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Authors' accepted manuscript

Article published in *Acta Materialia* vol. 109 (2016)

<https://doi.org/10.1016/j.actamat.2016.02.062>

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# Formation of Widmanstätten ferrite at very high temperatures in the austenite phase field

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## Abstract

Compression tests were carried out on a 0.06wt%C-0.3wt%Mn-0.01wt%Si steel at temperatures high in the austenite phase field. Eight deformation temperatures were selected in the range from 1000 to 1350 °C at 50 °C intervals. The quenched samples were examined using optical microscopy and EBSD techniques. It was observed that dynamic transformation took place and that the volume fraction of transformed ferrite first decreased with temperature (up to 1050 °C) and then increased as the delta ferrite temperature domain was approached. The EBSD results revealed the presence of Widmanstätten ferrite plates under all testing conditions, right up to 1350 °C.

Keywords: thermomechanical processing, dynamic transformation, Widmanstätten ferrite

## 1. Introduction

The transformation of austenite to ferrite during deformation above the  $A_{e3}$  temperature was first studied by Yada and co-workers in the 1980's [1, 2]. In their pioneering work, Yada et al. showed that DT ferrite could be formed as high as 166 °C above the  $A_{e3}$ . They also demonstrated the occurrence of this unusual phenomenon in real time by performing in-situ X-ray examinations while simultaneously deforming by torsion testing [3]. Follow-up work by Chen and Chen in 2000 [4] showed that DT ferrite retransformed back into austenite on prolonged holding, 30 °C above the  $A_{e3}$ . More recently, researchers in various countries have reported on other aspects of the dynamic transformation of austenite [5-10].

The dislocation density introduced by working was initially taken to be the driving force for dynamic transformation. For example, Sun et al. [11] in 2008, calculated the Gibbs energy increase in the deformed system to be 22.3 Jmol<sup>-1</sup> and concluded that this was responsible for DT. Somewhat similar results were obtained by Hanlon et al. [12], who justified the presence of dynamically transformed ferrite in this way at temperatures up to 10 °C above the  $A_{e3}$ . Ghosh et al. [13] extended the temperature range proposed by Hanlon and co-workers [12] by allowing for the distribution of dislocations to be inhomogeneous in nature. By increasing the estimated local stored energy to 197 Jmol<sup>-1</sup>, they were able to extend the predicted temperature range for the occurrence of this phenomenon up to 100 °C above the  $A_{e3}$ .

One limitation of the inhomogeneous distribution model is that it is unable to explain how strains as low as 10% can lead to the initiation of DT. This difficulty was

resolved by introducing the concept of mechanical activation by the applied stress, which can more readily account for the displacive nature of the forward transformation [14- 16]. In the most recent version of this approach, Aranas et al. [17- 19] proposed that the driving force for the transformation is the flow stress difference between the strain hardened austenite and the yield stress of Widmanstätten ferrite that takes its place. As will be shown below, such softening can provoke dynamic transformation at temperatures right up to the upper limits of the austenite phase field.

The objective of the present investigation was, therefore, to determine the characteristics of dynamic transformation at temperatures very high in the austenite phase field (up to 480 °C above the  $A_{e3(p)}$  in the present case). For this purpose, compression tests were performed on a 0.06wt%C-0.3wt%Mn-0.01wt%Si steel using a Gleeble 3800 thermomechanical system. The tests were conducted in the temperature range 1000 to 1350 °C (with intervals of 50°). Strains of 0.3 and 0.65 were employed in the tests and the strain rate was held constant at  $1\text{s}^{-1}$ . After water quenching, the specimens were polished and etched for examination by means of optical and electron back scattered microscopy. Double differentiation was also employed to identify the critical strains necessary for the initiation of dynamic transformation. The present observations indicate that the Fe-C phase diagram must be modified so as to apply to the case of dynamic loading.

## 2. Experimental Procedure

### 2.1 Compression testing

The plain C-Mn steel was received in the form of hot rolled plates with thicknesses of 12.5 mm. Cylindrical compression samples with dimensions of 15 mm X 10 mm were machined from these plates with the cylinder axes parallel to the rolling direction. The composition of this alloy is shown in Table 1 together with the respective paraequilibrium and orthoequilibrium  $A_{e3}$  temperatures [13]. These were calculated using the FSSel database of the FactSage [20] and were validated using the Thermo-Calc thermodynamic software [21].

The compression tests were carried out in a vacuum and the Gleeble 3800 (Dynamic Systems Inc. USA) thermomechanical simulator was interfaced with QuikSim software that controlled the heating rate, cooling rate, quenching medium, strain, strain rate and temperature. The thermomechanical schedule employed is displayed in **Fig. 1**. Here the specimens were heated at the rate of  $4.5\text{ }^{\circ}\text{C s}^{-1}$  to test temperatures in the range  $1000\text{ }^{\circ}\text{C}$  to  $1350\text{ }^{\circ}\text{C}$  and held for 3 minutes in order to fully austenize the microstructure before deformation. These were water quenched immediately after straining. Note that, a K-type thermocouple was used for the experiments carried out over the range  $1000\text{ }^{\circ}\text{C}$  to  $1250\text{ }^{\circ}\text{C}$ . For the compression tests above  $1250\text{ }^{\circ}\text{C}$ , an R-type thermocouple was employed. The data were later processed into stress vs strain curves obtained directly by the above software.

The first set of compression tests involved the imposition of a strain of 0.3 applied at the rate of  $1\text{ s}^{-1}$  over the temperature range 1200 to  $1350\text{ }^{\circ}\text{C}$ . In the second set, a higher strain of 0.65 was applied using the same parameters, but over the wider

temperature range 1000 to 1350 °C. Note that these temperatures are high in the austenite phase field and approach the delta ferrite formation temperature of approximately at 1472 °C.

## **2.2 Metallography**

For microstructural examination, central cross-sections perpendicular to the longitudinal axis were cut from the compressed specimens. The latter were then mounted in a phenolic hot mounting resin. The mounted specimens were polished using SiC papers from 400 to 1200 grit. Finally, these were subjected to 3 and 1 µm diamond polishing. Thereafter, the specimens were etched with 2% nital for optical microscopy. For determination of the volume fraction of DT ferrite in the austenite, etching was also carried out using a 10% sodium metabisulfite ( $\text{Na}_2\text{S}_2\text{O}_5$ ) solution. MIP microstructure analysis software was then used to calculate the volume fractions.

For the EBSD analysis, the specimens from each temperature were polished in the same manner as was employed for optical microscopy. Later, the specimens were subjected to final polishing using 0.05 µm silica in a vibromet for 6 to 8 hours.

## **3. Results**

The stress-strain curves associated with deformation over the temperature range 1000 to 1350 °C are displayed in **Fig. 2**. Here the samples were strained to 0.65 at the rate of 1 s<sup>-1</sup>. All the curves display softening after the peak stress is attained. As shown by earlier workers [6, 14] this is due to the concurrent operation of dynamic transformation and dynamic recrystallization. Steady state flow was attained at a

strain of about 0.4. An interesting feature of these curves is their somewhat “flattened” shape prior to the peak. This is an indication of the initiation of dynamic transformation, which reduces the net rate of strain hardening once it is underway. The transformation softening process makes it possible to detect its initiation by means of the double differentiation technique, as will be shown in more detail below.

### 3.1 Mean Flow Stress

The areas under the flow curves of **Fig. 2** were determined by integrating up to a strain of 0.65. The mean flow stresses derived from these areas are illustrated in **Fig. 3**, where they are plotted against inverse absolute temperature. The linear dependence shown here is in agreement with the exponential stress law for creep, as given by [19,22]:

$$\dot{\epsilon} = B \exp(C\sigma) \exp\left(\frac{-Q}{RT}\right) \quad (1)$$

which can be expressed as

$$\sigma = \frac{\ln(\dot{\epsilon}/B)}{C} + \frac{Q}{CR} \left(\frac{1}{T}\right) \quad (2)$$

where B and C are material constants, Q is the experimental activation energy and R is the universal gas constant. This approach is commonly employed in rolling mills to determine the  $T_{nr}$  of various steels [23], where the data are generally assumed to extrapolate (approximately) to zero stress at the melting point. This is of course an oversimplification, as crystalline materials have non-zero flow stresses at the melting point. Here, it can be seen that the data extrapolate to about 4-5 MPa at the melting

temperature, which is more realistic, physically, than the zero values conventionally employed for simplicity.

### 3.2 Critical strains for the initiation of dynamic transformation

Double differentiation was applied to the flow curves of **Fig. 2** using the MATLAB software [24]. Most of the curves were fitted using a 9<sup>th</sup> order polynomial, although in the higher temperature cases, a higher-order polynomial was used due to larger data fluctuations under these conditions. This method is illustrated in **Fig. 4**, where the strain hardening rate ( $\Theta$ ) is first defined, **Fig. 4a**. Here the fitting was performed starting from the plastic region of the curve up to the vicinity of the peak stress, as shown by the thicker solid line. DT and DRX are normally initiated before the peak stress.

