical analysis to find out (1) the most important parameter affecting the self-  
387 healing results; (2) interaction plots of improvement factors with respect to different key variables.  
388 To follow this statistical approach, two statistical software of “Minitab” [60] and “STATISTICA”  
389 [61] are used. Crack width ( $w$ ), healing period ( $H$ ), SAP percentage, SAP type, and AE percentage  
390 are the main variables considered for the input of the analysis. Improvement factors of maximum  
391 ( $IF_u$ ), average ( $IF_m$ ), and residual ( $IF_r$ ) bond strength are the output results. Additionally, the  
392 average values of these three improvement factors ( $IF_{ave}$ ) is also considered in the analysis.  
393 Analysis of variance (ANOVA) is conducted to explain the interaction between variables and also  
394 output. The main effects of variables obtained by ANOVA are illustrated in Fig. 23 for the average  
395 bond stress, the bond strength, and the residual bond stress improvement factor. Moreover, the  
396 average values of these improvement factors are measured and compared. From the ANOVA  
397 analysis on the average improvement factors ( $IF_{ave}$ ), P-values of 0.015, 0.06, 0.001, 0.91, and 0.12  
398 were obtained for input parameters of crack width ( $w$ ), healing period ( $H$ ), SAP percentage  
399 ( $SAP\%$ ), SAP type (or size), and AE percentage, respectively. Results indicate that the  $SAP\%$   
400 factor is the most influencing factor on the self-healing method, as compared to other parameters,  
401 while no clear trend was observed for the SAP type (or size) factor so that high P-value was obtained  
402 for this parameter. Results indicate that crack width smaller than 0.20 mm is fully recovered by  
403 wet-dry healing cycles (higher than 50%) (Fig. 23(a)). A similar range of around 0.14 mm is

404 reported by Snoeck et al. (2014) [46] to completely seal cracks by SAP. However, Fig. 23(a) shows  
405 that bond strength recovery (crack-healing) is difficult for large crack widths so that IF is around  
406 20% to 25% for  $w > 0.20$  mm. Similarly, in this context, Kua et al. (2019) [58] reported that the  
407 performance of crack-sealing by the combination of SAP and fiber is low for large crack widths  
408 ( $w > 0.5$  mm). It shows that more confinement methods are necessary to limit the initial crack  
409 width for improving the self-healing method at the rebar-concrete interface and/or the matrix.  
410 Regarding healing periods, ANOVA results show that an average value of 20% is obtained for 14-  
411 day wet-dry cycles, while the average value of 35% is obtained for 28-day wet-dry cycles (Fig.  
412 23(b)). As the healing period increases, enough time is available to provide more  $\text{CaCO}_3$   
413 participation at crack surfaces, which is similarly reported by Snoeck et al. (2018, 2019) [62, 63].  
414 The effect of SAP size (and type) on healing improvement factors is shown in Fig. 23(c). The  
415 analysis shows that SAP with larger size (0.50 mm, SAP-1) has considerably higher improvement  
416 factor as compared to the smaller SAP (0.15 mm, SAP-2). As comprehensively discussed by  
417 Mousavi et al. (2020) [47], concrete containing SAP-1 generates larger macro voids as compared  
418 to SAP-2, which may provide more possibility to pass the crack line. However, there is no fact  
419 regarding this difference in the literature. Different chemistry types of SAP used may affect the  
420 obtained results. The effect of AE admixture on the self-healing capacity of concrete is illustrated  
421 in Fig. 23(d). Results show that AE admixture has considerable influences on self-healing capacity  
422 so that improvement factor higher than 60% is obtained for the maximum improvement factor of  
423 AE mixtures. Fig. 23(e) shows that SAP percentage has considerable influence on improvement  
424 factors. Although NC without SAP obtained less than 10% IF, SAP concrete mixtures have a range  
425 of  $20\% \leq IF < 150\%$  for 1.0% SAP. Average improvement factor ( $IF_{ave}$ ) has a range 60%-90%  
426 for 1.0% SAP percentage. Regarding NC without SAP,  $IF_u$  has the lowest value among the

427 improvement factors, while this parameter is increased for 0.25% and 0.50% SAP (Fig. 23(e)).  
428 However, in the case of 1.0% SAP which small crack widths are tested, still lower healing capacity  
429 is observed as compared to other improvement factors. Moreover, results show that 28-day healing  
430 period is enough for regaining residual bond stress, as compared to the bond strength. It seems that  
431 more healing periods are necessary to regain bond strength after the pre-cracking phenomenon.  
432 Fig. 24 clearly confirms the results of the previous subsection regarding SAP percentage. Results  
433 indicate that a higher dosage of SAP has a significant impact on self-healing capacity, especially  
434 after 28-day healing periods and in concrete mixtures containing AE admixture. Based on  
435 statistical results obtained in the previous subsections, this section intends to propose a statistical  
436 equation to predict average improvement factor ( $IF_{ave}$ ). A multilinear regression model by  
437 STATISTICA software [61] shows that crack width plays a critical role in the self-healing method  
438 which has severally confirmed by Snoeck et al. (2014, 2019) [46, 62]. Moreover, SAP% and the  
439 healing period have considerable effects on the average improvement factor. However, SAP size  
440 has the lowest impact on  $IF_{ave}$ , as compared to other variables. Hence, the proposed model ignore  
441 this parameter. Finally, the statistical equation of Eq. (7) is obtained to predict average  
442 improvement factor ( $IF_{ave}$ ), as follows:

$$IF_{ave} = -0.30 + 0.18H + 0.46SAP\% + 0.17AE \quad (7)$$

443 where  $H$  is the healing period,  $SAP\%$  is polymer percentage replacement by cement weight, and  
444  $AE$  is air-entraining admixture percentage replacement by cement weight. Performance of Eq. (7)  
445 is shown in Fig. 25. It is worth mentioning that as Eq. (7) was obtained based on the experimental  
446 results of the present study, there are always some limitations. For instance, only one healing  
447 regime (wet-dry cycle) with limited healing periods (14 and 28 days) was considered. Additionally,

448 one dosage and type of AE was used in the experimental program. Moreover, as emphasized  
449 throughout the present study, different SAP types with different chemistries can be used in this  
450 context. For aiming that, more experimental studies are necessary for future works to determine  
451 the efficiency of the proposed equation.

#### 452 **4 Discussion of the results**

453 As mentioned in the previous sections, SAP percentage, AE, and healing periods have considerable  
454 impacts on the crack-healing at the rebar-concrete interface, which is summarized in Eq. (7). This  
455 section intends to explain the main reasons for these findings by using the “Buffon needle  
456 problem”, probability of crack-hitting by SAP particles (Fig. 26). Buffon’s problem considers a  
457 grid of parallel lines with spacing  $B$  and a needle length of  $D$ . When the needle is dropped at  
458 random, its position and orientation are random [64], the needle intersects at least one line of the  
459 grid by the probability of  $P_T$  [65]. Regarding SAP-modified concrete, we assume that SAP  
460 particles are randomly dispersed in the concrete mixture. As shown in Fig. 26(a), crack pattern is  
461 constant in the case of the pre-cracking phenomenon. The process of tossing SAP onto the crack  
462 network generates two scenarios including: (1) SAP particles intersecting the cracks; (2) SAP are  
463 far from the crack edges. Hence, these scenarios reminds the “Buffon needle problem”. For SAP  
464 particles, if there are  $N$  SAP particles and the crack-hitting probabilities by the SAP ( $P$ ) are  
465 considered the same, the random variable  $X$  meaning the total number of intersection in the area,  
466 and the mean of  $X$ , denoted as  $E(X)$ , can be given by Lin et al. (2018) [65]:

$$E(X) = N \times P_T \quad (8)$$

467 If each SAP has the ability to repair cracks of length equal to the threshold  $L_{heal}$ , the expected  
468 length of repairing the crack by  $N$  number of SAP can be written by  $L_{heal} \times E(X)$ . The total length  
469 of cracks in the material is  $L_T$ . If those cracks can be completely healed, the following formulation  
470 should be fulfilled:

$$L_{heal} \times E(X) \geq L_T \quad (9)$$

471 Hence, using Eq. (8) into Eq. (9), healing capacity of SAP intersected the crack lines ( $L_H$ ) can be  
472 given by Lin et al. (2018) [65]:

$$L_H = L_{heal} \times N_A \times A_T \times P_T \quad (10)$$

473 where  $N_A$  is the ratio of  $N/A_T$ . Regarding  $P_T$  of buffon needle, several studies reported Eq. (11)  
474 [64, 66]:

$$P_T = \frac{2l}{\pi B} \quad (11)$$

475 where  $B$  is the distance between cracks and  $l$  is the maximum dimension of SAP particles around  
476 the rebar. As reported by Mousavi et al. (2020) [47], this length is between 1.88 mm to 2.78 mm  
477 for 0.25% and 1.0% SAP respectively. Higher values for higher SAP% can be attributed to the  
478 accumulation of SAP which is similar to higher dosages of nanoparticles. Finally, results of the  
479 present study can be justified by Eq. (10), as follows:

480 a. Higher SAP percentage causes a considerable impact on the healing improvement factor. This  
481 can be related to the parameter of  $N \times P_T$ . By increasing the SAP percentage, the Intersection

482 probability of crack-hitting will be increased so that it causes higher healing possibilities at the  
483 rebar-concrete interface (Fig. 26(b)).

484 b. Statistical results indicate that 28-day healing periods are more efficient as compared to the  
485 14-day healing periods. This can be attributed to the  $L_{heal}$ . Additionally, as crack width  
486 increases, self-healing capacity decreases which similarly can affect the  $L_{heal}$ . There is no  
487 specific research on studying the expected crack-repairing length by each SAP particle. As  
488 shown in Fig. 26, regarding the pre-cracked concrete surrounding the rebar, there are two main  
489 potential zones including (1) zone I around the rebar with a distance of  $w/2$ ; and (2) zone II  
490 far from the rebar as compared to zone I. Zone I is more dominant for starting the healing  
491 process due to the existence of the calcite layer around the rebar, which is essential for  $\text{CaCO}_3$   
492 precipitation. Many studies reported the enriched quantity of calcium hydroxide at the rebar-  
493 concrete interface, as compared to the bulk cement paste [8, 67, 68], observed by the SEM  
494 images as well as the EDS analysis [69]. To explain this phenomenon, Moreau (1973) [70]  
495 reported that the cement particles inclined to separate from the matrix, generating a slender  
496 zone around the rebar with fewer cement particles and thus more water. This provides a layer  
497 in which  $\text{Ca}^{2+}$  ions can diffuse from outside the interface region, resulting in the formation of  
498 the considerable content of calcium hydroxide [70]. As shown in Fig. 27, the domain of zone  
499 II is determined by  $\alpha d_b$ . This distance is a controlled zone in which concrete cover has a  
500 considerable impact on bond strength and failure modes. For concrete without stirrups, the  
501 limiting value is reached when  $c/d_b \geq 3.0$  [71], while for concrete with a  $0.4f'_c$  lateral  
502 pressure, the normalized ratio  $\tau_{max}/\sqrt{f'_c}$  tends to stop increasing after  $c/d_b \geq 2.0$  [72]. The  
503 present study suggests the simplified following equations for the first potential healing volume



504 around the rebar (Zone I), and the second scenario which is the developed version of the first  
505 scenario (zone I and zone II):

$$(V_{healed})_{zone I} = 3.93wd_b[2d_b + w] \quad (12)$$

$$(V_{healed})_{zone I+zone II} = 5wd_b[5.57d_b - 0.21w] \quad (13)$$

$$(V_{healed})_{zone I+zone II} > (V_{healed})_{zone I} \quad (14)$$

506  $(V_{healed})_{zone I}$  corresponds to the concrete mixtures with medium healing improvement factor,  
507 while  $(V_{healed})_{zone I+zone II}$  corresponds to a high healing improvement factor. For instance,  
508 for the rebar nominal diameter of 10 mm and the crack width of 0.20 mm, values of 158.77  
509  $\text{mm}^3$  and 556.58  $\text{mm}^3$  are obtained for  $(V_{healed})_{zone I}$  and  $(V_{healed})_{zone I+zone II}$ , respectively.  
510 As shown in samples after healing periods in Fig. 28, white powders around the rebar and also  
511 at rebar rib places are clear and the content is higher than the bulk matrix. This can clearly  
512 confirm the hypothesis presented in Fig. 27, where healing probability at Zone I is higher as  
513 compared to Zone II.