The dependence of  $\Theta$  on  $\sigma$  is plotted in **Fig. 4b**, which shows the two inflection points that correspond to the moments of initiation of dynamic transformation and dynamic recrystallization. The locations of these points were then determined more precisely by noting that they correspond to the following condition:

$$\frac{\delta}{\delta\sigma}\left(\frac{\delta\Theta}{\delta\sigma}\right) = 0 \quad (3)$$

The two minima seen in the plot of  $(-\partial\Theta/\partial\sigma)$  against stress displayed in **Fig. 4c** obey this condition. These minima represent the critical stresses at which dynamic transformation and dynamic recrystallization are initiated during deformation. The critical strains that correspond to these stresses were then evaluated by referring back to the initial flow curves, **Fig. 2** [25].



The critical stresses determined in this way over the temperature range 1000 °C to 1350 °C are shown in **Fig. 5a**. These both decrease with temperature [19]. The critical strains that correspond to these stresses are illustrated in **Fig. 5b**. The error bars are based on two sources of experimental error, namely: i) measurement errors associated with the Gleeble machine, and ii) the uncertainties inherent in the double differentiation method. In previous investigations, these have been observed to be about 5%.

Here the critical strains for DRX decrease with increasing temperatures in the normal way [19]. By contrast, the DT critical strains first increase with temperature to a maximum and then decrease as the delta ferrite phase field is approached. The average values for the DT and DRX critical strains are about 0.08 and 0.15, respectively.

### **3.3 Dynamic transformation microstructures**

As demonstrated in more detail elsewhere [16, 19], dynamic transformation involves the initial formation of near-identically oriented Widmanstätten ferrite plates followed by their coalescence into polygonal grains. In order to check if this sequence of events was followed at the much higher temperatures employed here, optical microscopy was performed on the samples deformed to the lower strain of 0.3. Examples of the colonies of ferrite plates formed under the present conditions are shown in **Fig. 6**. Here, the darker regions correspond to martensite (prior austenite) and the lighter regions to ferrite. It can be seen that the volume fraction of Widmanstätten ferrite increases with temperature, as will be demonstrated in more

detail below. There is also a tendency for the plate width to increase with temperature. It should be noted that the ferrite plates formed are mostly along the grain boundaries of the prior austenite, although plates can also nucleate within the grains [13, 15].

In order to support the above interpretation of the microstructure, Vickers hardnesses were measured in selected regions in the samples strained to 0.3. Examples of the values obtained in the 1200 to 1350 °C samples are presented in **Fig. 7**. These values are consistent with the results obtained in tests carried out below 1000 °C [26]. Here, the average polygonal ferrite microhardness was about 170 HV and that of the martensite was 263 HV. The latter value is consistent with martensite hardness values in the range 200 – 300 HV expected in low C steels [27]. By contrast, the hardness of the Widmanstätten ferrite plates was somewhat higher than for polygonal ferrite at 203 HV vs. 174 HV, as seen in the sample deformed at 1300 °C (**Fig. 7c**).

The microstructures associated with the samples deformed to a strain of 0.65 are illustrated in **Fig. 8**. Here appreciable amounts of ferrite are present, which are homogeneously distributed throughout each specimen. The volume fraction of DT ferrite was calculated using the MIP software and at least 15 micrographs were scanned for each condition for this purpose. As mentioned earlier, the darker and lighter regions correspond to martensite (prior austenite) and ferrite, respectively.

The result of these measurements are displayed in **Fig. 9**. Here, it can be seen that the volume fraction of ferrite first decreases to a minimum of about 10% at 1050 °C. It then increases with temperature to about 25% at 1200 °C.

### 3.4 High magnification (EBSD) microstructures

The optical micrographs in the previous section indicated that Widmanstätten ferrite plates continued to be formed in the samples deformed at the highest temperatures in the austenite phase field. The orientations of these plates were characterized by means of the electron backscattered diffraction (EBSD) technique. An inverse pole figure map of some of the plates formed at 1200 °C ( $Ae_3(p) + 330$  °C) is illustrated in **Fig. 10 a**. This sample was strained to  $\epsilon = 0.3$  at  $1\text{ s}^{-1}$ . Here, the black regions are martensite (prior austenite) and the plates can be seen to be present in colonies of similar orientation [28].

On increasing the magnification to 7500X (**Fig. 10b**), the plates can be seen more clearly. Their widths fall in the range  $1 - 2\text{ }\mu\text{m}$ ; these are nearly an order of magnitude thicker than the 200 nm plates formed at 900 – 1000 °C [26, 27]. The coalescence of the plates into polygonal ferrite is illustrated in **Fig. 10c** for  $\epsilon = 0.65$  at  $1\text{ s}^{-1}$ . It is likely that the coalesced plates of **Fig. 10c** were formed early in this experiment, for instance at a strain of 0.10 to 0.15, while the ‘fresh’ plates of **Fig. 10b** were formed closer to the final experimental strain of 0.3, e.g. at  $\epsilon = 0.25$  to 0.30. As described earlier [16,18], Widmanstätten ferrite plates form by means of a shear process on habit planes and along shear directions that are well-aligned with respect to the applied stress. Thus the plates in Fig. 10c are associated with high

Schmid factors in the most suitably oriented grains. As these plates are almost identically oriented and have parallel habit planes, they readily coalesce into polygonal grains upon further straining [15]. Such coalescence involves the removal or dissolution of the dislocations located at the boundaries of the plates, a process that is driven by the excess free energy of the dislocations and is a recovery process.

The widening of the plates is probably associated with the increased diffusivity of C in ferrite over this temperature range. This hypothesis can be evaluated by calculating the carbon diffusion distance under the present conditions. This is specified by the following relationship:

$$\bar{X} = \sqrt{(Dt)} \quad (4)$$

where  $\bar{X}$  is the mean diffusion distance,  $D$  the carbon diffusion coefficient in ferrite and  $t$  the time. The diffusion coefficient is in turn given by:

$$D = D_0 \exp (-Q/RT) \quad (5)$$

where  $D_0 = 7.9 \times 10^{-3} \text{ cm}^2\text{s}^{-1}$  (for carbon diffusion in ferrite) and  $Q = 75.6 \text{ KJmol}^{-1}$  [29].

According to this relation, the diffusivity increases by a factor of 4.8 when the temperature is increased from 900 to 1200 °C. In a similar manner, the diffusivity increases by a factor of 8.6 over the range from 900 to 1350 °C. The plates formed at 900 °C are about 200 nm or so thick [16]. Thus, the above diffusivity ratios

suggest that, for equal diffusion times, the plate thicknesses at 1200 and 1350 °C should increase to 440 and 600 nm, respectively, at these two temperatures.

Thus the increase in the rate of carbon partitioning cannot account for the full increase in plate thickness if the plate growth time is held constant. A further factor that may be playing a role is the increasing recovery rate associated with the increase in temperature. The plates form in sequences of self-accommodating pairs, the second of which is induced so as to relieve the internal stresses developed during accommodation of the first member of the pair [28]. As the rate of development of the internal stress depends on the recovery rate, larger strains and therefore times (and amounts of plate growth) are probably associated with the higher temperature tests.

### **3.5 Perpendicularity of the DT ferrite plates**

When Widmanstätten ferrite plates form in the absence of an applied stress, their orientations are essentially random, that is within the limits set by the Kurdjumov-Sachs and other correspondence relations. In this way, all 24 K-S variants have an equal probability of appearing. By contrast, under dynamic transformation conditions, two habit planes/shear direction combinations are favored in each grain; those that lie closest to the plane and directions of maximum resolved shear stress [28]. Some examples of the presence of such perpendicular plates are provided in **Fig. 11**. Here the loading direction is vertical in the micrographs. These plates can be expected to have been aligned close to the maximum shear stress planes (inclined at 45° with respect to the direction of applied stress) when they were

formed. However, during compression, these plates gradually rotate away from their initial orientations by an amount that increases with the amount of strain undergone beyond the critical strain applicable to the grain in question. It can also be observed that regions with near identical orientations have coalesced into polygonal grains on further straining.

### **3.6 Plate disintegration**

During these very high temperature experiments, the plates were subjected to more “break-up” than that takes place at the lower temperatures studied to date [16-19, 30, 31]. Some examples are provided in **Fig. 12** illustrating the microstructures of samples strained to  $\epsilon = 0.3$  at 1250 and 1350 °C. For reference, an EBSD micrograph of a sample deformed to  $\epsilon = 0.3$  at the somewhat lower temperature of 1200 °C is also presented here. The rate of plate disintegration can be seen to increase with temperature. Similar trends were observed in both the low strain (0.3) and high strain (0.65) samples.

## **4. Discussion**

### **4.1 The Gibbs energy barrier to dynamic transformation**

The observation that the critical strain for DT displays a maximum at about 1050 °C in **Fig. 5 (b)** was initially surprising. So was the later finding that the volume fraction of ferrite is at a minimum at this temperature, **Fig. 9**. These trends can be given a physical interpretation by examining the free energy barrier to the transformation illustrated in **Fig. 13**. This depicts the temperature dependence of the Gibbs energy

difference between the stable austenite and the metastable ferrite as a function of  $\Delta T$  (experimental temperature – paraequilibrium temperature). This was calculated using the FSSkel database of the FactSage thermodynamic software [20].