514 c. Regarding AE admixture, the statistical results indicated that AE admixture has a positive  
515 impact on the healing improvement factor at the rebar-concrete interface. As shown in Fig.  
516 26(b), AE admixture provides a pore network in the matrix, which makes it easy to transfer  
517 water between SAP particles. This clearly increases the parameter  $L_{heal}$  in the Eq. (10). The  
518 distribution of SAP particles along with AE pores is illustrated in Fig. 29.

519 It is worth mentioning that the present study is only an initial effort to determine the effect of AE  
520 admixture on the self-healing method at the rebar-concrete interface. More research is needed to

521 understand the optimum structure of the bubble network (volume and spacing) for different  
522 dosages of AE admixture and SAP. Moreover, different types of SAP (varied chemical  
523 composition) with different water absorptions are necessary to be tested for obtaining optimum  
524 SAP+AE-contained concrete. Furthermore, as mentioned in Eq. (10), results showed that  $L_{heal}$  of  
525 SAP concrete can be improved by the AE network. However, more studies are needed to quantify  
526 this parameter as a function of SAP percentage and AE dosage. Additionally, future works need  
527 to extend the research on using the “Buffon needle problem” for optimizing the SAP-AE  
528 combination, considering different chemistries.

## 529 **5 Summary and concluding remarks**

530 This study evaluated the effect of air-entraining admixture on interfacial properties between the  
531 steel rebar and un-cracked, pre-cracked, and healed concrete by extensive experimental tests. A  
532 comparison study was conducted between AE and non-AE concrete. Two dosages of 0.25% and  
533 1.0% SAP and one dosage of 0.21% AE were considered for the AE-contained mixtures. Results  
534 were compared with a recently published paper by authors [47] for non-AE concrete. Additionally,  
535 a statistical approach is performed to comprehensively analyse the results. The following critical  
536 concluding remarks are drawn from the experimental and statistical results:

- 537 - The optimum dosage of 0.25% SAP is obtained for both AE and non-AE mixtures.
- 538 - AE admixture is more adaptable with SAP-1 as compared to SAP-2 for uncracked specimens  
539 so that AE concrete mixtures containing both 0.25% and 1.0% SAP-1 have similar normalized  
540 maximum and residual bond stress, and even higher average bond stress, as compared to the  
541 non-AE mixtures.

- 542 - Results of uncracked specimens show that SAP type has a significant impact on porosity  
543 patterns of AE and non-AE mixtures so that there are some conflicting results between  
544 compressive strength results and bond strength results.
- 545 - Overall, the results of the pre-cracked specimens show that the pre-cracking phenomenon has  
546 higher and more impacts on residual bond stress, as compared to the bond strength.
- 547 - AE concrete mixtures are less sensitive to the pre-cracking phenomenon, as compared to the  
548 non-AE mixtures.
- 549 - Results of the healed specimens show that SAP can improve the self-healing capacity of AE  
550 concrete for mitigating damages at the rebar-concrete interface.
- 551 - SEM results show that healing products at the external surface of crack have a considerable  
552 content of calcium (Ca), while the content is lower than the internal surfaces of cracks.
- 553 - It can be deduced from both experimental and statistical results that AE admixture can provide  
554 a stabilized bubble network along with SAP locations for improving the self-healing method.

### 555 **Conflict of interests**

556 The authors declare that there are no competing interests regarding the publication of this paper.

### 557 **Data Availability Statement**

558 All data, models, and code generated or used during the study appear in the published article.

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561

562 **Notation**

AE	air-entraining admixture
ANOVA	analysis of variance
$B$	distance between cracks
$d_b$	rebar diameter
$f'_c$	concrete compressive strength
GU	general use cement
$H$	healing period
$IF$	improvement factor for self-healing method
$IF_{\tau_m}$	healing improvement factor of average bond stress
$IF_{\tau_u}$	healing improvement factor of bond strength
$IF_{\tau_r}$	healing improvement factor of residual bond stress
$IF_{ave}$	average healing improvement factor
$L_{heal}$	threshold length of crack healed by SAP
$L_T$	total length of cracks in the material
$L_H$	healing capacity of SAP intersected the crack lines
$l$	maximum dimension of SAP particles around the rebar
$N$	number of SAP particles passing cracking path
NC	normal concrete
$P_T$	crack-hitting probabilities by SAP
RH	relative humidity
SAP	superabsorbent polymer
SAP%	percentage of SAP used by weight of cement
SEM/EDS	scanning electron microscopy/energy dispersive X-ray spectrometry
$w$	initial crack width
$w/d_b$	initial crack width-to-rebar diameter ratio
$W_T/c$	total water-to-cement ratio
$X$	total number of intersection in the area
$\tau_m$	average bond stress
$\tau_m^*$	normalized average bond stress
$\tau_u$	maximum bond stress (or bond strength)
$\tau_u^*$	Normalized bond strength
$\tau_r$	residual bond stress
$\tau_r^*$	normalized residual bond stress
$(\tau)_c$	bond properties of pre-cracked specimen
$(\tau)_{un}$	bond properties of uncracked specimen
$\tau_{Uncracked}$	bond properties of intact specimens
$\tau_{Precracked}$	bond properties of pre-cracked specimens
$\tau_{Healed}$	bond properties of healed specimens

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## **List of Tables:**

- 564 **Table 1** Concrete composition of AE concrete mixtures
- 565 **Table 2** Configurations of mixtures

566 **Table 1** Concrete composition of AE concrete mixtures

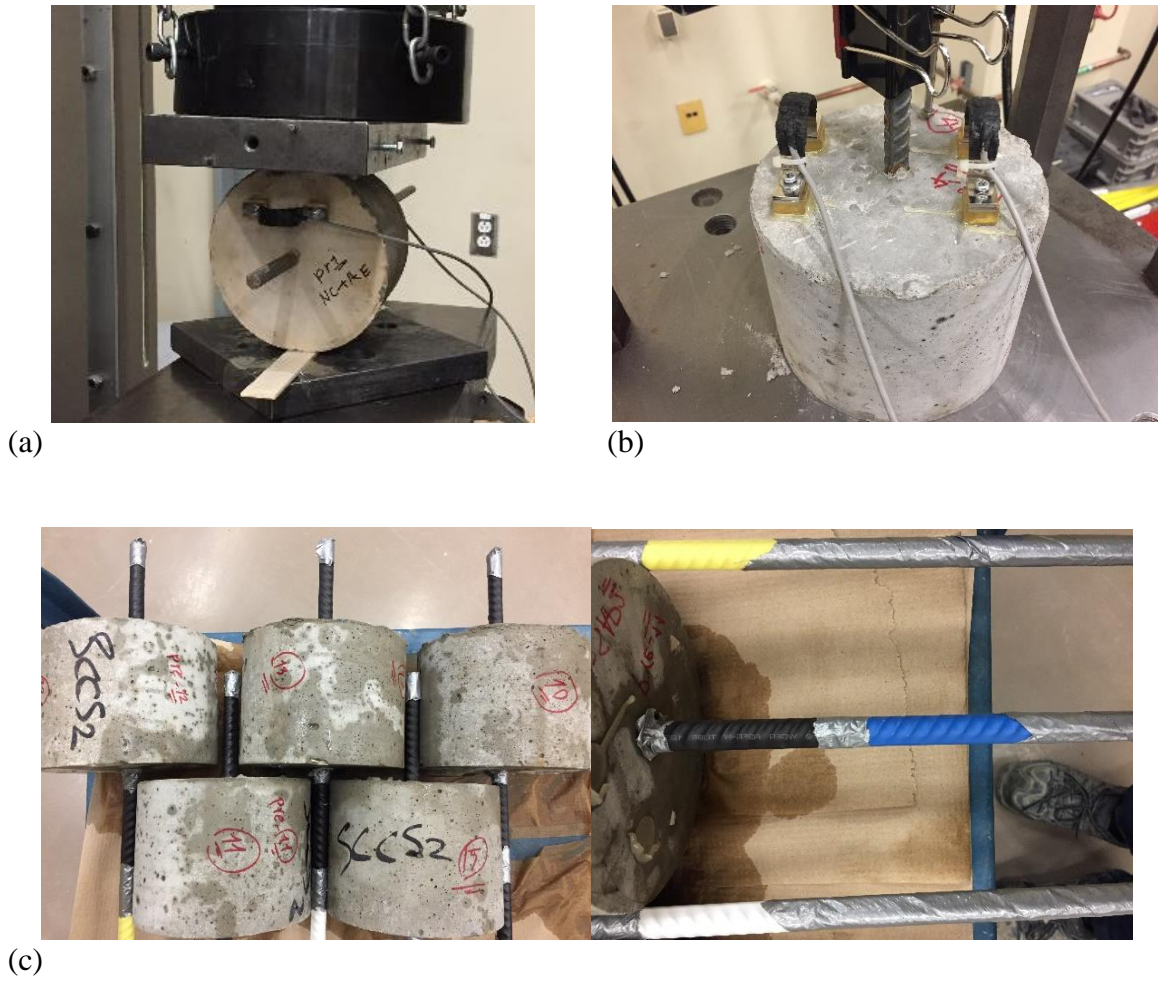
Mix	Cement	Sand	Gravel 5/10	Gravel 10/14	Water	Add. water	SP	AE	SAP
	(kg/m <sup>3</sup> )								%
RA-1	395	788	822	258	165	0	3.98	0.83	0
RA-2	395	788	822	258	165	0	5.23	0.83	0
25S1A	395	788	822	258	165	24.7	3.27	0.83	0.25
25S2A	395	788	822	258	165	24.7	2.23	0.83	0.25
100S1A	395	788	822	258	165	98.8	4.15	0.83	1.0

\* Note: Add=additional water, SP=superplasticizer by MasterGlenium 1466 for all mixture except mixes RA-1 and 100S1A which used EUCON PLASTOL 341, SAP= % wt. of cement, AE=air entraining by Eucon air mac 6 (0.21% wt. of cement).

567 **Table 2** Configurations of mixtures

Mixture	AE		Polymer		SAP percentage (%)				$W_T/c$	Slump (mm)	Density <sup>1</sup> (kg/m <sup>3</sup> )
	With	Without	SAP-1	SAP-2	0	0.25	0.50	1.00			
R		×			×				0.41	97	2453.80
RA-1	×				×				0.41	110	-
RA-2	×				×				0.43	200	2390.08
25S1		×	×			×			0.48	104	2416.79
25S1A	×		×			×			0.48	170	2368.02
25S2		×		×		×			0.48	109	2419.22
25S2A	×			×		×			0.48	191	2283.30
50S1		×	×				×		0.54	95	2335.76
100S1		×	×					×	0.66	91	2256.72
100S1A	×		×					×	0.66	100	2219.85

\* Note:  $W_T/c$ = total water-to-cement ratio.<sup>1</sup> average hardened density of mixtures after 28 days curing.



**Fig. 1** Experimental procedure:  
(a) pre-cracking test; (b) pull-out test; (c) heat-shrinkable tube



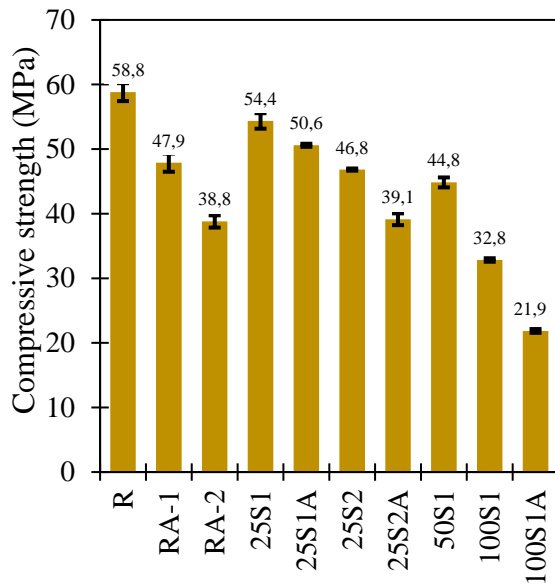


(a)

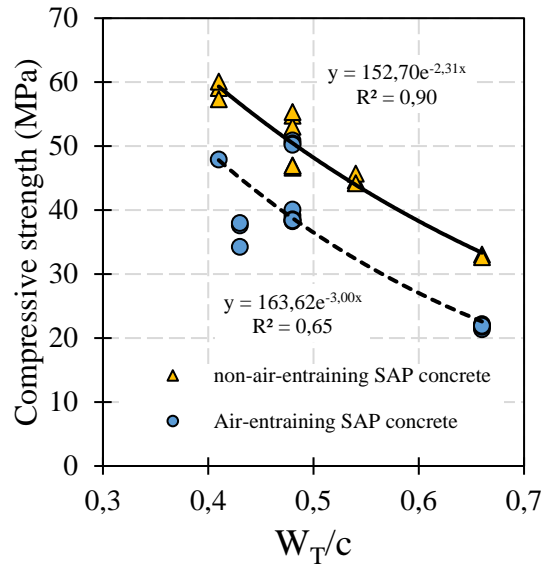


(b)