As can be seen, this obstacle to the transformation is at a maximum at around 1080 °C, that is, approximately midway between the  $A_{e3}$  and the  $\delta$  – ferrite phase field. This indicates that when the temperature is increased beyond the obstacle peak it becomes easier and easier to form Widmanstätten ferrite dynamically. The decrease in obstacle height in turn means that less work hardening is required in the austenite to provide the amount of transformation softening necessary to overcome the obstacle. The increasing ease of ferrite formation as the delta ferrite phase field is approached is also consistent with the ferrite volume fraction data displayed in **Fig. 9**.

In the lower temperature range, from the  $A_{e3}$  temperature to 1080 °C, a critical strain increase of 0.01 per 21 °C was observed. That is, higher driving forces are necessary because of the increase in obstacle height. This requires more work hardening and therefore increases the critical strain. Over the higher temperature range, from 1080 °C to the delta ferrite formation temperature, a critical strain decrease of 0.01 per 50 °C was detected. In this case, lower and lower driving forces are necessary to initiate the transformation. This in turn requires the application of less and less work hardening for the initiation of dynamic transformation.

## 5. Conclusions

1. The critical strains for the initiation of dynamic transformation and dynamic recrystallization were calculated using the double differentiation method. The DRX strains decreased with increasing temperatures in the conventional manner. By contrast, the critical strains for DT increased initially with temperature but then decreased as the temperatures approached the  $\delta$ - ferrite phase field. This is consistent with the shape of the Gibbs energy obstacle to the transformation, which is at a maximum approximately midway between the  $A_{e3}$  and the  $\delta$ - ferrite phase field.
2. Optical micrographs confirmed the presence of dynamically formed ferrite plates at temperatures as high as 1350 °C ( $A_{e3(p)} + 480^\circ$ ). The ferrite volume fraction increased with the magnitude of the temperature interval above the Gibbs energy peak. This observation is also consistent with the tendencies displayed by the free energy obstacle and the DT critical strains.
3. The Widmanstätten ferrite plates produced at these very high temperatures have thicknesses of about 1 to 2  $\mu\text{m}$  and are therefore about an order of magnitude wider than the plates formed at 900 °C. This can be attributed to the higher diffusivity of carbon at these temperatures, as well as to the lower rate of work hardening. The latter is probably responsible for the somewhat slower rate of plate propagation at these very high temperatures.
4. The ferrite plates that form dynamically are frequently aligned along two approximately perpendicular directions. These correspond to the traces of planes



close to the planes of maximum shear stress at the moment of plate formation. There is considerably more plate disintegration and break-up than observed in the microstructures produced at lower temperatures.

### **Acknowledgements**

The authors acknowledge with gratitude funding received from the McGill Engineering Doctoral Award (MEDA) program and the Natural Sciences and Engineering Research Council of Canada.

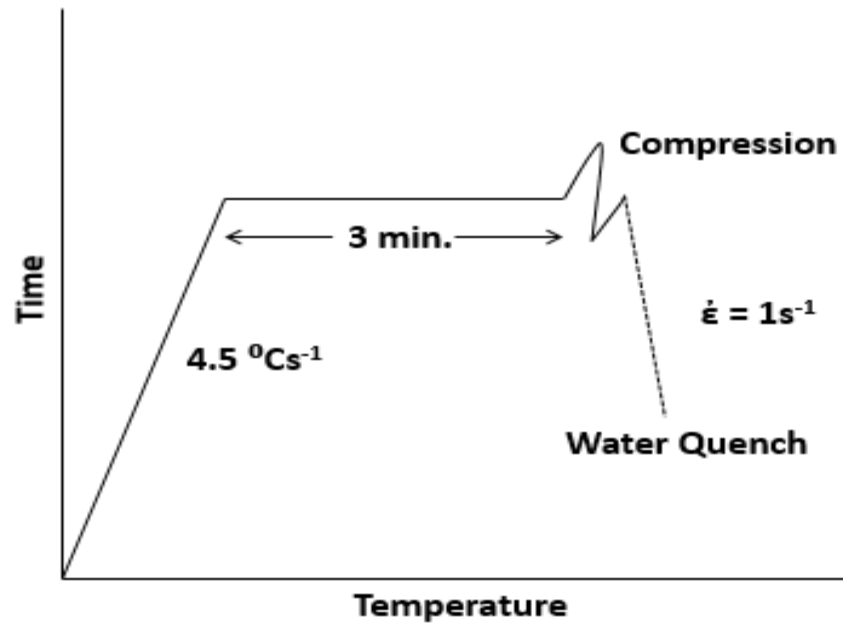
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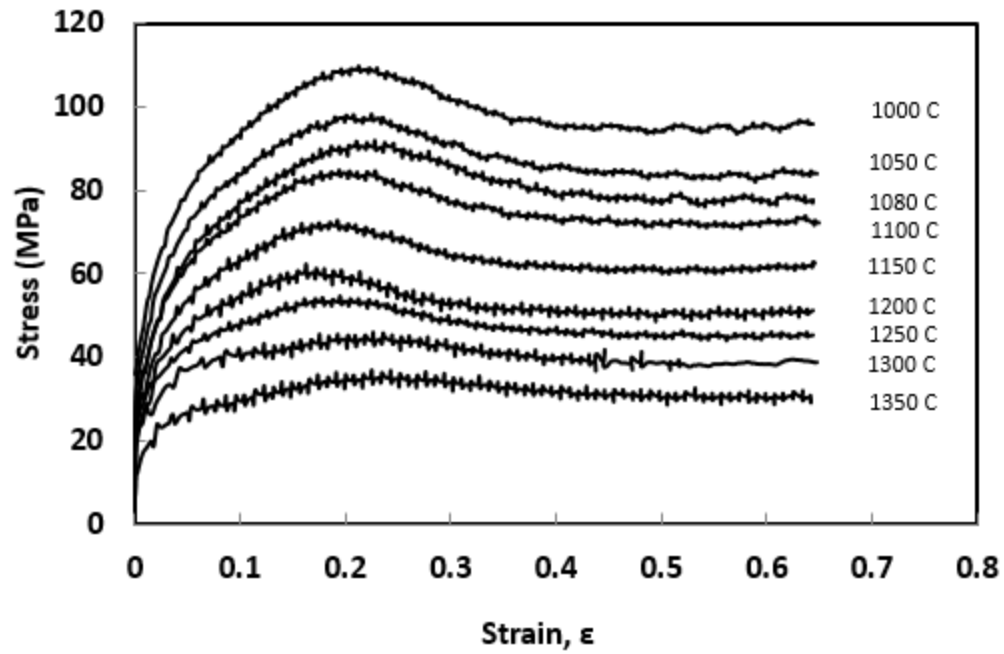
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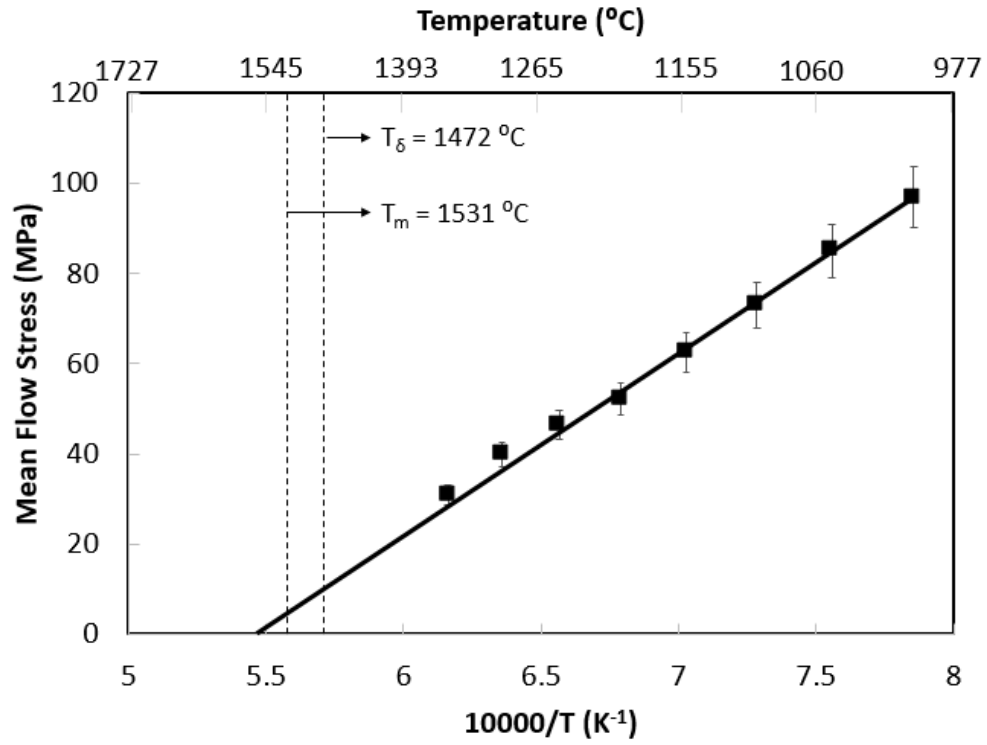
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**Fig. 1** Thermomechanical schedule of the compression tests carried out to strains of i) 0.3 at temperatures in the range from 1200 – 1350 °C and ii) 0.65 in the range 1000 – 1350 °C. The strain rate was  $1\text{ s}^{-1}$  in both series of tests.