**Fig. 2** Failure modes for pull-out test specimens: (a) pull-out failure; (b) splitting failure

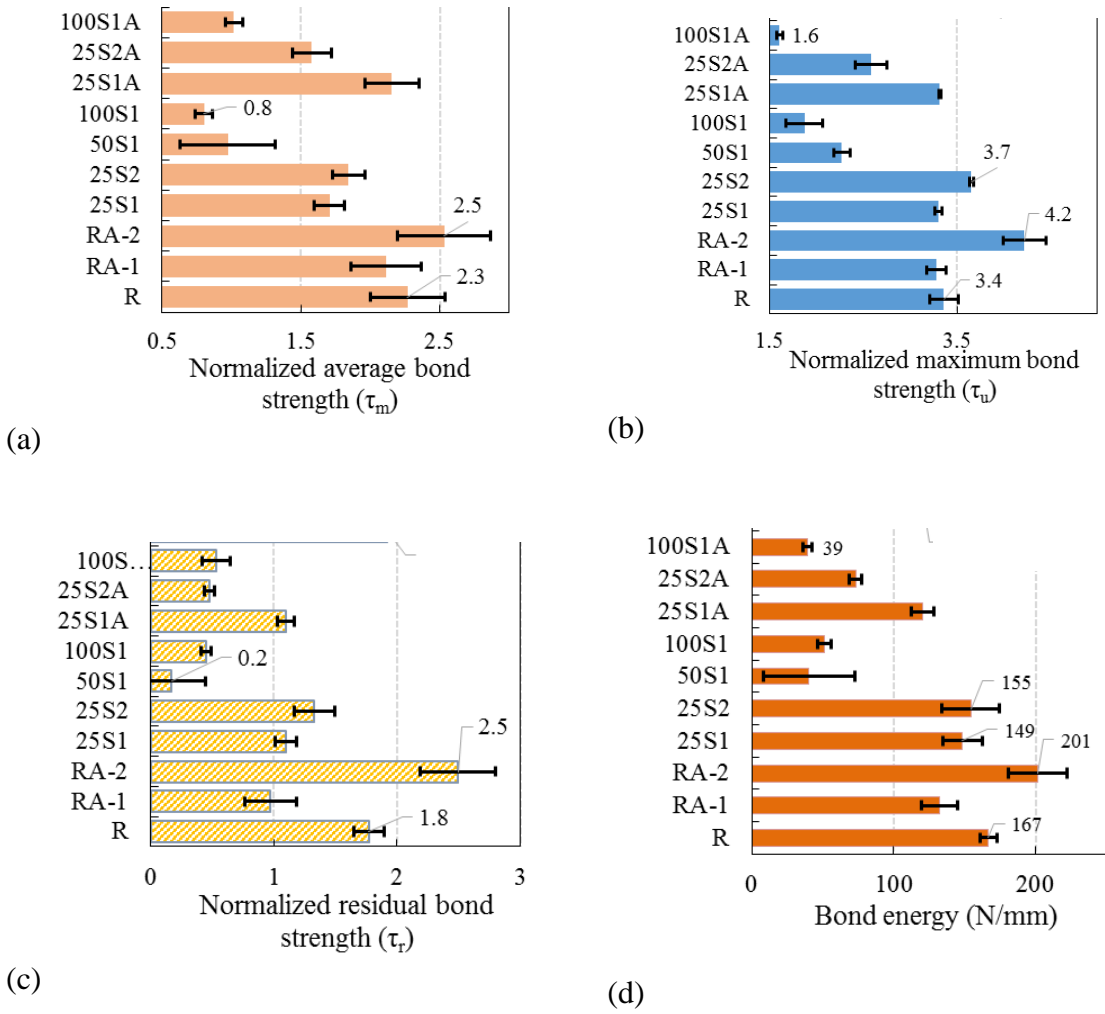


(a)

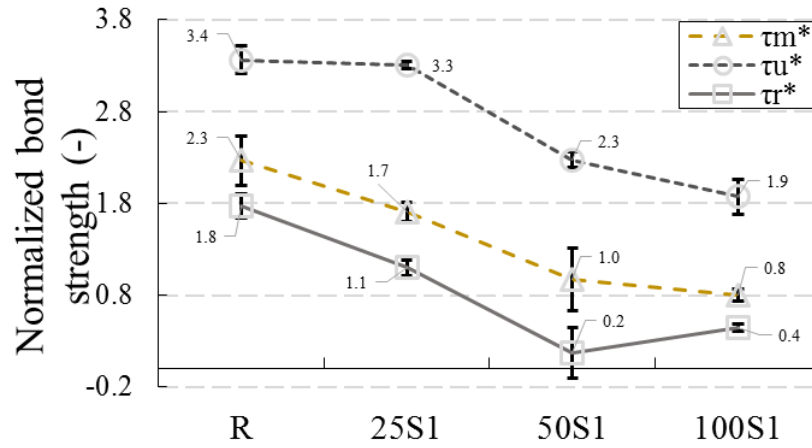


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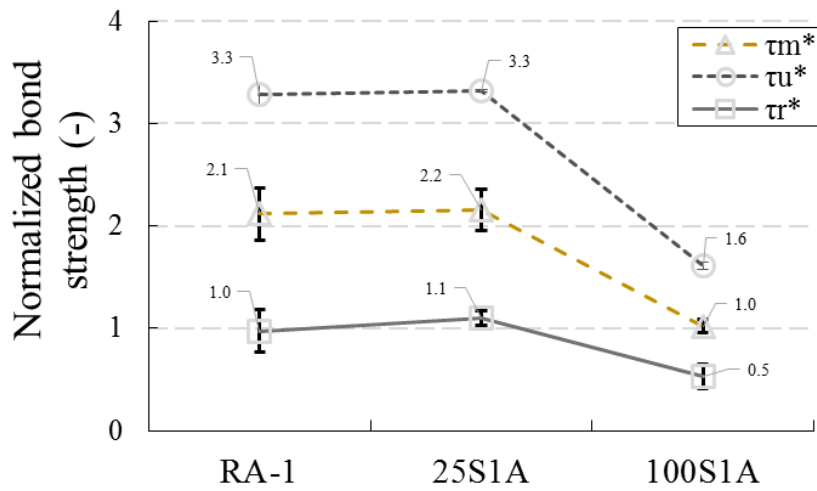
**Fig. 3** Compressive strength of concrete mixtures containing SAP and AE



**Fig. 4** Normalized bond properties of mixtures: (a) average bond stress; (b) bond strength; (c) residual bond stress; (d) bond energy

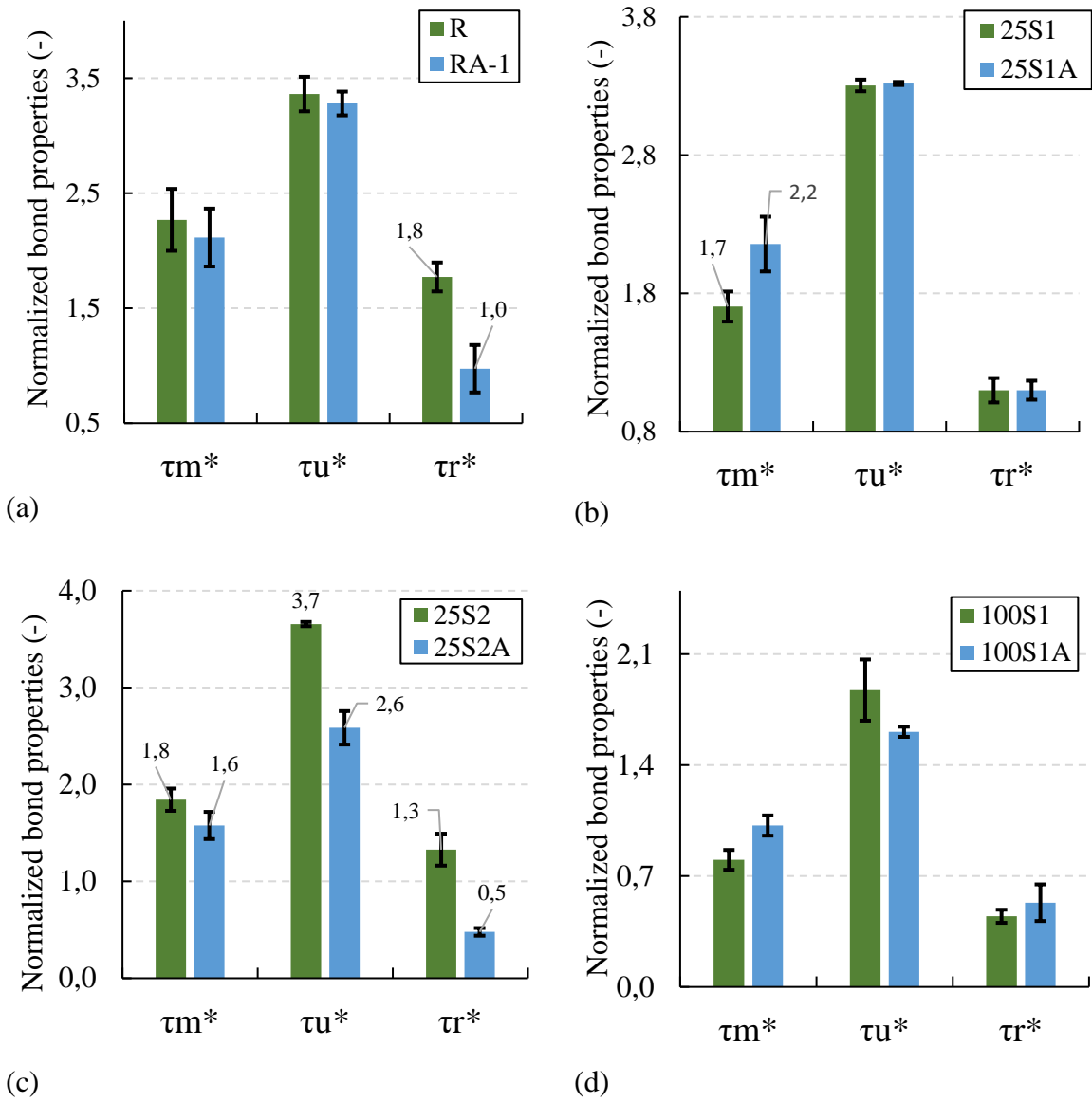


(a)

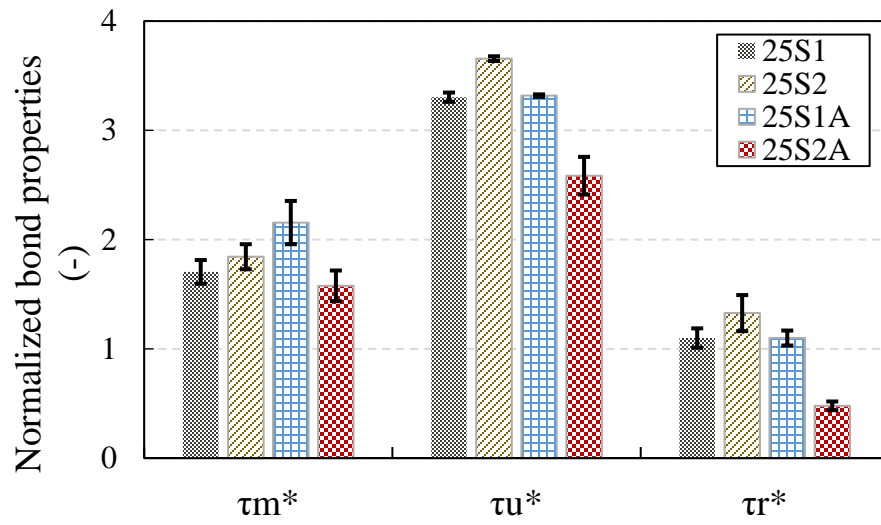


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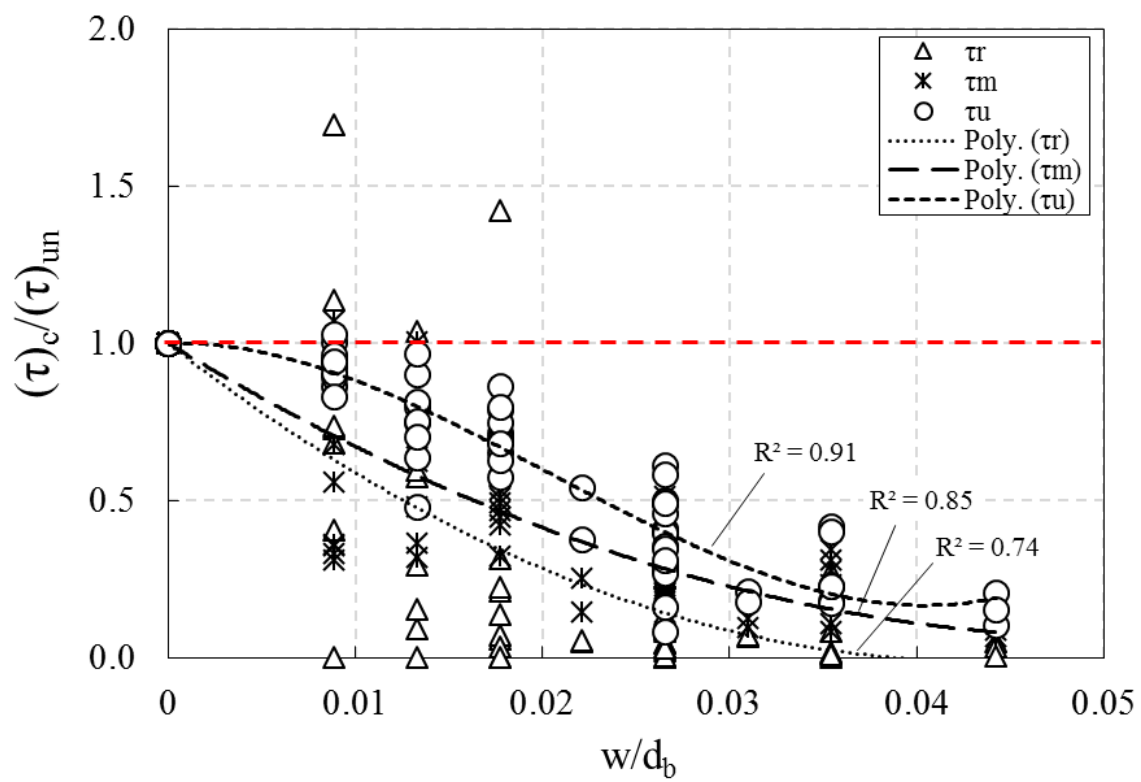
**Fig. 5** Effect of SAP percentage on normalized bond properties of uncracked concrete: (a) non-AE concrete; (b) AE concrete



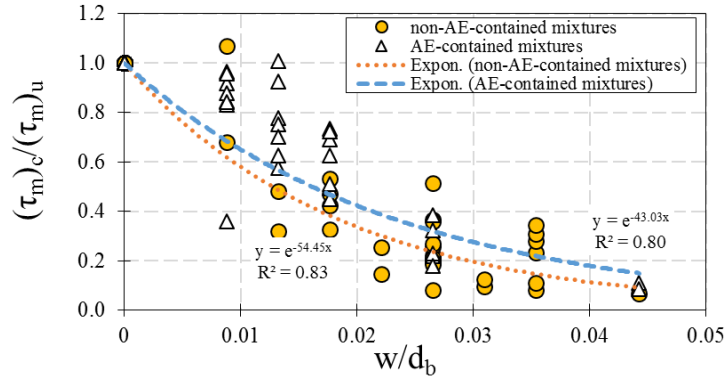
**Fig. 6** Effect of AE admixture on normalized bond properties of uncracked concrete: (a) reference mixtures (0% SAP); (b) 0.25% SAP-1; (c) 0.25% SAP-2; (d) 1.0% SAP-1



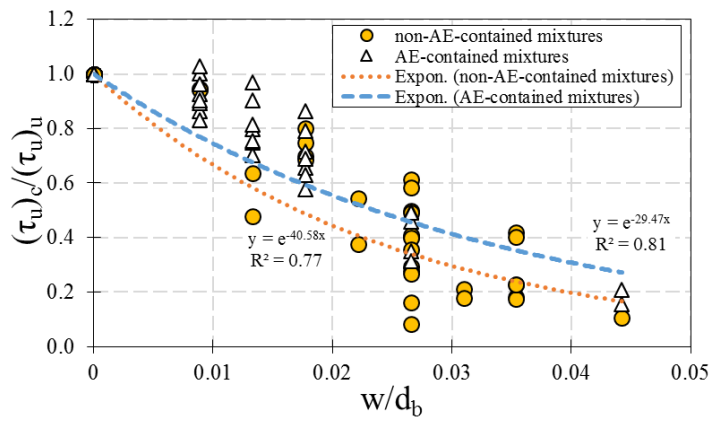
**Fig. 7** Effect of SAP type and particle size on normalized bond properties of AE and non-AE uncracked concrete



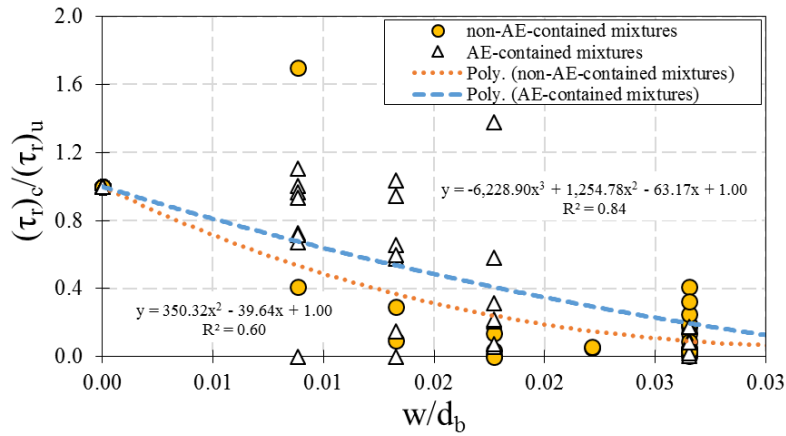
**Fig. 8** Effect of the pre-cracking phenomenon on bond properties for all mixtures



(a)



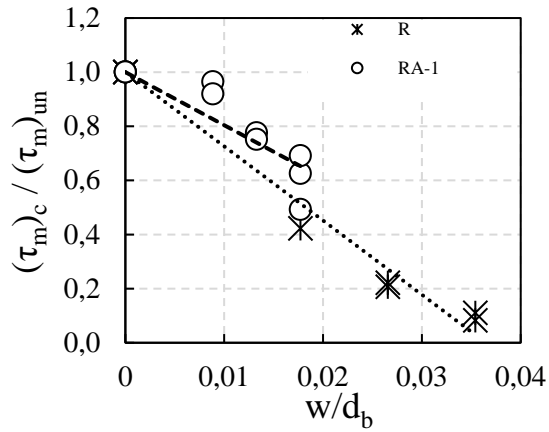
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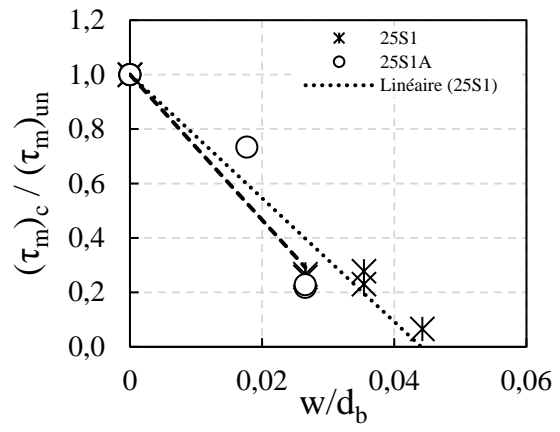
(c)

**Fig. 9** Effect of the pre-cracking phenomenon on bond properties with respect to AE admixture: (a) average bond stress; (b) bond strength; (c) residual bond stress

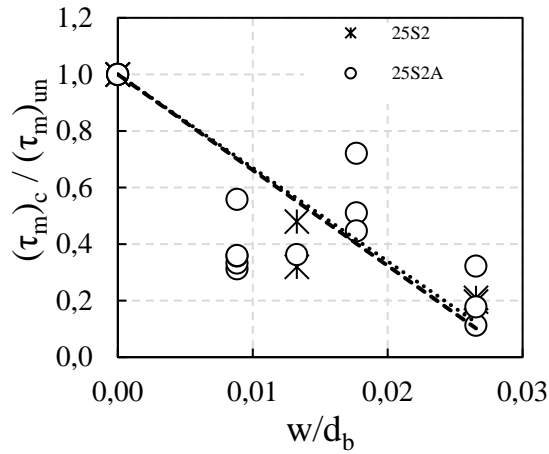




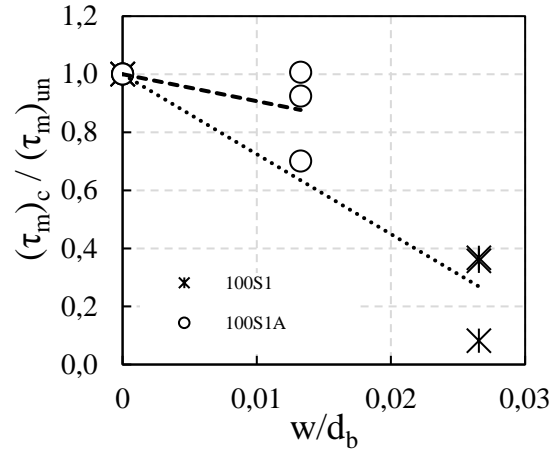
(a)



(b)

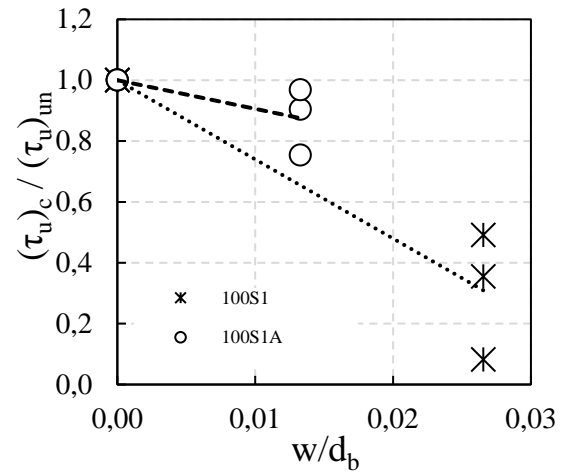
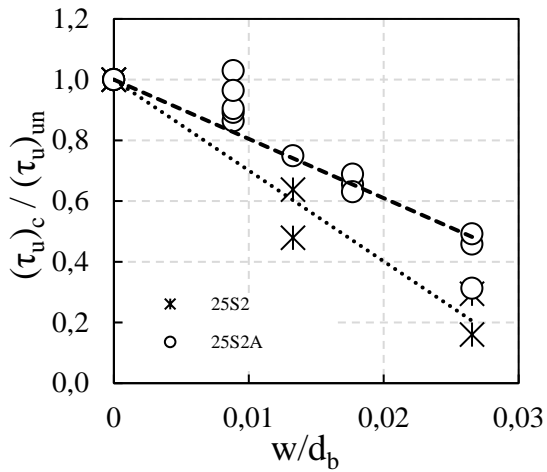
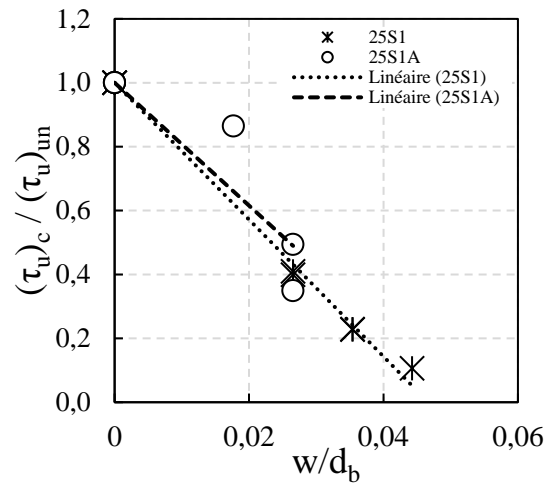
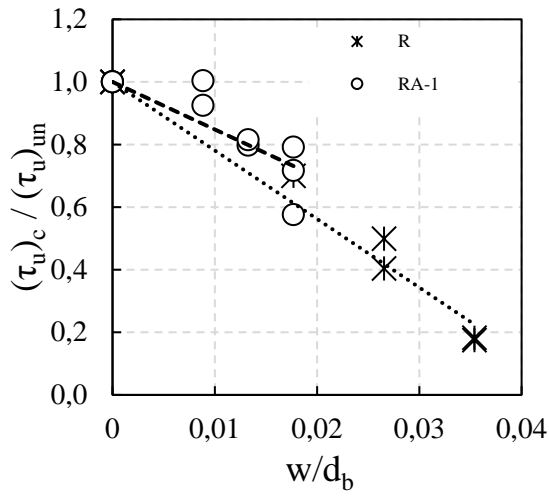