**Fig. 2** Stress vs strain curves of the 0.06wt% C- 0.3wt% Mn- 0.01wt% Si steel compressed to a strain of 0.65 at  $1\text{s}^{-1}$  over the temperature range 1000 to 1350 °C. Flow softening of about 10% is generally observed after the peak stress is attained.



**Fig. 3** Mean flow curves calculated from the stress-strain curves of **Fig. 2** for the 0.06wt%C-0.3wt%Mn-0.01wt%Si steel.

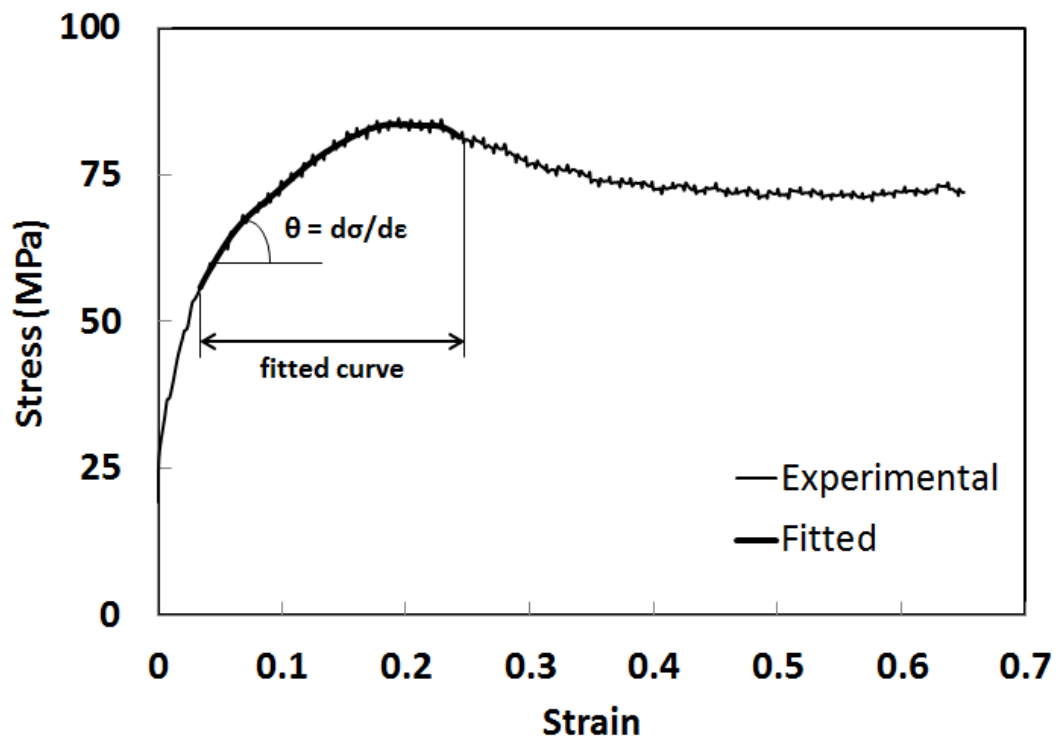


Fig. 4a

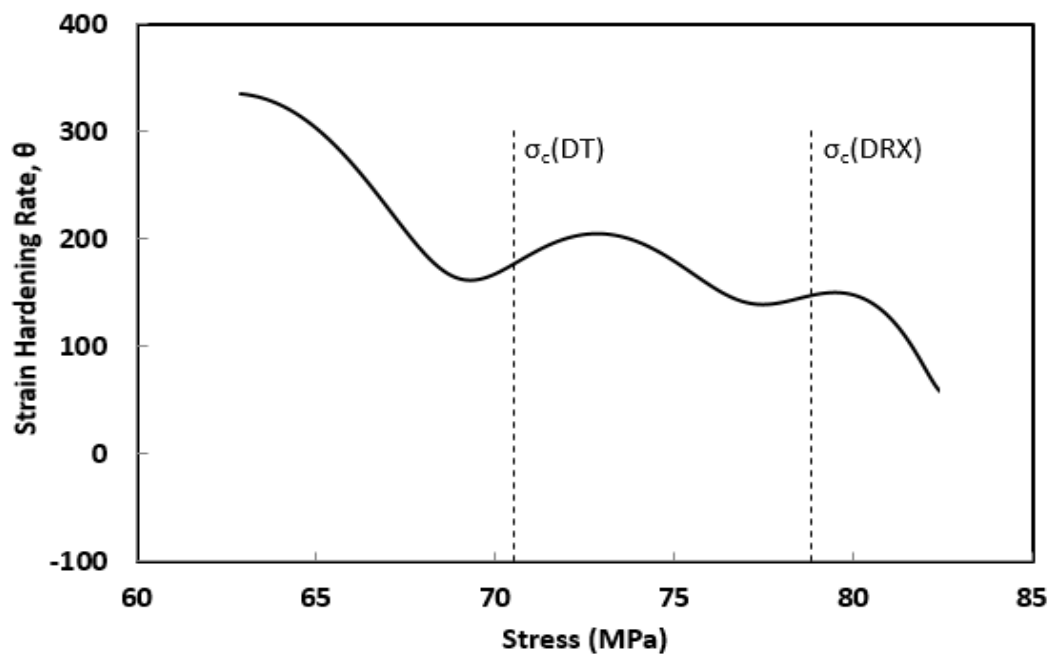
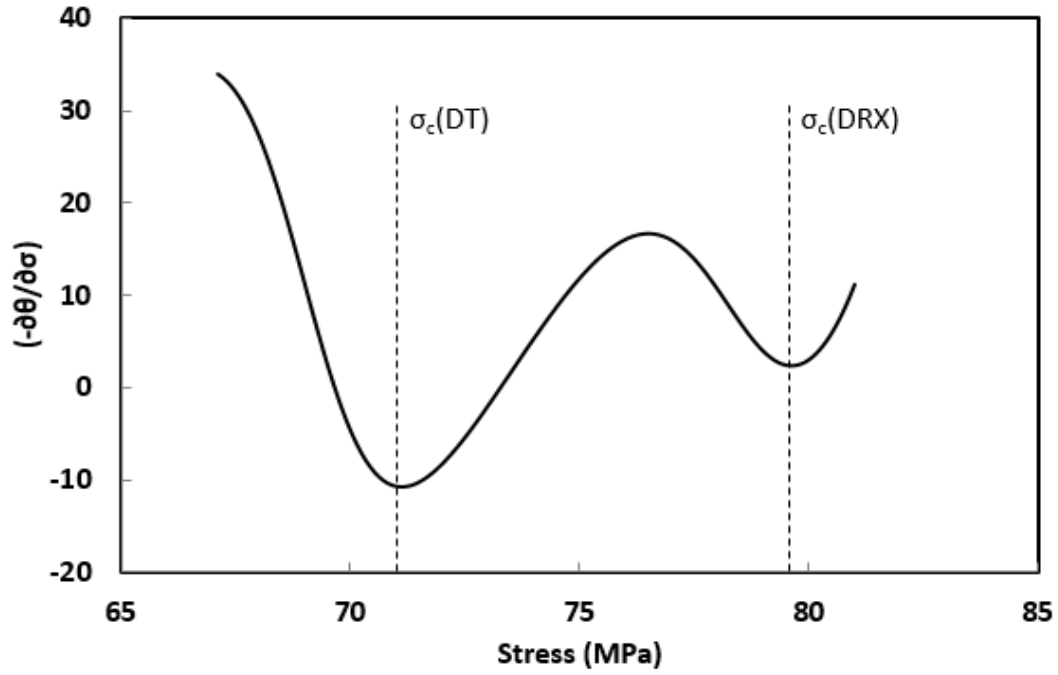


Fig. 4b





**Fig. 4c**

**Fig. 4** The double differentiation method employed in determination of the critical stresses and strains: a) definition of the strain hardening rate; b) plot of  $\Theta$  vs stress illustrating the presence of two (of the three) inflection points; and c) examples of the dependence of  $(-\partial\Theta/\partial\sigma)$  on stress. This experiment was carried out at 1100 °C.