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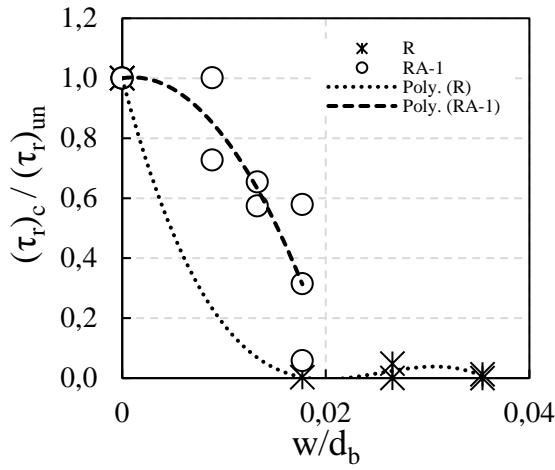


(d)

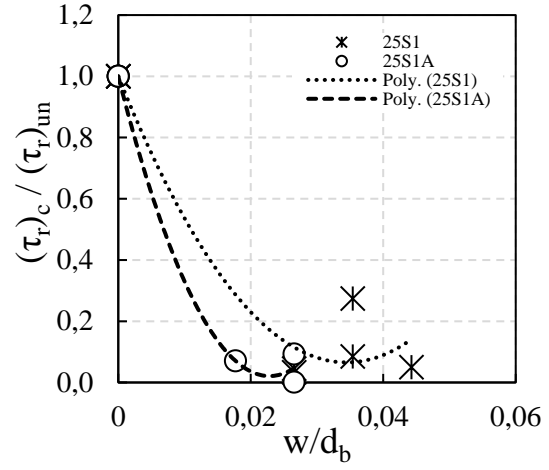
**Fig. 10** Effect of AE admixture on the average bond stress of pre-cracked concrete with respect to different SAP percentages: (a) 0% SAP; (b) 0.25% SAP-1; (c) 0.25% SAP-2; (d) 1.0% SAP-1



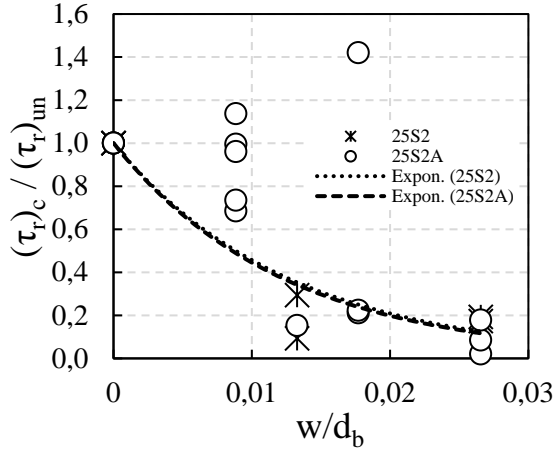
**Fig. 10** Effect of AE admixture on the bond strength of pre-cracked concrete with respect to different SAP percentages: (a) 0% SAP; (b) 0.25% SAP-1; (c) 0.25% SAP-2; (d) 1.0% SAP-1



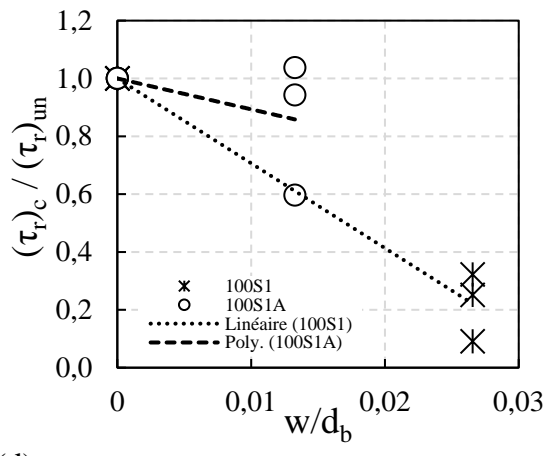
(a)



(b)

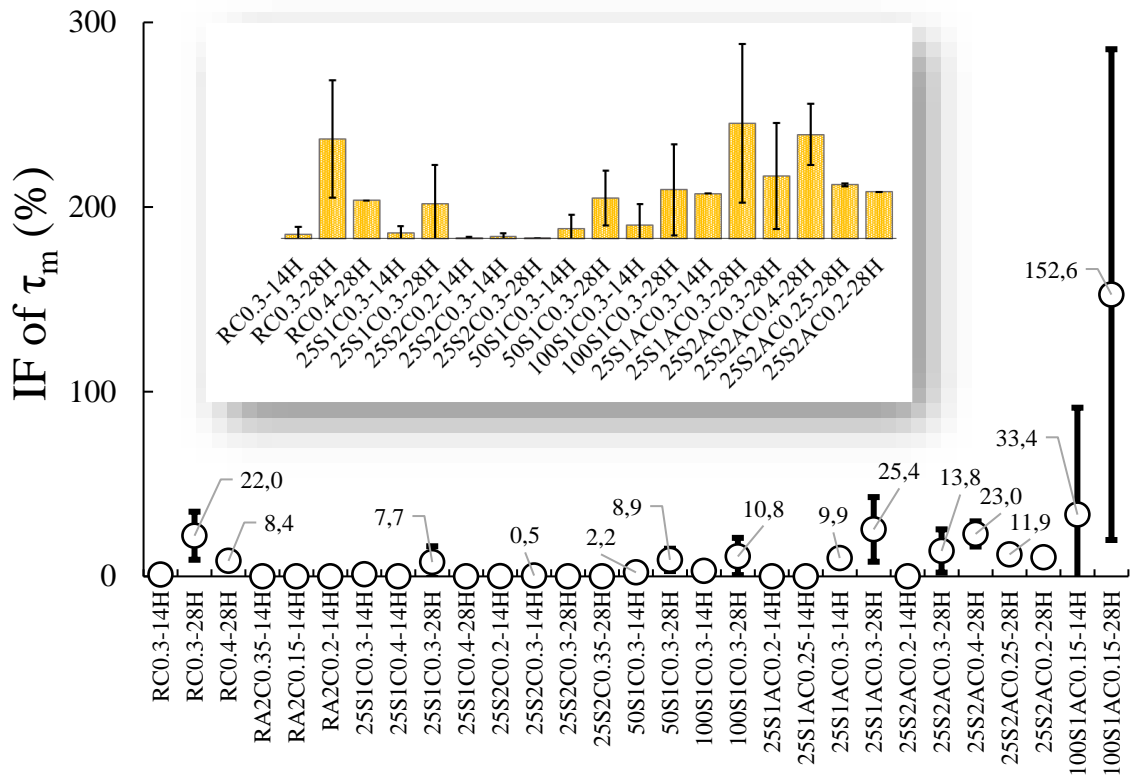


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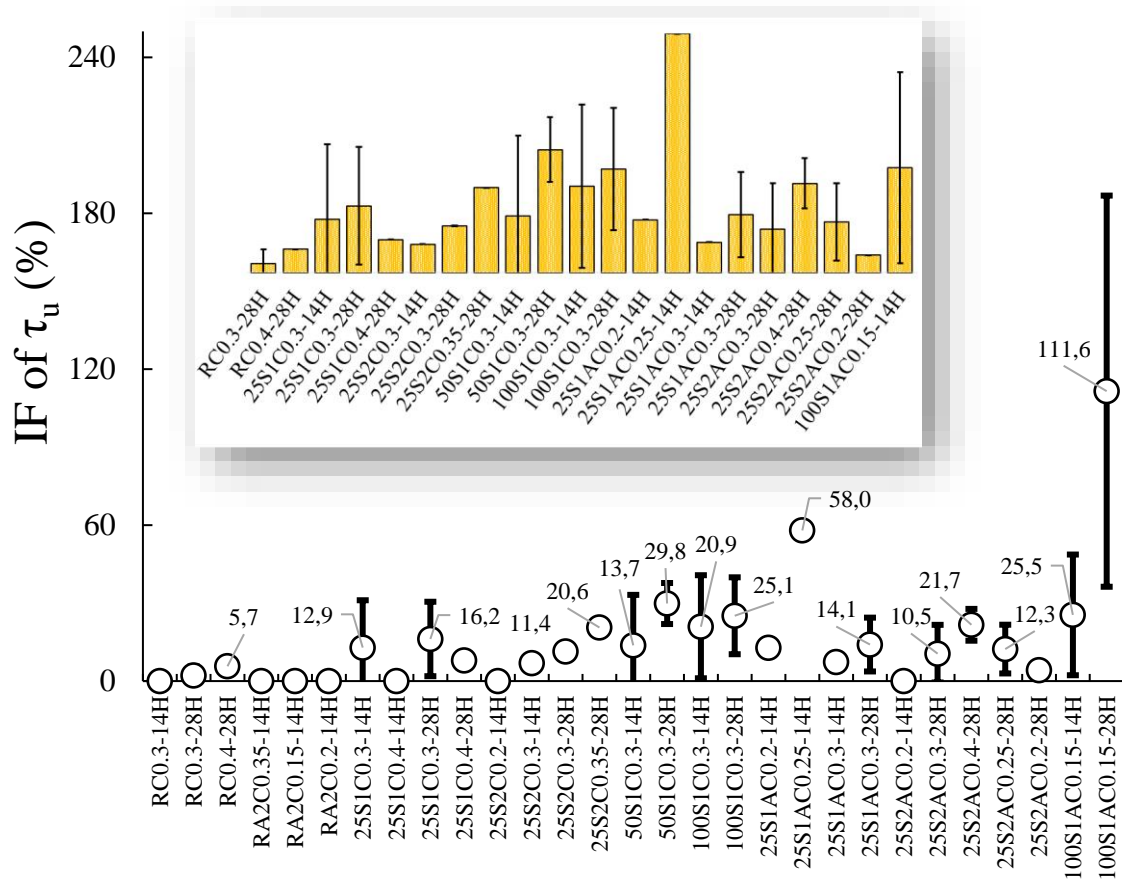


(d)

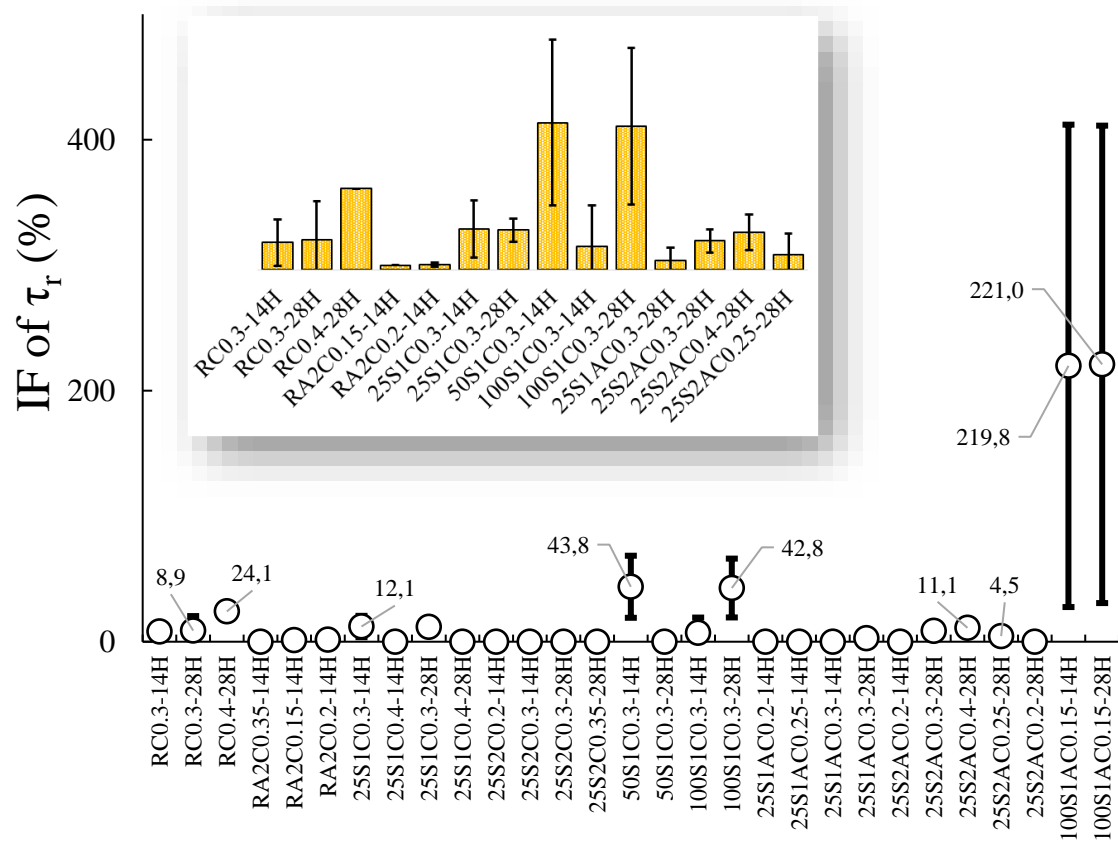
**Fig. 11** Effect of AE admixture on the residual bond stress of pre-cracked concrete with respect to different SAP percentages: (a) 0% SAP; (b) 0.25% SAP-1; (c) 0.25% SAP-2; (d) 1.0% SAP-1



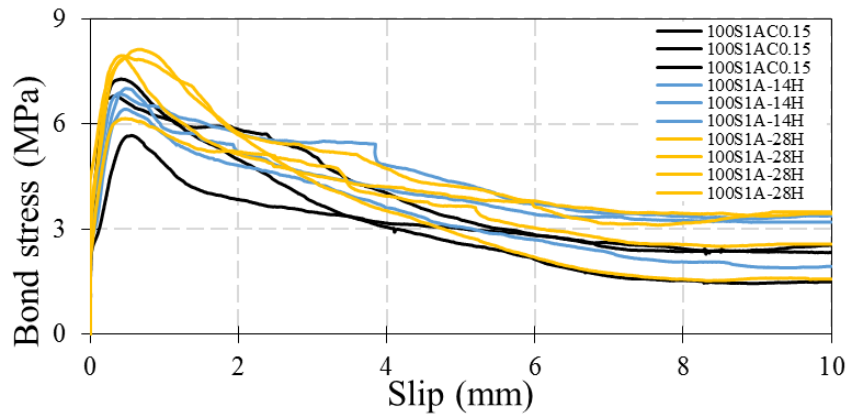
**Fig. 12** Determination of IF for average bond stress



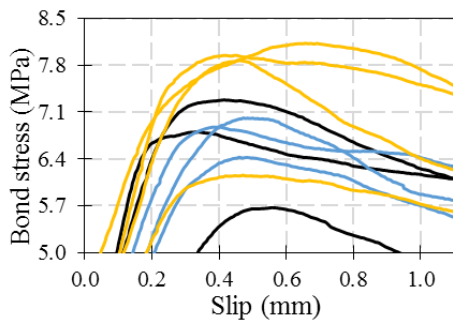
**Fig. 13** Determination of IF for bond strength



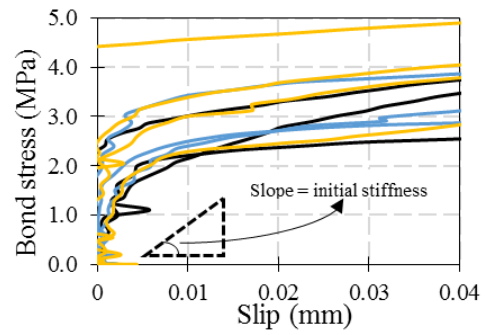
**Fig. 14** Determination of IF for residual bond stress



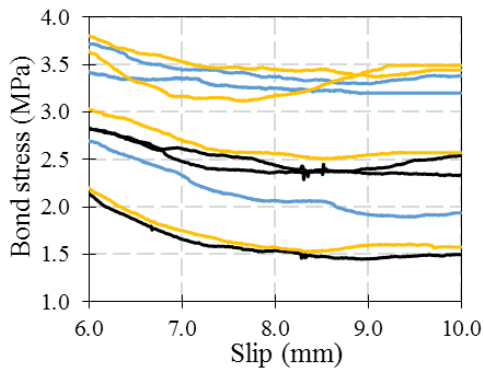
(a)  $w = 0.15 \text{ mm}$



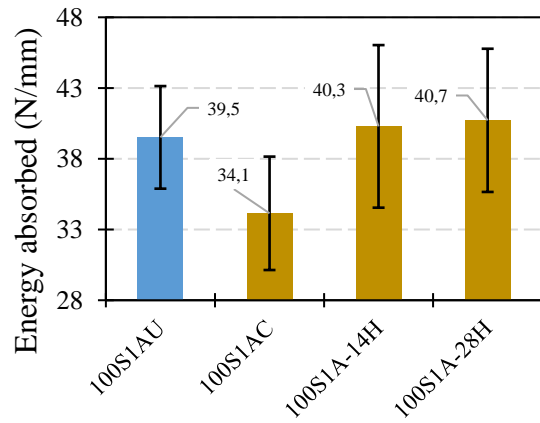
(b)



(c)

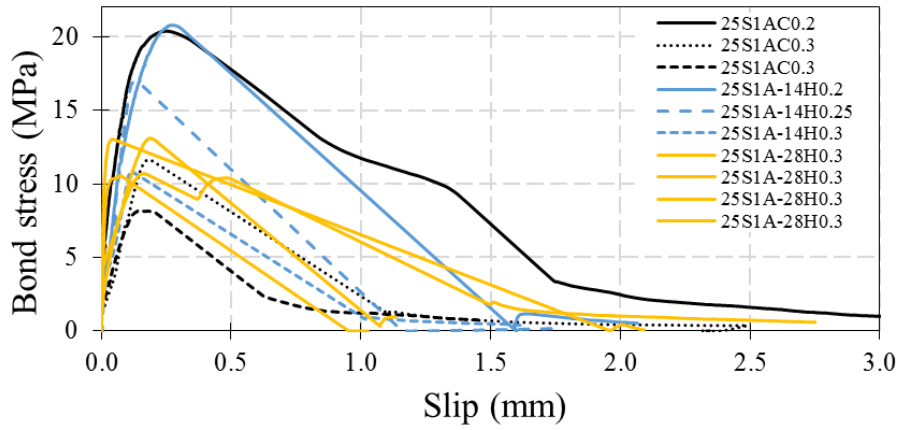


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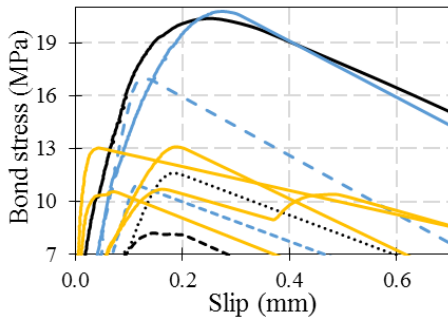


(e)

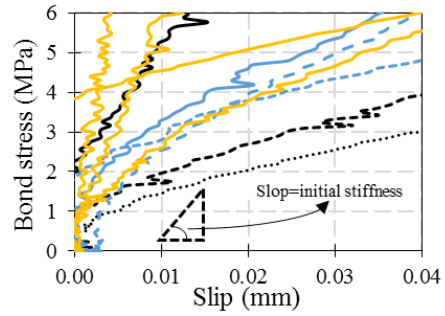
**Fig. 15** Results of 100S1A mixtures: (a) bond-slip curves; (b) bond strength; (c) initial bond stiffness; (d) residual bond stress; (e) energy absorbed



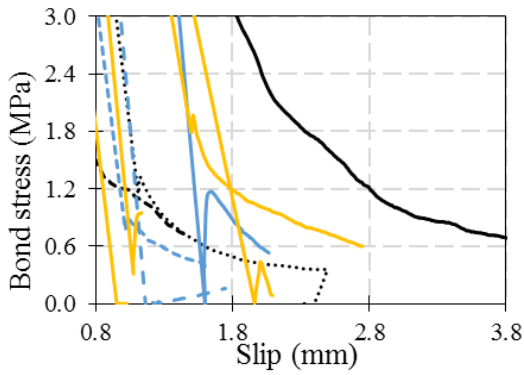
(a)  $w = 0.20 \text{ mm}, 0.25 \text{ mm}, 0.30 \text{ mm}$



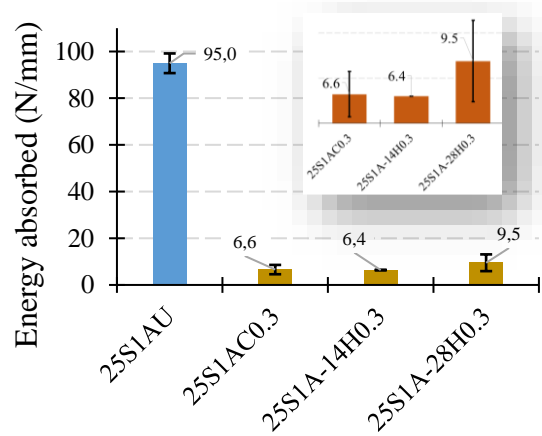
(b)



(c)



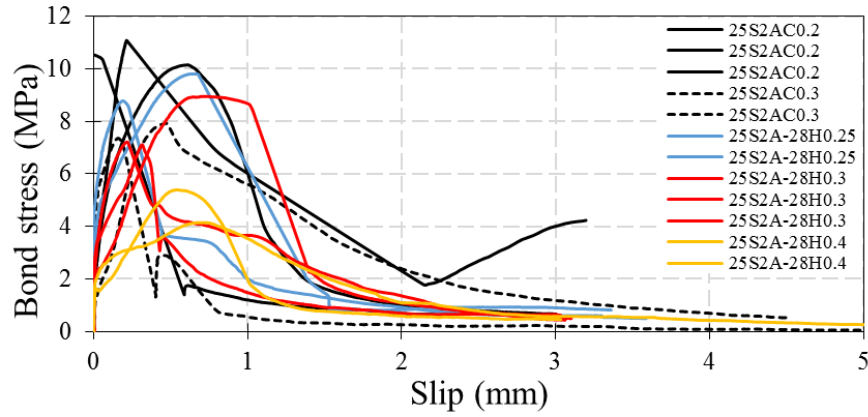
(d)



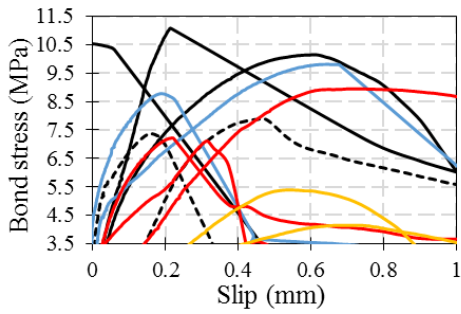
(e)

**Fig. 16** Results of 25S1A mixtures: (a) bond-slip curves; (b) bond strength; (c) initial bond stiffness; (d) residual bond stress; (e) energy absorbed

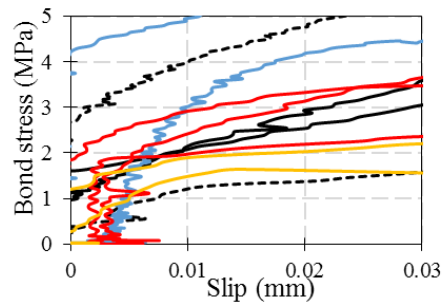




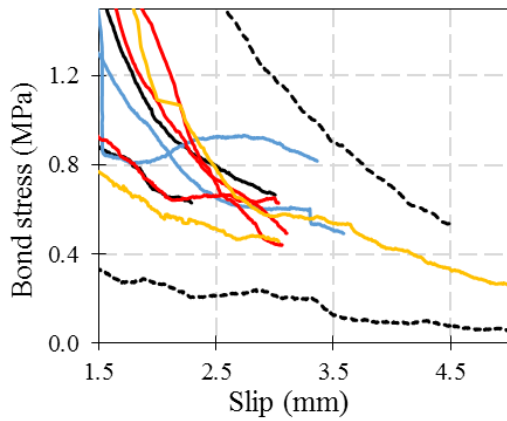
(a)



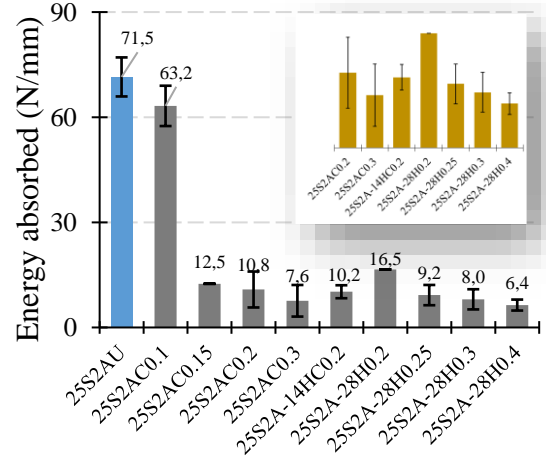
(b)