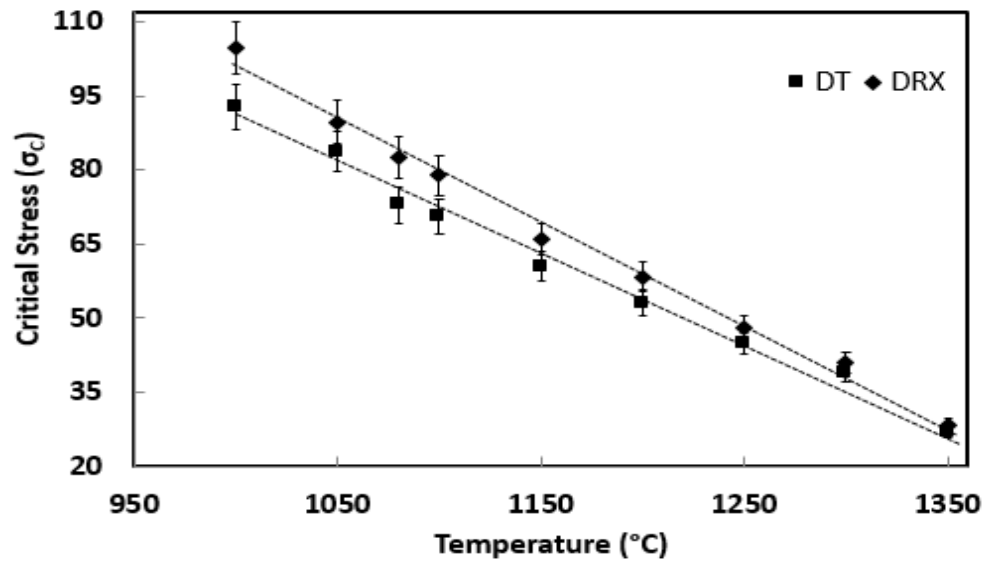


Fig. 5a

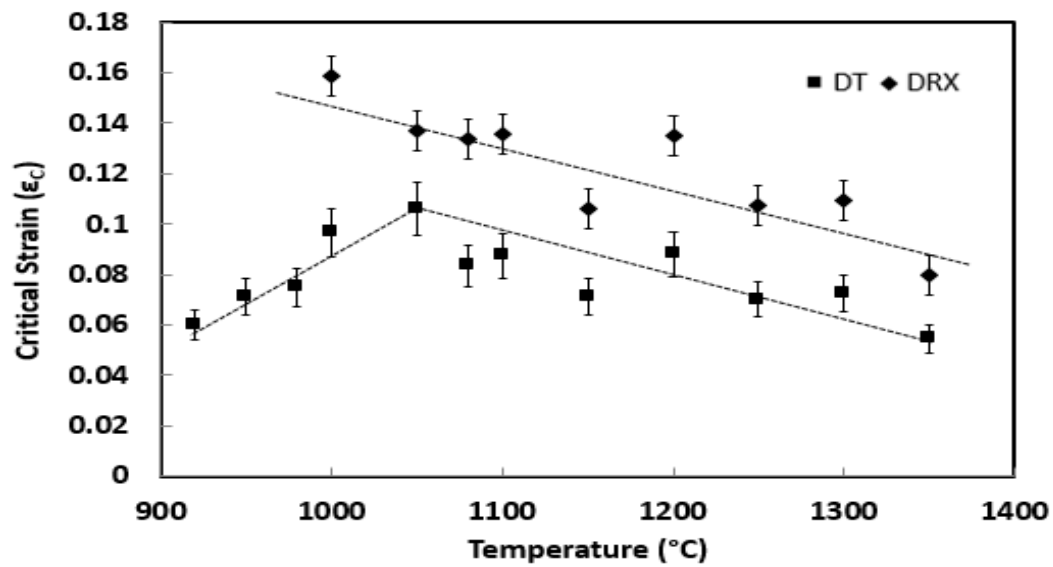
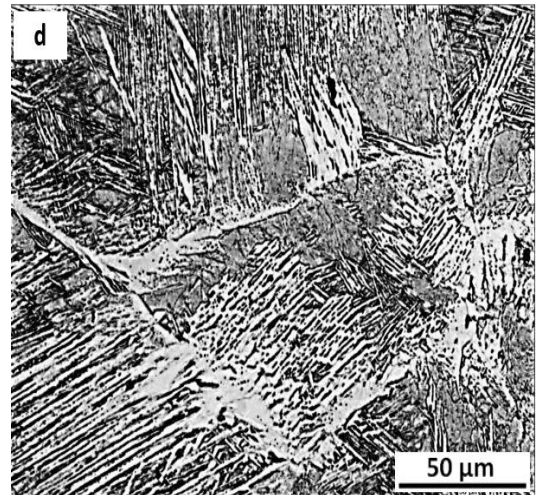
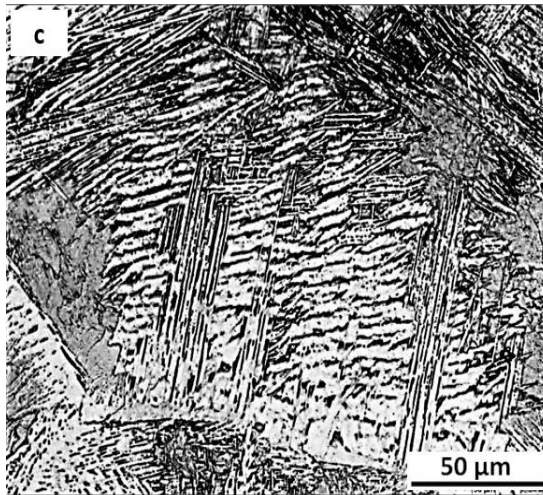
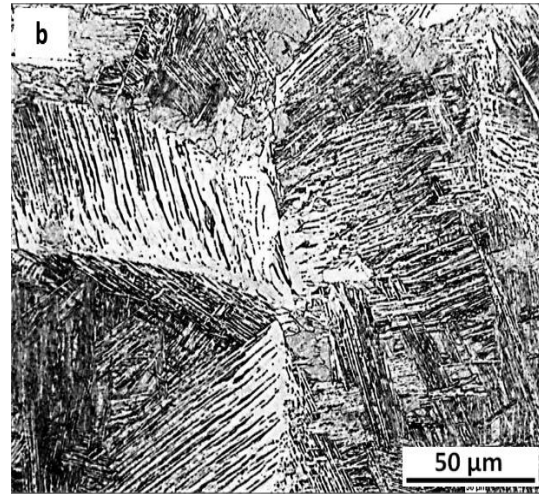
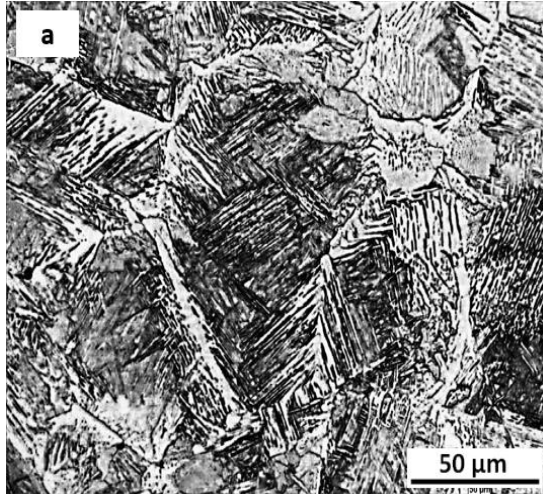
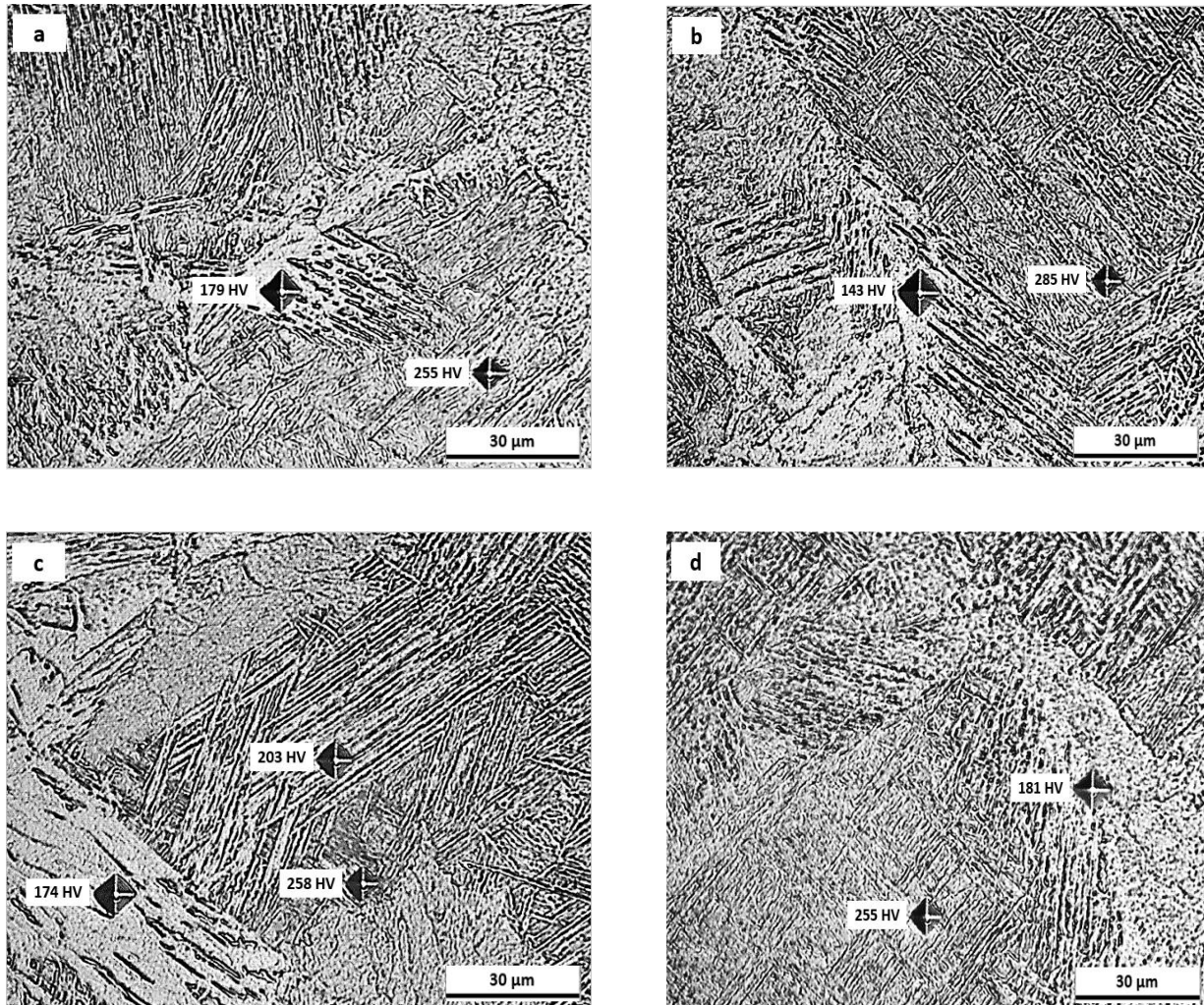