(c)

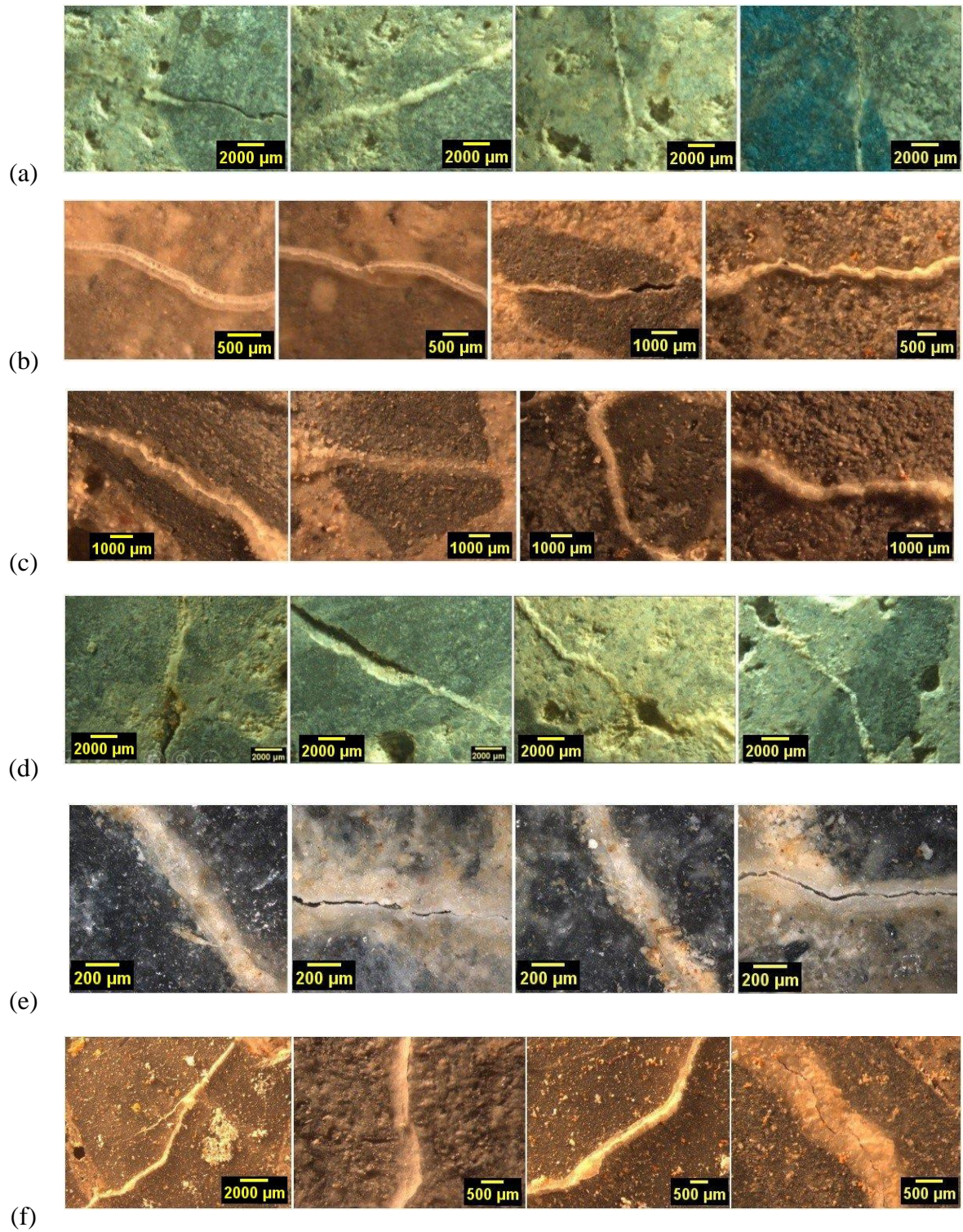


(d)



(e)

**Fig. 17** Results of 25S2A mixtures: (a) bond-slip curves; (b) bond strength; (c) initial bond stiffness; (d) residual bond stress; (e) energy absorbed

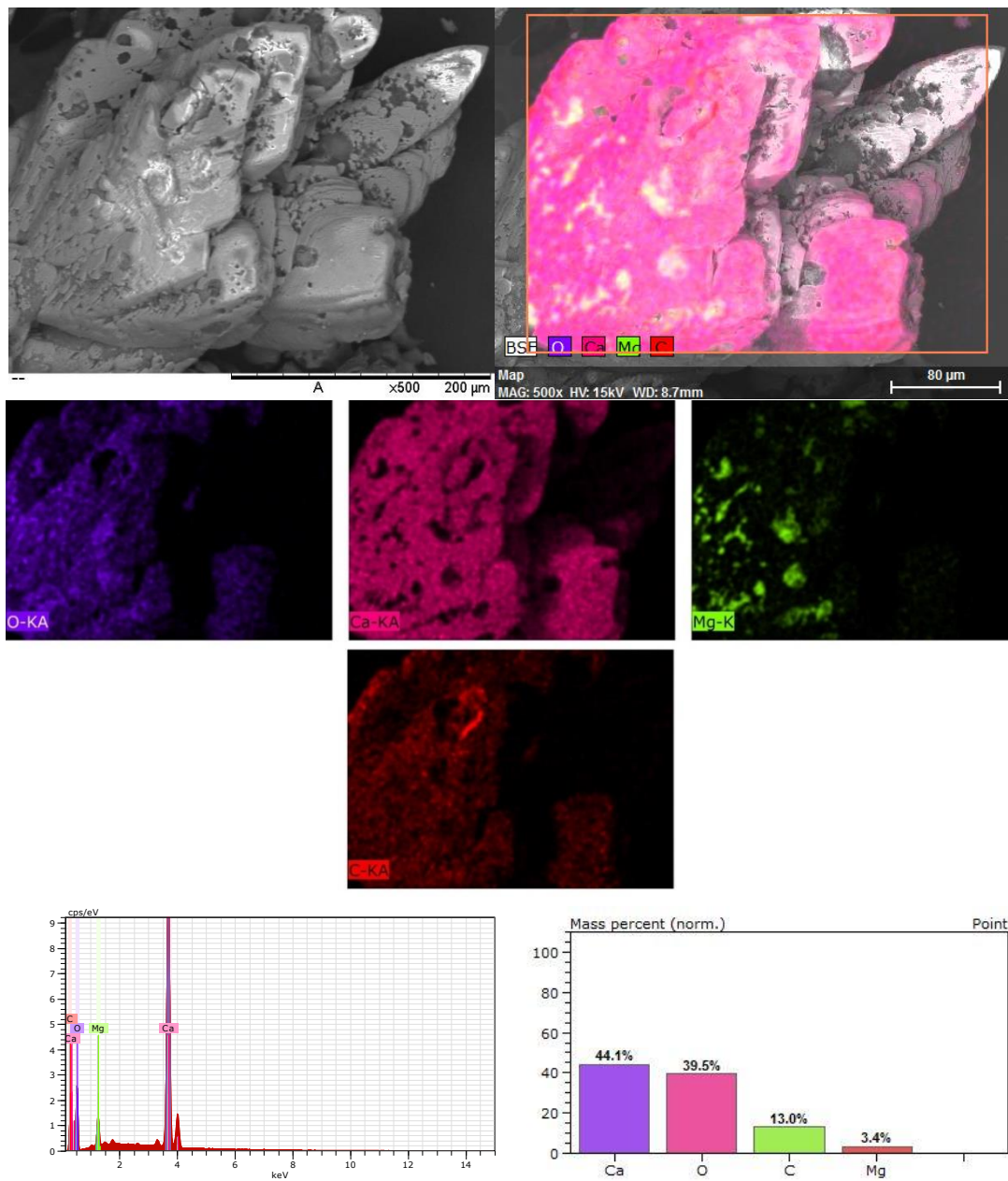


**Fig. 18** Self-healing (and/or sealing) products on crack surface after wet-dry cycles:  
 (a) 25S1; (b) 25S2; (c) 25S2A; (d) 50S1; (e) 100S1; (f) 100S1A

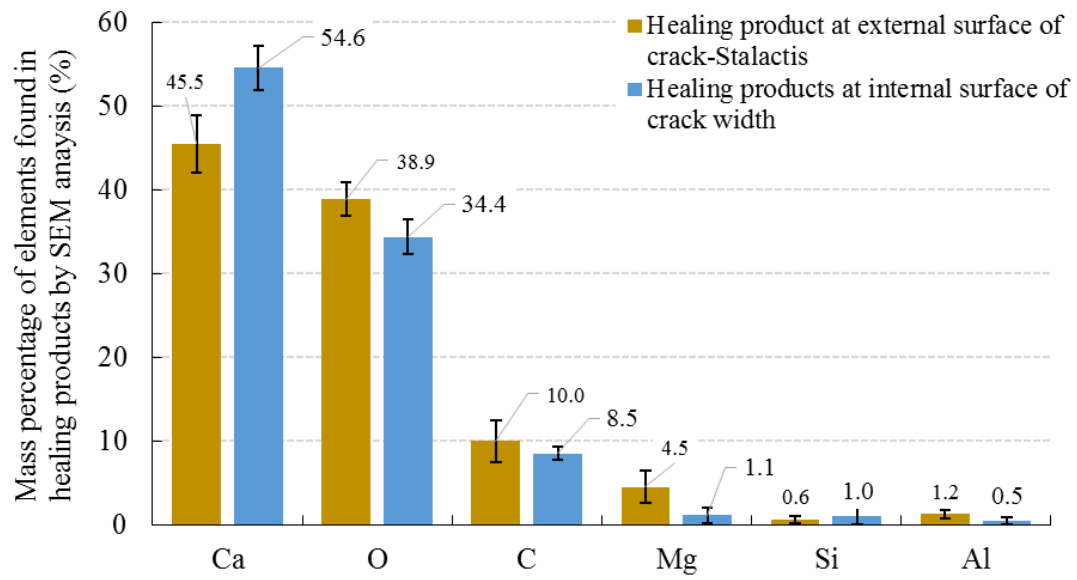




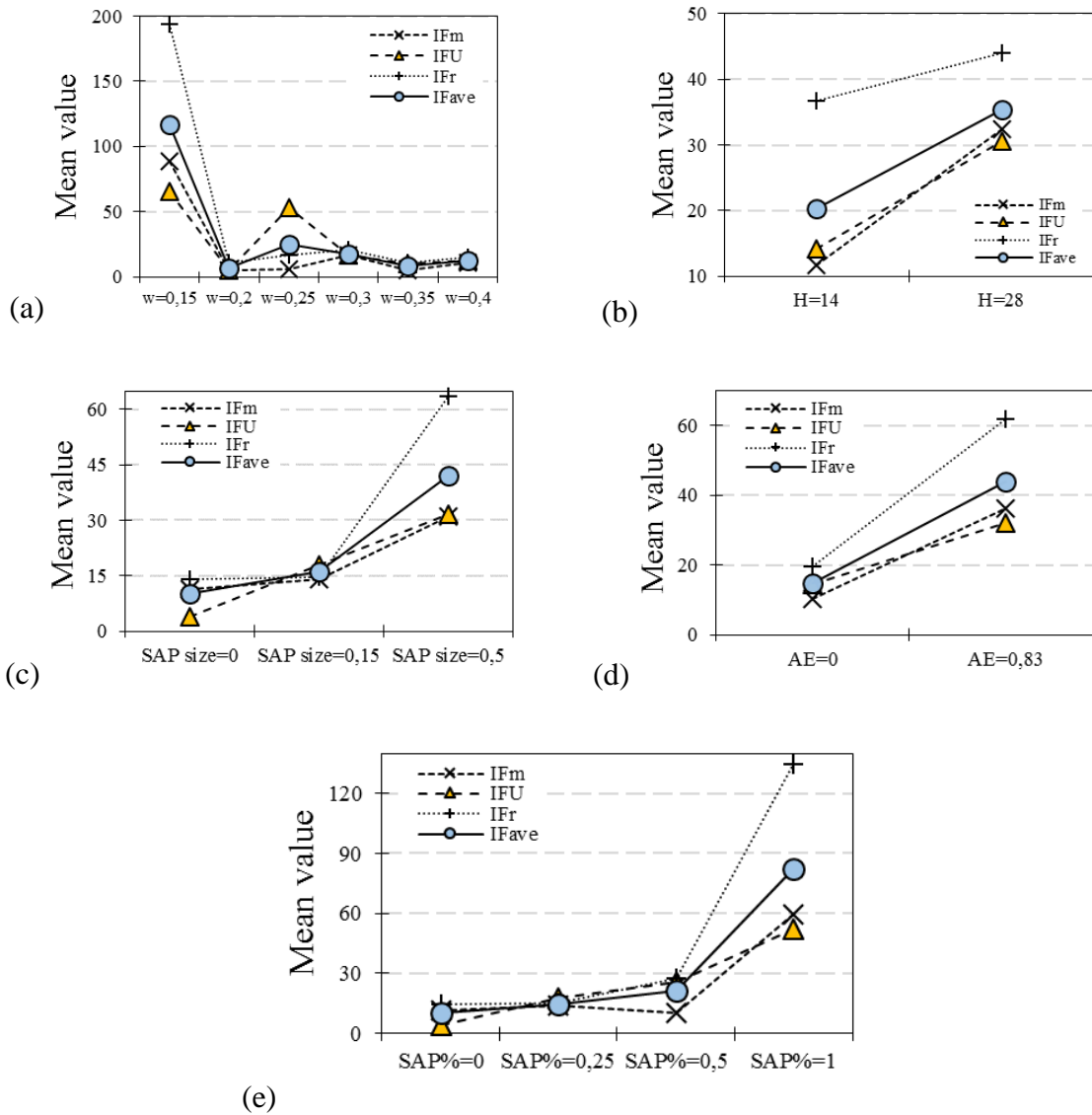
**Fig. 19** Healing products at the external crack surface of pull-out specimens of SAP-based NC mixtures with and without AE



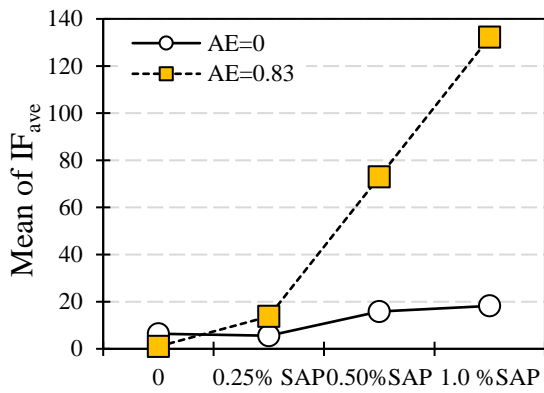
**Fig. 20** SEM image analysis of healed products at the external lip of cracks



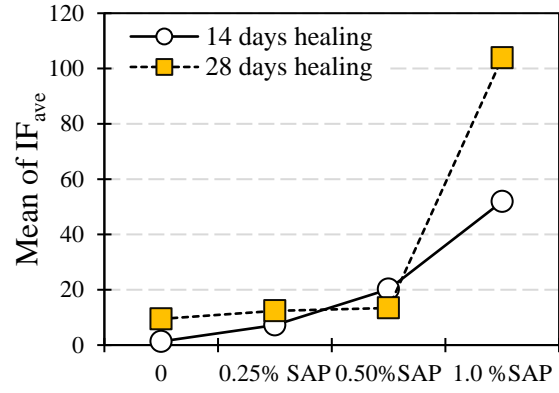
**Fig. 21** Comparison of mass percentage of elements found in the healing products at the internal and external surfaces of cracks



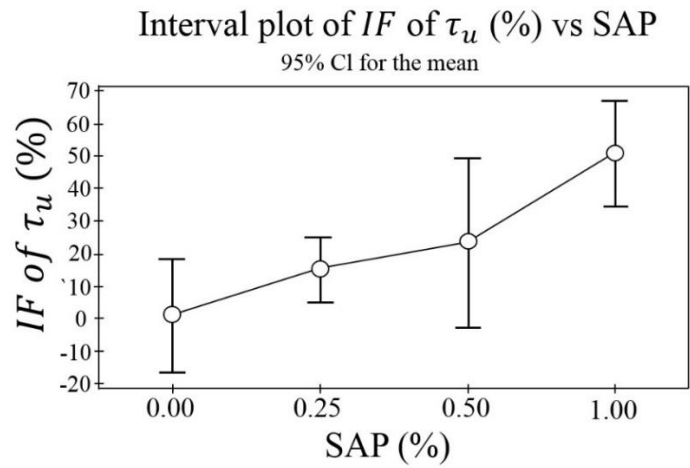
**Fig. 22** Main effects plot obtained by ANOVA with respect to: (a) crack width; (b) healing period; (c) SAP size; (d) AE dosage; (e) SAP percentage



(a)



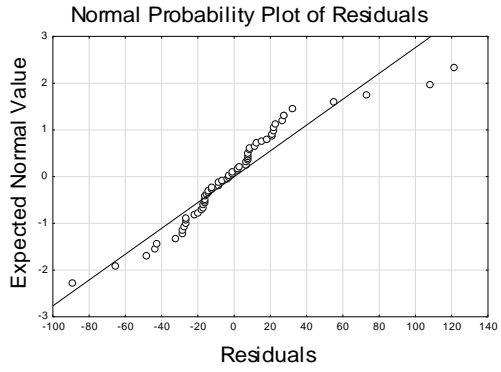
(b)



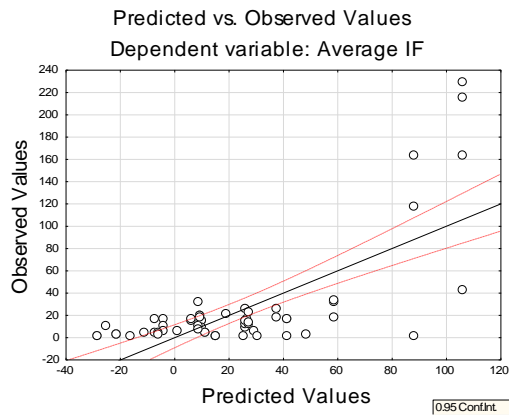
(c)

**Fig.** Erreur ! Il n'y a pas de texte répondant à ce style dans ce document. **23** Influence of SAP percentage based on ANOVA analysis:

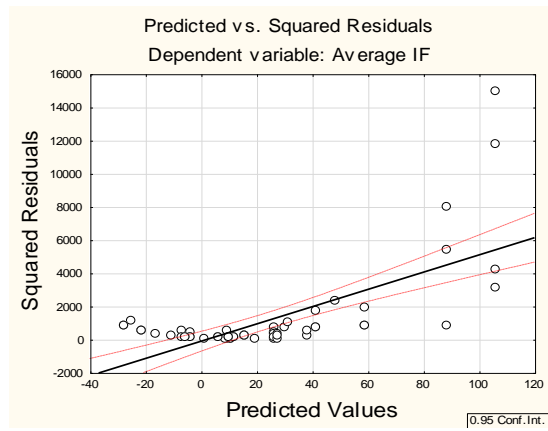
- (a) interaction plot with respect to AE;
- (b) interaction plot with respect to healing period;
- (c) interval plot of  $IF_u$



(a)



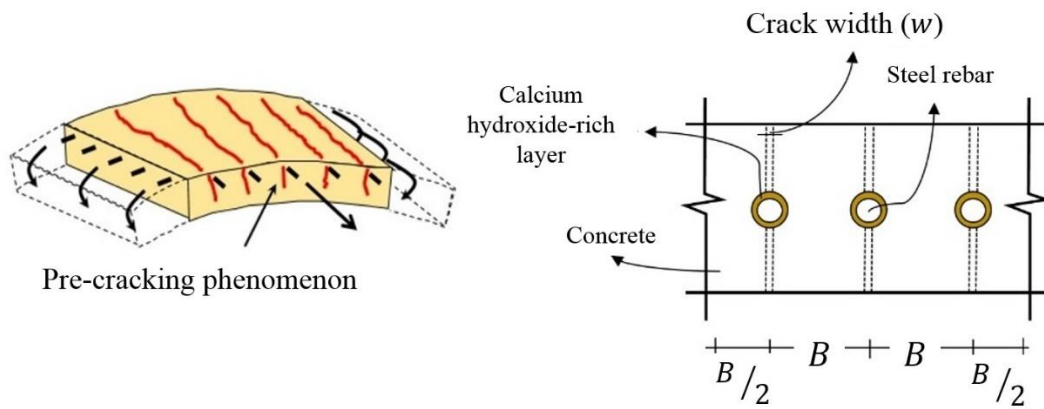
(b)



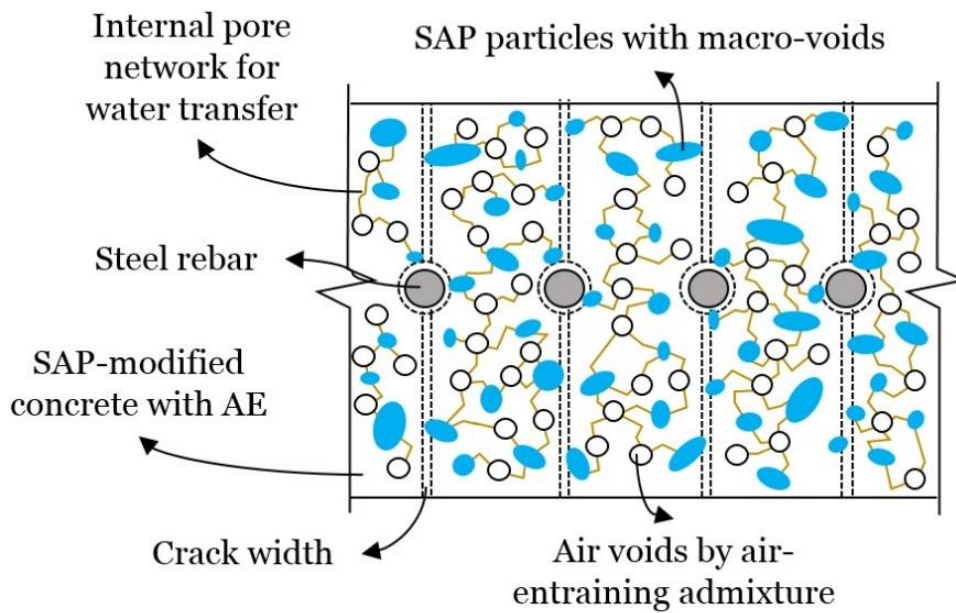
(c)

**Fig. 24** Performance of Eq. (7) for  $IF_{ave}$  by STATISTICA



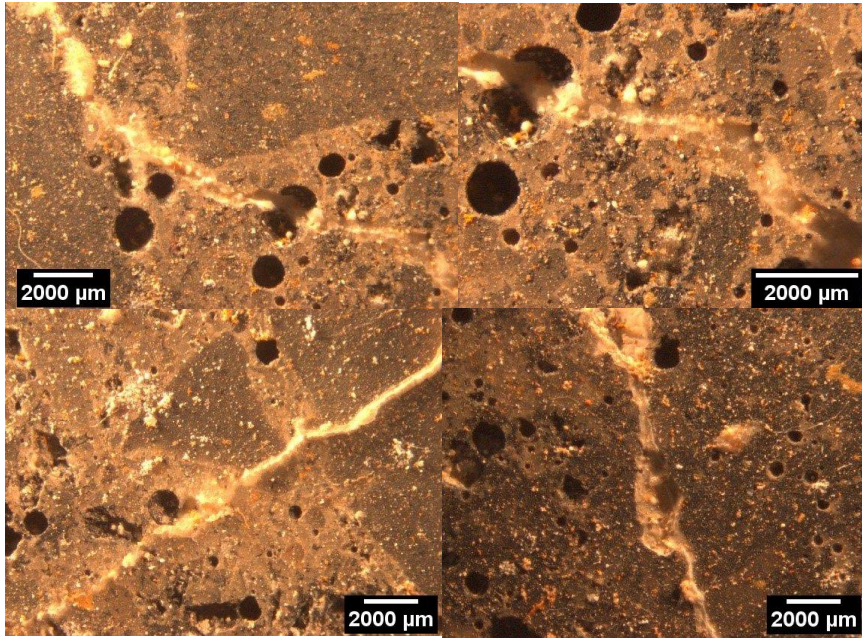


(a)



(b)

**Fig. 25** Schematic representation of the Buffon needle problem: (a) existence of  $\text{Ca}(\text{OH})_2$  around rebar for increasing the probability of crack healing; (b) internal pore network for water transfer in self-healing method of SAP concrete containing AE admixture



**Fig. 26** Distribution of SAP and AE pores around the crack path (1.00SAP1AE-healed)