Fig. 5b

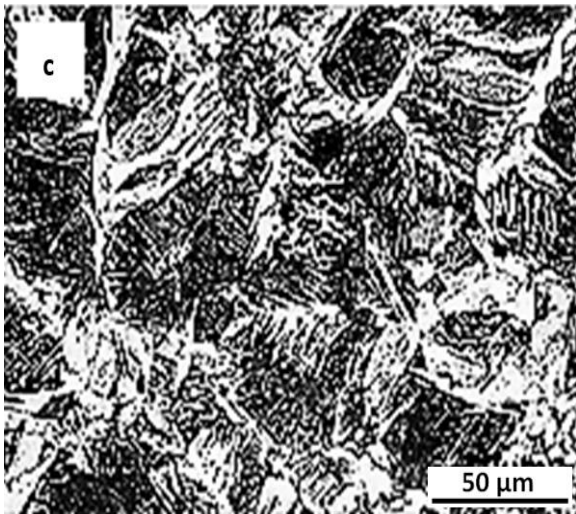
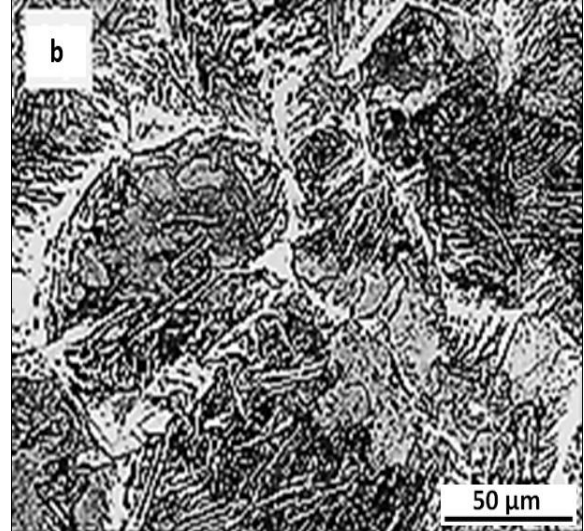
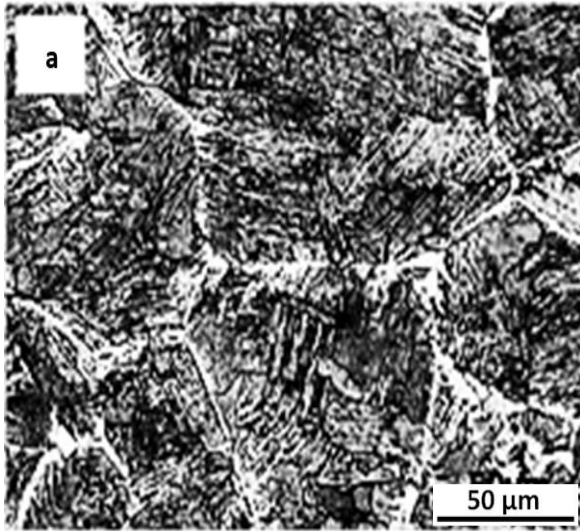
**Fig. 5** a) Critical stresses for dynamic transformation (DT) and dynamic recrystallization (DRX) determined over the temperature range 1000 to 1350 °C; b) critical strains over the same temperature range.



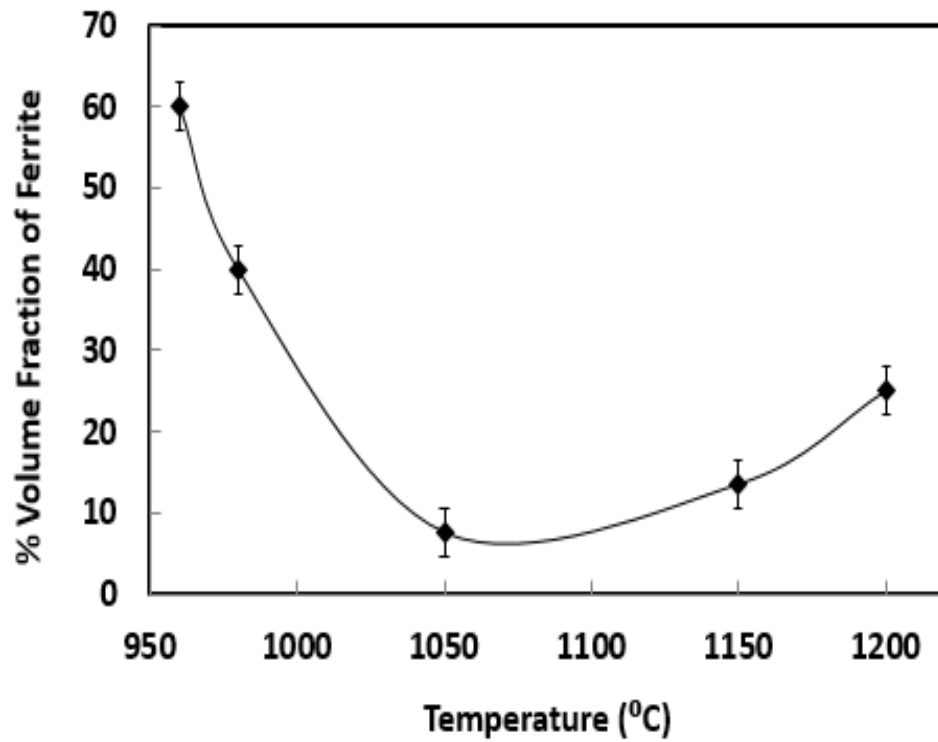
**Fig. 6** Optical micrographs at 500X of the present steel compressed to a strain of 0.3 at  $1s^{-1}$ : a) 1200 °C b) 1250 °C c) 1300 °C d) 1350 °C. The dark regions are martensite (prior-austenite) and the lighter ones are ferrite. The formation of plate-like Widmanstätten ferrite is evident even at 1350 °C.



**Fig. 7** Vickers microhardnesses of the polygonal ferrite, Widmanstätten ferrite and martensite (prior-austenite) in samples strained to 0.3 at a) 1200 °C b) 1250 °C c) 1300 °C d) 1350 °C.



**Fig. 8** Optical micrographs of the present steel compressed to a strain of 0.65 at  $1\text{s}^{-1}$  at:  
a) 1050 °C b) 1150 °C c) 1200 °C. The volume fraction of ferrite increases with temperature. The darker and lighter regions correspond to martensite (prior austenite) and ferrite, respectively.



**Fig. 9** Volume fraction of ferrite vs temperature at a strain of 0.65. The volume fraction is lowest (about 7.5 %) midway between the  $Ae_3$  and the  $\delta$ -ferrite phase field.



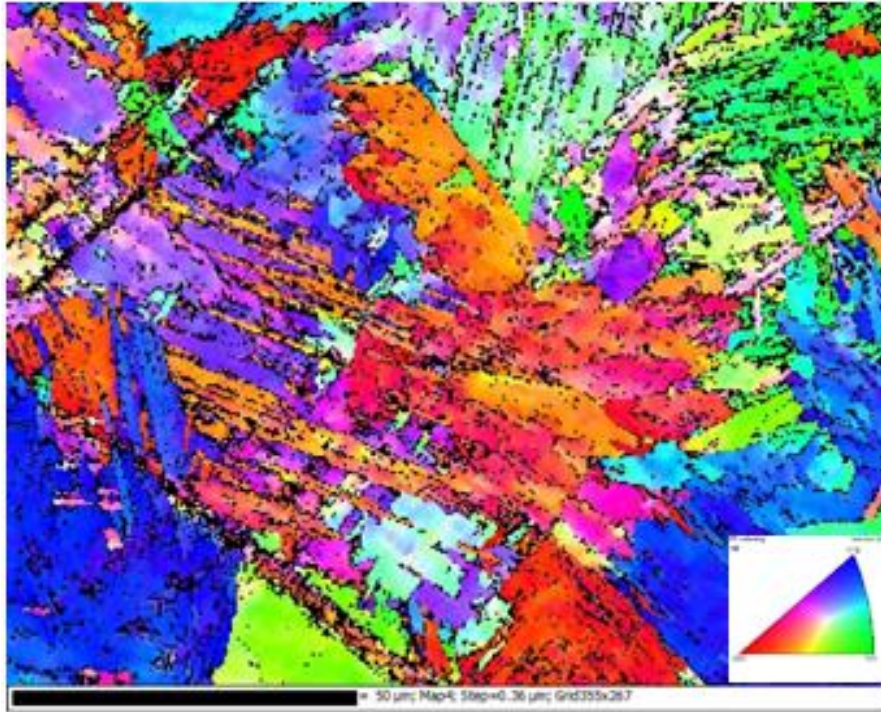


Fig. 10a

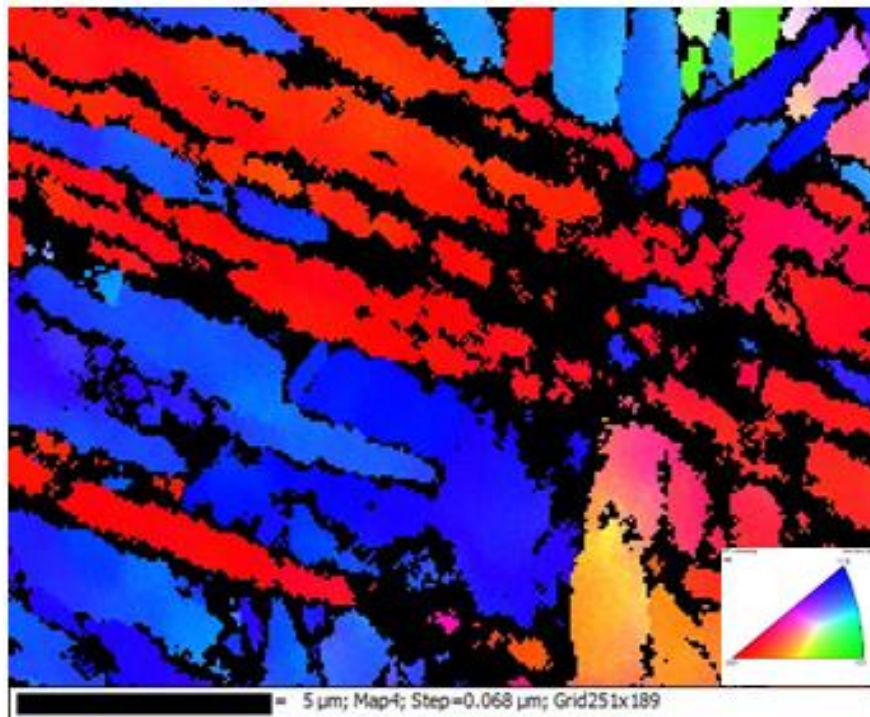
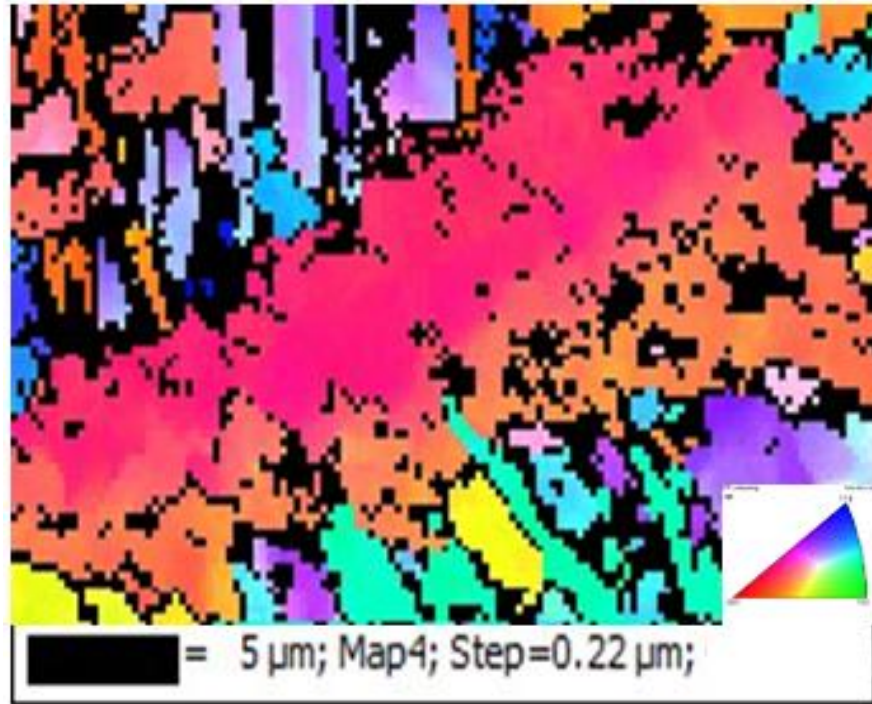


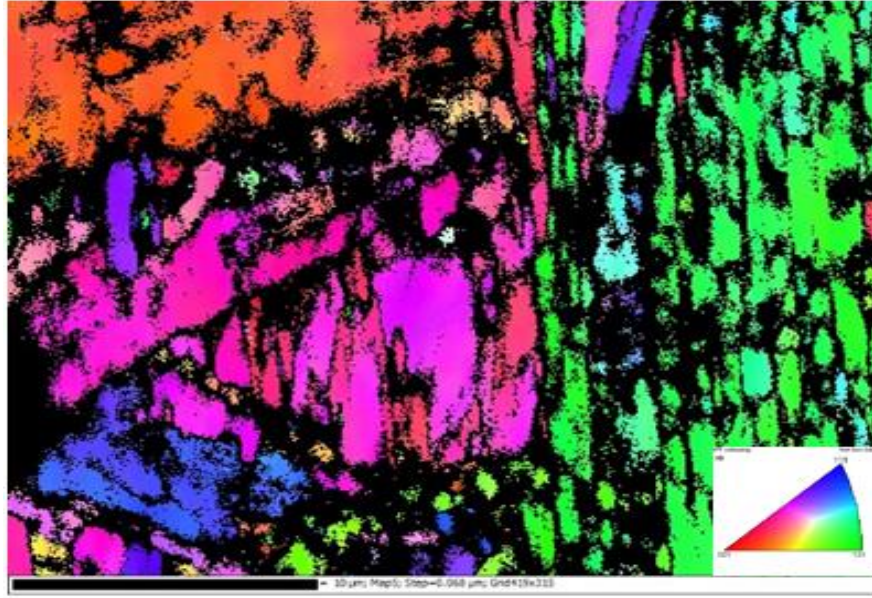
Fig. 10b



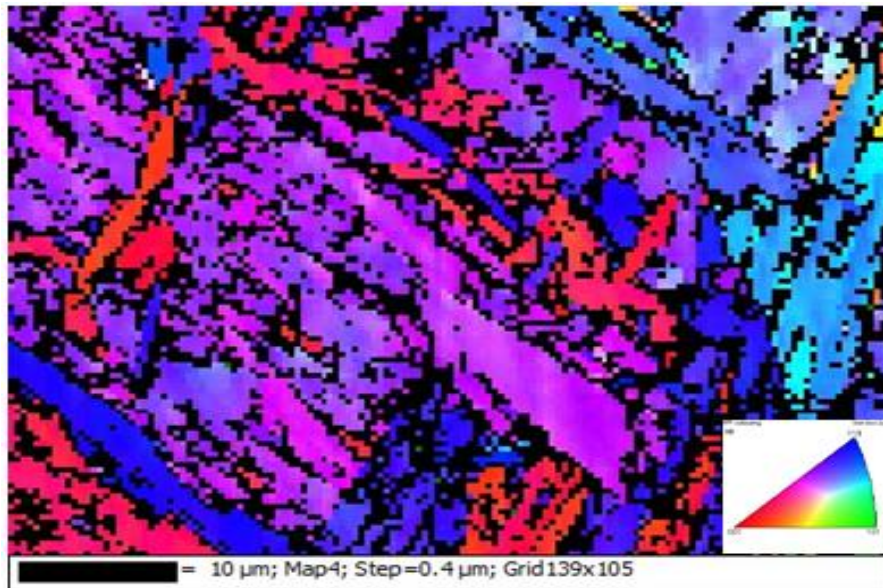
**Fig. 10c**

**Fig. 10** Self-accommodating plates in sample strained to  $\epsilon = 0.3$  at 1200 °C: a) 1000X, b) 7500X, c) Coalescence of plates in sample strained to  $\epsilon = 0.65$  at 1350 °C and  $1\text{s}^{-1}$ .





**Fig. 11a**



**Fig. 11b**

**Fig. 11** Widmanstätten ferrite plates in samples strained to  $\epsilon = 0.65$  at: a) 1250 °C and b) 1350 °C. Note the presence of approximately perpendicular plates.

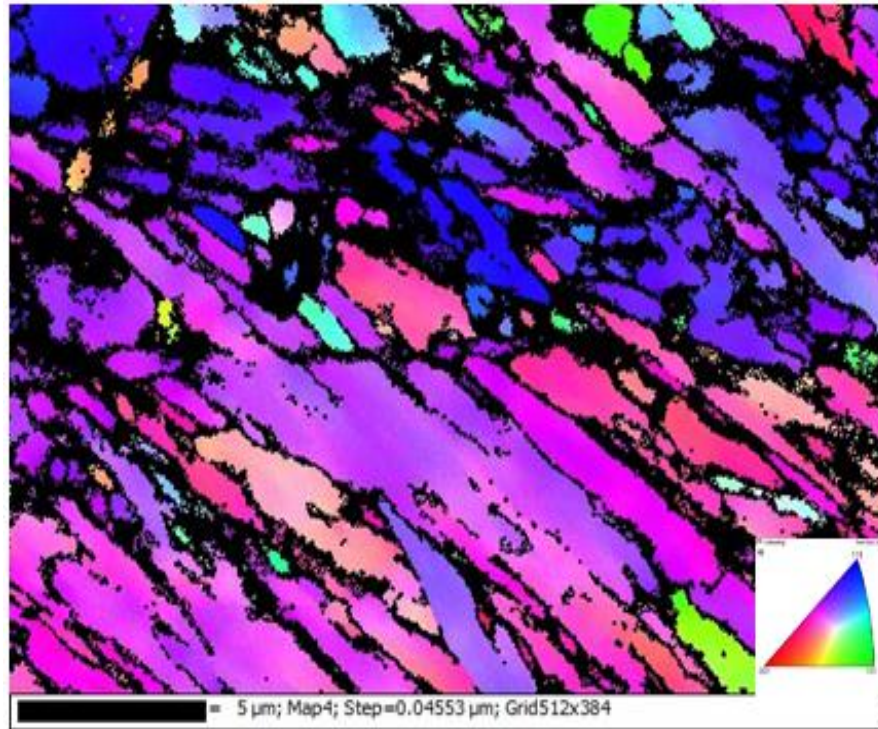


Fig. 12a

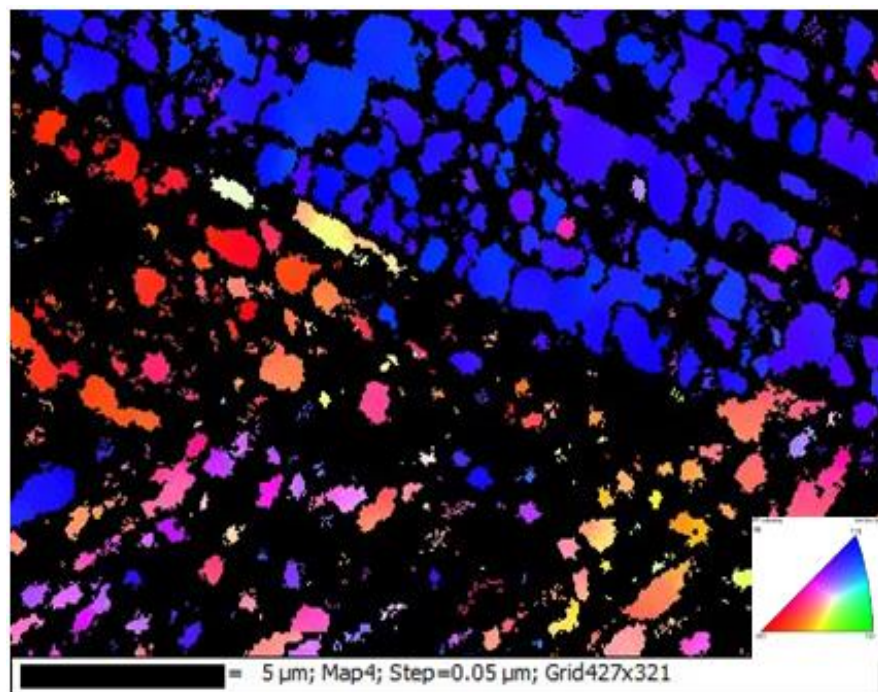
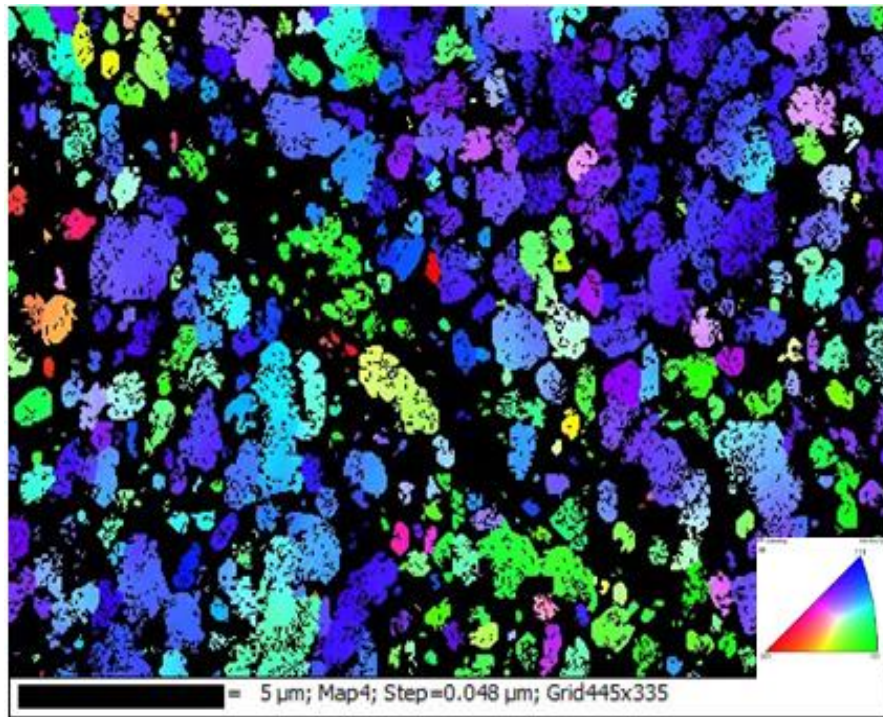


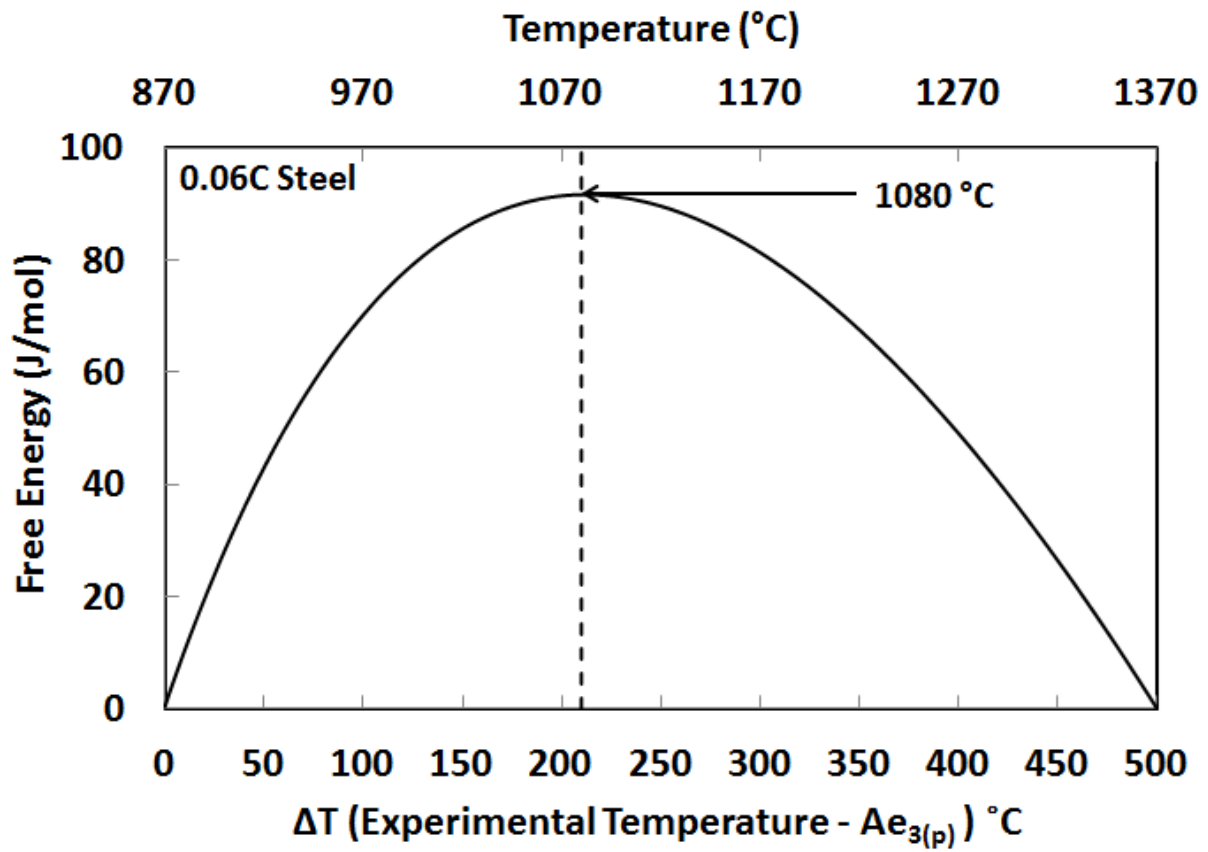
Fig. 12b





**Fig. 12c**

**Fig. 12** Increasing disintegration of the ferrite plates as the temperature is increased: a) 1200 °C b) 1250 °C c) 1350 °C.



**Fig. 13**  $\Delta G_{(\alpha-\gamma)}$  vs  $\Delta T$  ( $Ae_{3(p)}$  – experimental temperature) for the present steel showing the Gibbs energy obstacle opposing dynamic transformation.

## **Table**

Table 1. Chemical composition (weight %) and equilibrium transformation temperatures (°C)

<b>C</b>	<b>Mn</b>	<b>Si</b>	<b>Orthoequilibrium Ae<sub>3</sub></b>	<b>Paraequilibrium Ae<sub>3</sub></b>
0.06	0.30	0.01	877 °C	870 °C